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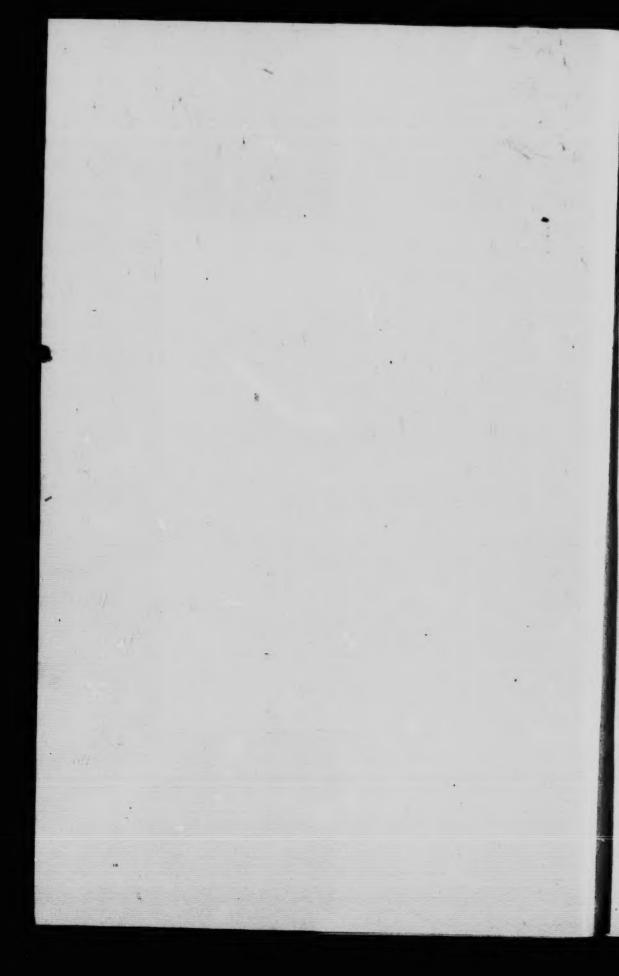
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		4	5	6	



COMPANION

TO THE

PUBLIC SCHOOL ARITHMETIC.

FOR THE USE OF TEACHERS AND PRIVATE STUDENTS.

WM. SCOTT, B.A.,
PRINCIPAL OF THE TORONTO NORMAL SCHOOL,

AND

CHARLES A. BARNES, M.A.,
PUBLIC SCHOOL INSPECTOR.

TORONTO: CANADA PUBLISHING COMPANY, LIMITED, 1901. PA 106 S36

Entered according to the Act of Parliament of Canada, in the year 1901, by the CANADA PUBLISHING COMPANY (Limited), in the Office of the Minister of Agriculture.

PREFACE.

This is a work intended for the use of teacher, and private students.

In preparing the Public School Arithmetic, it was deemed advisable to omit the answers to the purely mechanical examples. This book gives the answers to all the examples so that the teacher may be saved the trouble of working them.

The time of the teacher is so fully occupied by the ordinary school duties, that it is not always possible to find an opportunity for solving all the more difficult problems, hence a work such as this becomes a great convenience.

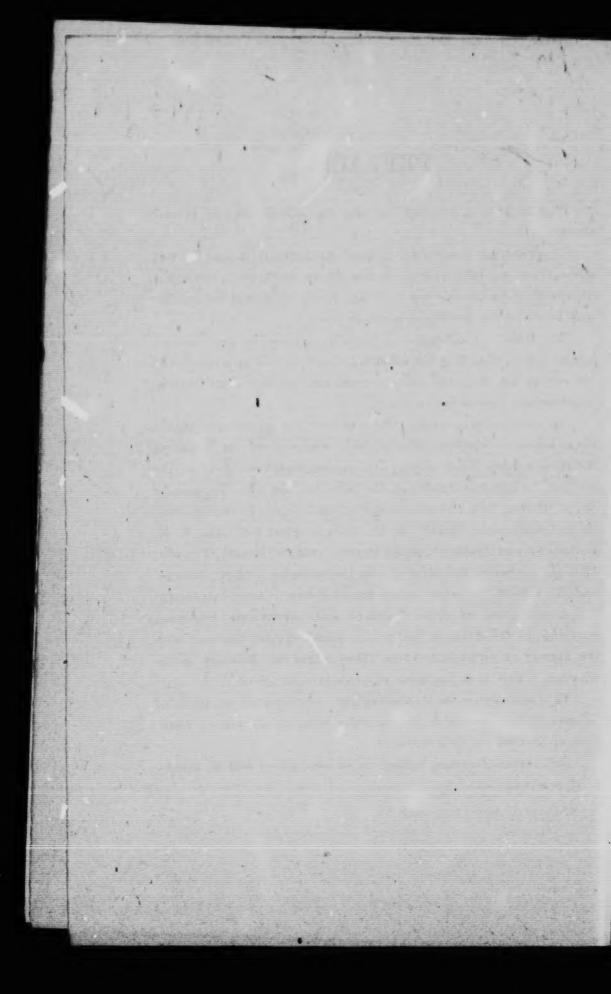
To supply the younger teachers with the experience gained from years of teaching this subject, Suggestions for Teaching Arithmetic have been added. In the preparation of these the authors desire to acknowledge the valuable aid given to them by W. H. Elliott, B.A., Vice-Principal of the Toronto Normal School; A. McIntosh, Head Master, R. W. Murray, First Assistant, T. M. Porter, Second Assistant, of the Provincial Model School, Toronto; Miss M. T. Scott, Principal of the Presbyterian Ladies' College, and W. Wilson, Principal of the Model School, Toronto Junction.

A collection of seven hundred and twenty-one problems, covering all the fields of the public school course, together with the answer to each, and where there might be difficulty in the solution, a hint as to the mode of procedure are given.

To facilitate certain mechanical calculations, a table of squares, cubes, square roots and cube roots of all integral numbers up to 1000 has been inserted.

Indications of errors, omissions or obscurities will be thankfully received.

TORONTO, July 24th, 1901.



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COMPANION TO THE PUBLIC SCHOOL ARITHMETIC.

PART I.

Answers.

EXERCISE I. PAGE 8.

1. Siz; ave; nine; seven; eight; four.

247 256

250 262

263 264 266

267 268

269

271

272

273

274

275

278

280

281

282

285

307

- 2. Fifteen; twenty-one; twelve; thirty-one; thirteen; seventeen.
- 3. Sixteen; sixty-one; seventy-one; eighty-one; eighteen; ninety-two.
- 4. Twenty-nine; ninety-three; thirty-nine; forty-seven; seventy-four; forty-nine.
- 5. Ninety-four; eighty-six; sixty-eight; seventy-six; sixtyseven; thirty-two.
- 6. Twenty-three; thirty-four; forty-three; forty-five; fifty-four; fifty-six.
- 7. Sixty-five; seventy-eight; eighty-seven; ninety-one; nineteen; twenty-four.
- 8. Forty-two; twenty five; fifty-two; twenty-six; sixty-two; eighty-two.
- 9. Twenty-eight; ninety-five; fifty-nine; sixty-nine; ninetysix; ninety-seven.
- 10. Seventy-nine; forty-eight; eighty-four; sixty-four; fortysix; one hundred.

EXERCISE II. PAGE 8.

- 1. Five hundred; seven hundred; eight hundred; two hundred; six hundred; four hundred.
- 2. Eight hundred and thirty; four hundred and seventy; six hundred and nine; seven hundred and fourteen; eight hundred and six; nine hundred and ninety.
- 3. Six hundred and seven; seven hundred and six; six hundred and seventy; seven hundred and sixty; nine hundred and one; one
- 4. Eight hundred and forty-seven; seven hundred and eightyfour; four hundred and seventy-eight; seven hundred and fortyeight; eight hundred and seventy-four; four hundred and eighty-

- 8. Two hundred and five; four hundred and six; five hundred and seven; seven hundred and five; five hundred and seventy; seven hundred and fifty.
- 6. Four thousand, seven hundred and five; five thousand, eight hundred and forty-three; nine thousand, one hundred and sixty-eight; two thousand and forty-nine; four thousand, nine hundred and five; four thousand, two hundred and thirty-one.
- 7. Eight thousand and seven; eight thousand and seventy; eight thousand, seven hundred; seven thousand and eighty; seven thousand and eight; nine thousand and forty-five.
- 8. Five thousand and sixty-eight; nine thousand and eight; six thousand, two hundred and two; one thousand, five hundred and eight; three thousand, seven hundred and forty-six; five thousand, seven hundred and eighty-six.
- 9. Two thousand, one hundred and thirty-four; one thousand, two hundred and thirty-four; one thousand, two hundred and forty-three; four thousand, three hundred and twenty-one; four thousand, one hundred and thirty-two; eight thousand and nine.
- 10. Nine thousand and one; one thousand and sixty-nine; nine thousand, six hundred and one; nine thousand, one hundred and six; nine thousand, six hundred and ten; nine thousand and eighty.

EXERCISE III. PAGE 8.

- 1. Forty thousand, eight hundred and seventy-six; fifty-four thousand and eighty-nine; thirty thousand and seventy; ninety-one thousand, one hundred and eleven.
- 3. Fifty-four thousand and eighty-nine; forty thousand and fifty-eight; thirty-nine thousand and seven; forty thousand, one hundred and six.
- 5. Eighty-one thousand and ninety-five; fifty-nine thousand, one hundred; ninety-five thousand, one hundred and one; thirty-seven thousand, six hundred and ninety-eight.
- 4. Eight hundred and nineteen thousand and seventy-five; eight hundred and ninty-one thousand, four hundred and ninety-two; two hundred and ninety-four thousand, seven hundred and sixteen; four hundred and ten thousand, one hundred and one.
- 6. Two hundred and ten thousand and ten; nine hundred and eighteen thousand and five; two hundred and thirty-one thousand and forty-six; two hundred and seventeen thousand and six.
- 6. One million, four hundred and seventy-six thousand, nine hundred and thirty-one; three million, seven hundred and ninety-six thousand, eight hundred and forty-two; nine hundred and ten thousand and ten; two million, one hundred and three thousand and one.
- 7. Three million, ninety-one thousand and six; four million, seven thousand and seven; one hundred and ninety thousand, one hundred; three million, nineteen thousand and forty-seven.

8. Seventeen million, ninety-one thousand, eight hundred and seven; ninety-three million, seven hundred and four thousand, nine hundred and five; nine hundred and three thousand, seven hundred and five; twenty-one million, ten thousand, one hundred

9. Forty million, ninety-seven thousand and six; thirty million, nine hundred and ten thousand, four hundred and five; nine million, three hundred and seventeen thousand, nine hundred and sixty; seventy million, six hundred and five.

10. Two billion, three hundred and nine million, four hundred thousand, one hundred and six; ninety-one billion, four hundred and ninety-one million, five hundred and ninety-one thousand, six hundred and ninety-one; one billion, thirteen million, two hundred and ten thousand and twelve; seven billion, sixty million, seven hundred thousand and one.

EXERCISE IV. PAGE 8.

1. 15; 21; 34; 75; 87; 19; 91.

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8. 100; 107; 316; 440; 909; 919; 991.

3. 1000; 1402; 8006; 8060; 2496.

4. 1011; 10604; 29470; 80990. 10. 536347972.

S. 804016; 291704. 11. 6000095148; 700090000001. 6. 1101001; 5004030.

12. 99000037004. 7. 954000806. 13. 864538217953. 8. 7707707.

14. 40004400414. 9. 146147047. 18. 490000000058798.

EXERCISE V. PAGE 9.

1. V; VI; VIII; IX; IV.

2. XV; XVI; XVIII; XIX; XIV.

s. xxv; xxvi; xxviii; xxiv; xliv.

4. XLIX; XLV; XCIV; XCVIII; XCIX.

s. CIX; CIV; CV; CCXIX; CCCXXIX. 6. COXL; CCXLIX; CCCXCIV; CCCLXXXVIII; CCCLVI.

7. CDIV; CDXLIV; CDXCIX; DLXXXIX; DXCIV.

8. DCCXCVI; DCCLXXXIX; DCCLXXVII; DCCLXVI; DCXCIX.

9. DCCCLXXV; DCCCLVII; DLXXVIII; DCCCXCIV:

10. CMLXXIII; CMLXV; CMXCIX; CMLXXXVII; CMXLIV.

11. MCM; MDCCCLXXXIX; MDCCCXCIX; MDCCCXLIX;

EXERCISE VI. PAGE 10.

1. 15; 90; 94; 69; 44; 90; 89; 110.

2. 111; 109; 144; 229; 504; 249; 709.

- 5. 404; 730; 540; 444; 529; 624.
- 4. 833; 484; 888; 484.
- S. 505; 430; 297; 244; 323; 555.
- 6. 1111; 1500; 1014; 990; 999; 1354.
- 7. 1290; 1555; 1444; 1009; 1222; 1490.
- 8. 2222; 947; 1906; 1400; 1909; 1555.
- 9. 1744; 1449; 1666; 2009; 1119.
- 10. 1599; 1900; 1901; 1899.

EXERCISE VII. PAGE 10.

- 1. 10; 100; 1000.
- s. CMXCIX.
- 3. The value of the letter to the left is to be subtracted from that to the right; IV; IX; XL; XC.
 - 4. I can be written to the left of V and X.
 - S. X can be placed to the left of I, V, L and C.
- 9, IX. 1; 2, II; 3, III; 4, IV; 5, V; 6, VI; 7, VII; 8, VIII;
- 7. V, L, and D are not be repeated. If repeated, they would give one of the next higher order.
- 8. The earth is ninety-two million, eight hundred and ninety thousand miles distant from the sun. The length of the equator is forty-three million, eight hundred and twenty-seven thousand and thirty-three yards. The cheese factories of Ontario produced one hundred and thirty-seven million, three hundred and sixty-two thousand, nine hundred and sixteen pounds of cheese in eighteen hundred and ninety-seven. The milk used in making the cheese was one billion, four hundred and fifty-five million, nine hundred and thirty-seven thousand, one hundred and forty-eight pounds. In eighteen hundred and ninety-eight, the ninety-eight creameries making returns to the Bureau of Industries produced nine million, eight thousand, nine hundred and ninety-two pounds of butter, valued at one million, six hundred and thirty-two thousand, two hundred and thirty-four dollars.
 - 9. V; X; XV; XXV; XXXV.
 - 10. 100; 110; 120; 130; 200; 210; 220; 230; 300; 310; 320; 330.

EXERCISE VIII. PAGE 11.

- 1. 76; 67; 77; 89; 69.
- 2. 988; 896; 1098; 999; 998.
- 3. 8999; 11636; 9987; 9998; 9968.
- 4. 18576; 20687; 20987; 19585; 19967.
- 5. 204996; 225469; 196678; 187896; 214829.
- 6. 7497. 7. 8789. 8. 7898. 9. 35888. 10. 39476.

EXERCISE IX. PAGE 12.

1. 49 ct. 2. \$47. 3. 300 bu. 4. 87 mi. 5. 124 mi. 6. 945769. 7. 969 yd. 5. 1367 mi. 9. 786. 10. 1668 pages.

EXERCISE X. PAGE 13.

1. 1433; 1330; 1020; 1314; 1312; 13312.

#. 15242; 14151; 14422; 14822; 183188; 182248.

J. 141722; 162222; 152651; 157526; 173245; 160518.

4. 184254; 198598; 178467; 206676; 189805; 172498.

5. 200396; 246121; 220250; 285326; 221632; 238796.

e. 249180; 192931; 820105; 217479; 276014; 258123.

7. 21164; 268399; 209846; 2634792; 25869; 242007. 8. 268655; 294395; 269181; 303376; 249409; 303787.

9. 277929; 304154; 289039; 289446; 308648; 285296.

10. 358489; 302884; 231960; 266875; 368887; 301027.

EXERCISE XI. PAGE 14.

1. 3432890; 4584711; 3328081; 5437312; 4801749.

\$. 3380656; 4164757; 4212613; 4644085; 5870413.

3. 3885336; 4150872; 3515001; 3929106; 3462627.

4. 1521900; 4812101; 5478906; 1109747; 14126839.

5. 40393623; 472198044; 465850334; 80717060; 57286686.

6. 52888932; 366547583; 377268904; 530116458; 436075579.

7. 30970654; 6772830; 4564359; 11556690; 39154681.

8. 65331127; 11813141; 12048191; 22755959; 28313249.

9. 186811552; 77223388; 29185155; 49579202; 467645729.

10. 62637126; 661580628; 723283090; 550941556; 746063693.

EXERCISE XII. PAGE 16.

1. 62075. 2. 10601. 3. 5186837. 4. 3309278. 8. 5199140. 6. 13786. 7. 2688. N. 10288. 9. 11947. 10. 13254.

EXERCISE XIII. PAGE 17.

1. 87432779. 8. 66751805. 8. 68318319. 4. 2384473.

5. 2000000. 6. 5263704. 7. 21044. 8. 53497. 9. 457709135.

EXERCISE XIV. PAGE 17.

1. 303. 2. 354 A. 3. 272 marbles. 4. 158 mi. 5. \$7353.

6. 1273 animals. 7. 885 trees. 8. MCXVII. 9. 46391. 10. 226.

EXERCISE XV. PAGE 18.

1. 40 marbles. 2. \$45. 3. 870 pages. 4. 300 mi. 5. 1000 et. 6. \$1900. 7. \$270. 2. 98 et. 9. 208 mi. 10. \$7856.

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EXERCISE XVI. PAGE 18.

1. 9054. 3. 90000. 3. 814 baskets. 4. 106 ft. 5. 170 et. 6. \$129. 7. 144 et. 8. 500 et. 9. 160 A. 10. 90 sheep; \$389.

EXERCISE XVII. PAGE 19.

1. \$9991. \$. \$350. \$. 197795. \$. \$52948276. \$. 3617 sheep. \$6. 510 mi. 7. \$100. \$8. \$120. \$9. 195 et. \$10. 3666.

EXERCISE XVIII. PAGE 20.

1. 76 mi. 2. 1159620. 3. \$45000. 4. 1171460 oranges. 5. \$3811. 6. 78. 7. \$31839. 8. \$12085. 9. \$33820. 10. \$88020.

EXERCISE XIX. PAGE 21.

1. 1990977. 8. 72720, 147720. 3. \$18565. 4. 154 yd. 5. 31136. 6. 131 et. 7. 365 days. 8. 12413. 9. 1832.

EXERCISE XX. PAGE 22.

1. 36; 18; 13; 26; 64; 35; 26.

\$. 541; 526; 833; 568; 851; 446.

3. 622; 482; 518; 811; 242; 517.

4. 4635; 2745; 5245; 4711; 1111; 3531.

6. 20582; 76464; 51236; 96835; 20142; 18156.

6. 14984; 15524; 26152; 26324; 52433; 834251.

7. 24780; 16330; 16230; 36310; 44002; 86443.

8. 6232; 24414; 3445; 3117; 2543; 46444.

9. 5215; 106542; 7724; 3232; 845462.

10. 125553; 505072; 224; 245000; 67302.

EXERCISE XXI. PAGE 23.

1. 111 cows. 3. 40 chickens. 5 \$23. 4. 113 pages. 5. 272 gal. 6. \$150. 7. 254 bbl. 8. 1252 sheep. 9. 433 A.

EXERCÍSE XXII. PAGE 23.

1. 55; 27; 23; 29; 24; 51; 25.

2. 185; 452; 193; 746; 581; 690.

3. 447; 582; 222; 547; 656; 423.

4. 2215; 1414; 2343; 3212; 2962; 3925.

5. 1345; 1254; 1365; 3312; 1524; 1018.

6. 18364; 25233; 38222; 35343; 17427; 27728.

7. 105054; 107014; 302073; 304022; 177244; 312816.

8. 226173; 114542; 234121; 213653; 132590; 679924. 9. 457022; 318234; 515255; G25223; 725675; 876899.

10. 491978; 261636; 294928; 680929; 281939; 577184.

EXERCISE XXIII. PAGE 24.

1. 545: 788. A. 022; 112. s. 1353; 5896.

170 et.

sheep.

nges.

13020.

4 yd.

1832.

ges.

A,

280.

4. 29597; 28655. S. 22610; 6779. 6. 387712; 476998. 7. 601; 479779.

.S. 322229; 199600. 9. 457710; 191188. 10. 185118; 409086.

EXERCISE XXIV. PAGE 24.

1. 3658; 4256; 5328. #. 5368; 4656; 4296.

3. 5257; 7766; 4454. 4. 3257; 775; 3252. 6. 6389; 2766; 2682.

6. 8157; 1444; 4474. 7. 4887; 822; 5275.

8. 4127; 2077; 6255. 9. 4549; 3885; 3786. 10. 5667; 1382; 2456.

EXERCISE XXV. PAGE 25.

1. 82423; 7775; 277553. 2. 20884; 60622; 443674.

3, 35524; 16653; 236387. 4. 23691; 15343; 378778.

8. 47171; 25665; 315829. 6. 55857; 38755; 350646. 7. 59094; 46558; 351705.

8. 42875; 37810; 382316. 9. 9795; 30542; 345467. 10. 6272; 30878; 434717.

EXERCISE XXVI. PAGE 25.

1. 4989050; 4997999. #. 1700261; 6088013.

3. 8974088; 75489688. 4. 99019119; 6363637. 5. 6821430; 7276195.

6. 798499; 4099996. 7. 7783440; 9797978.

8, 8526021; 18351936. 9. 999989; 4058809. 10. 3800909; 3770438.

EXERCISE XXVII. PAGE 25.

1. 74. 2. 286032. 3. 6319267. 4. 32299. 5. 676. 6. 2714. 7. 526084. 8. 2578. 9. 6667315. 10. 141998.

EXERCISE XXVIII. PAGE 26.

1. 80 sheep. 2. \$257. 3. \$468. 4. 24168 bu. 5. \$1779.

6. \$2168. 7. \$49. 8. 1432 mi. 9. 162482. 10. 158677 cows.

EXERCISE XXIX. PAGE 26.

1. \$807. 2. 39 marbles. 3. 13999 men. 4. \$3816.

5. 351636 min. 6. 439 pages. 7. \$21506957. 8. 6300636 ft. 9. 117993. 10. 83849884 lb.

EXERCISE XXX. PAGE 27.

1. 27 et. 2. 288. 3. \$11993. 4. \$35. 5. 1642. 7. 968 yr. 8. 3688 ft. 9. 1325 votes. 10. 3969356. 6. 89 Tr.

EXERCISE XXXI. PAGE 27.

1. 45. 2. \$198. 8. 215 bu. 4. \$3250. 8. \$32. 6. \$107950. 7. \$7178. 2. 5 mi., 137 yd. 9. 225 mi. 10. 2210.

EXERCISE XXXII. PAGE 28.

1. \$245. 2. 1950. 3. 1487 A. 4. 45 yr., 38 yr. 5. Loss, \$2410. 6. Jas. 31, Jno. 26. 7. 45 A. S. 70 da. 9. 18 marbles. 10. 21171, 14896, 18691.

EXERCISE XXXIII. PAGE 29.

1. 6746. \$. 12968. \$. 1606. 4. 2658225. \$. 6529. 6. 925856. 7. 2534. 8. 73699. 9. 2155. 10. 8453. 11. 23718. 13. 74128.

EXERCISE XXXIV. PAGE 31.

- 1. 6080408; 8604864; 846084; 680486; 6408604.
- 2. 1948468 | 9926482; 1759432; 19694912; 14169184.
- 3. 1536128; 1156984; 1416192; 1197492; 1985780.
- 4. 1726856; 1536994; 1401216; 734992; 1569984.
- 5. 10369362; 10363935; 13630368; 19603068; 10636892.
- 6. 26305425; 28942092; 26306368; 28454895; 23698458.
- 7. 13616586; 2536972; 16549616; 6713372; 27133748.
- 8. 21749956; 27156052; 3914596; 1383948; 16559056.
- 9. 1152280; 27160305; 17876320; 12682360; 6172835.
- 10. 22985225; 48412345; 39465430; 35404520; 38424815.
- 11. 28048225; 4475347); 27894780; 24488245; 43288245. 18. 22446384; 204, 26884; 22311858; 251844206; 25180824.

EXERCISE XXXV. PAGE 32.

- 1. 26254716; 41354790; 30484236; 22136562; 47081712.
- 2. 47345790; 28257882; 50944776; 41367474; 53267976.
- 3. 52199686; 53519851; 59197488; 63483546; 53794835.
- 4. 1719746; 26197948; 37944438; 29775494; 49045199.
- 8. 28615842; 28609378; 21636118; 34283578; 69135801.
- 6. 29136432; 25968520; 36836504; 18765080; 34821384. 7. 38352688; 71101248; 73876536; 63172344; 58606472.
- 8. ~1479736; 20505024; 12289688; 26452200; 40130584. 9. 11111085; 50789376; 18661185; 38111103; 51880568.
- 10. 27583101; 58310775; 72813627; 49219155; 70776783.
- 11. 15846201; 47805255; 28395837; 13806819; 46219419.
- 12. 76897450; 70000680; 95060780; 56789430; 76847960.

EXERCISE XXXVI. PAGE 33.

- 1. 757283586; 1135925349; 1514567132; 1898208915; 2271850698;
- 2. 957200648; 1435800972; 1914401296; 2393001620; 2871601944;
- 8. 757283668; 1135025502; 1514567836; 1893209170; 2271851004;
- 4. 986743668; 1405115502; 1873487336; 2341859170; 2810231004;
- 8. 8567201386; 4459001735; 5350802082; 6242602429; 7134402776; 8026203123.
- 6. 2431560780; 3039450975; 3647341170; 4255231365; 4963121560; 5471011755.
- 7. 4839170896; 5207004474; 6074688553; 6942672632; 7810506711; 8678340790.
- 8. 8891709845; 4070051214; 4748398083; 5426734952; 6105076821; 6783418690.
- 9. 2391890325; 2870268390; 3348646455; 3827024520; 4305402585; 4783780650.
- 10. 2091789230; 2510087076; 2928434922; 3346782768; 3765130614; 4183478460.

EXERCISE XXXVII. PAGE 33.

1. 73185; 186612; 87822; 170765.

107950.

82410.

25358.

74128.

- #. 94990; 122130; 169625; 284970.
- 3. 226752; 255096; 297612; 347214.
- 4. 201264; 431280; 469616; 517536.
- S. 60936; 63475; 91404; 159957.
- 6. 205024; 288315; 345978; 461304.
- 7. 368880; 384250; 461100; 537950.
- 8. 677950; 774900; 871650; 968500.
- 9. 346005; 415206; 484407; 622800.
- 10. 146250; 195000; 243750; 292500.

EXERCISE XXXVIII. PAGE 33.

- 1. 1649466; 2434926; 3220386; 4005846; 5576766.
- \$. 4153795; 4834745; 5515695; 6196645; 1293805.
- 3. 1026571; 1342439; 1500878; 2290048; 29217,79.
- 4. 5051124; 5633946; 6152010; 4144512; 3820722.
- 5. 11207664; 16524120; 21840576; 27731784.
- 6. 55361880; 87094880; 33881080; 62294320.
- 7. 29272750; 23147990; 62058230; 87008320.
- 8. 23515182; 31123035; 54407676; 54100288.
- 9. 395846112; 601940584; 494708876; 892826560.
- 10. 442875810; 616023720; 617415864; 783690063.

EXERCISE XXXIX. PAGE 34.

1. 1900 mi. 1. \$195695. 3. 607488 os. 4. 1622060 mi.

8. 63168 et. 6, 702 trees. 7. 2920 mi. 8. 95424 hills.

9. \$130455. 10. 75067 lemons.

EXERCISE XL. PAGE 34.

7. 1530000 et. S. 22076 yd. S. 2268 mails. J. 62640 mi.

8. 171216 in. 6. 383600 et. 7. 482040 et. 8. \$204000.

9. 525800 min. 10. 5285484 papers.

EXERCISE XLI. PAGE 35.

1. 43050. S. \$2341190. S. \$5. d. 553 et. S. \$516.

6. Gain, \$32. 7. 94720 ct. 8. 2472 ct. 9. 1087 mi. 10. Gain, \$61

EXERCISE XLII. PAGE 38.

1. 172484. 2. 233180. 3. 1062847. 4. 67419148. 5. 15408465 6. 2016978981. 7. 1123193115. 2. 68096083. 9. 50700. 10. 14254

EXERCISE XLIII. PAGE 36.

1. 55986805. 2. 1516. 3. 62985. 4. 9989001. 5. 7051253. 6. \$30613. 7. 57415 et. 8. 15725910 A. 9. 703 stooks, 8436 sheaves 10. 99693084.

EXERCISE XLIV. PAGE 37.

1. 12; 23; 48; 42.

J. 321; 238; 229; 292.

6, 117; 127; 41; 140.

7. 107; 121; 82; 185.

9. 91; 102; 81; 40.

g. 234; 236; 418; 473.

4. 121; 142; 184; 156.

6. 108; 61; 81; 160.

8. 121; 105; 116; 91.

10. 571; 821; 749; 301.

EXERCISE XLV. PAGE 37.

1. 214321; 104231; 121340; 212413; 231430.

\$. 78996; 67897; 175896; 268979; 157985.

\$. 182023; 52315; 154572; 288819; 248561.

4. 183692; 196181; 203878; 168627; 140668.

8. 36952; 100207; 148360; 71437; 185530.

6. 114126; 102057; 140292; 155246; 116667.

7. 102116; 135101; 88538; 45923; 90149.

8. 91016; 114830; 111420; 92654; 18567.

9. 23859; 92729; 52818; 76067; 60931.

10. 101281; 100406; 83171; 17687; 143688.

EXERCISE XLVI. PAGE 38.

- 1. 2000017; 1302078; 1044658-2; 835736-4; 696430; 596047-8;
- g. 3351700; \$234408-2; 1075051-2; 1340001-1; 1117234-2; 667659-3; 857925-6.

d.

ala, 963.

5408465.

. 14254.

253.

73.

56.

11.

01.

sheaves.

- 3. 2003933-1; 1355955-2; 1016966-3; 813673-2; 677977-5; 581123-6; 506483-8.
- 4. 3301933-1; 2261280; 1605066-3; 1356773-2; 1130644-3; 909123-6; 847963-8,
- 8. 1889028-2; 1041771-2; 833417-1; 694514-2; 595298; 520005-6: 462009-5.
- 6. 1859534-1; 1019650-3; 815720-3; 679767-1; 582657-4; 500025-3: 458178-1.
- 7. 1028547-1; 767660-2; 614126-2; 511773-4; 438663-1; 383830-2; 341183-4.
- a. 767603; 614062-2; 511735-2; 438680-2; 383801-4; .1156-8; 307041-3.
- 9. 1003169-2; 802535-8; 668779-4; 573239-5; 501584-6; 445863-1; 401267-8.
- 10. 767716; 614172-4; 511810-4; 428694-6; 383858; 341207-1; 307086-4.

EXERCISE XLVII. PAGE 38.

1. 16, 28, 44, 88 yd. 8. \$121. 8. \$75. 4. \$29 bbl. 5. 142 lb. 6. 524 lb. 7. 15065 lb. 8. 532 pk. 9. \$7625. 20. 370 t.

EXERCISE XLVIII. PAGE 30.

1. 480 mi. 2. 1760 yd. 3. \$13. 4. 18 hr. 8. 30 ct. 6. \$32. 7. 87 persons. 8. 362 mi. 9. 11625000 mi. a min. 10. 5642 pence.

EXERCISE XLIX. PAGE 39.

- 1. 1220-34; 1020-84; 876-58; 768-46; 684-10.
- 8. 556-17; 420-33; 243; 213; 180-54.
- 3. 3111; 2501; 2091; 1574-57; 1262-89.
- 4. 1725-18; 1482-21; 1299-24; 1156-47; 349-194.
- 8. 1481-255; 741-595; 659-377; 1174-92; 843-664.
- 6. 1566-216; 941-141; 2346-36; 776-550; 582-774.
- 7. 1188-529; 965-82; 847-460; 1296-121; 1577-390.
- 8. 824-106; 672-178; 582-568; 669-124; 494-460.
- 9. 1168-775; 1042-525; 1913-40; 2896-7; 1737-340.
- 10. 786-586; 1554-10; 801-424; 872-706; 1985-853.

EXERCISE L. PAGE 39.

- 1. 1082-870; 1071-192; 1057-416; 1012-964; 1048-438.
- #. 929-464; 896-573; 888-482; 880-509; 897-594.

- J. 1128-90; 1118-150; 1102-450; 1007-46; 1110-780.
- 4. 1456-466; 1433-317; 1421-50; 1413-666; 1417-5.
- 8. 1383-429; 1898-861; 1818-480; 1884-941; 1814-195.
- 6. 1443-225; 1411-224; 1425-465; 1464-266; 1466-204.
- 7. 2288-101; 2218-208; 2253-80; 2196-298; 2213-140.
- 8. 9456-40; 2364-256; 2617-274; 2360-200; 2492-42.
- 8. 20406-8; 26315-20; 34463-22; 50623-9; 52631-11; 27027-1.
- 10. 94906-9; 73021-10; 00067-1; 64977-4; 49671-8; 31065-22.

EXERCISE LI. PAGE 40.

- 1. 11550-5; 9625-5; 8250-5; 6000-5.
- #. 36519; 39215-6; 34346; 20066.
- 8. 21217-8; 17000-48; 17040-24; 15155-3.
- 4. 29745-20; 23238-29; 30656-29; 18591-5.
- 8. 27374-8; 26027-31; 20066-24; 16221-42.
- 6. 25000-7; 21428-31; 12500-7; 11111-16,
- 7. 13240-16; 9987-6; 7949-96; 6694-46.
- 8. 18116-18; 11942-38; 9837-18; 8744-18.
- 0. 9676-41; 4908-41; 3392-41; 3469-41.
- 10. 1975-185; 1646-85; 1410-665; 1234-485. .

EXERCISE LII. PAGE 40.

1. 6540. S. 301625. S. 480673. S. 150287. S. 481. S. 4788. 7. 61. S. 378. D. 9605. SD. 223689.

EXERCISE LIN. PAGE 40.

- 1. 184 da. R. \$3008. S. 2840. 4. 29608 lb. S. \$658.
- 6, 100 eq. rd. 7, 337 ml. 8, 275 persons. 9, 108 lb. 10, 9 da.

EXERCISE LIV. PAGE 41.

- 1. 179 mi. S. 96084 yd. S. 10 mi. 4. 64 bu. S. 51 bu.
- 6. 245 bu. 7. 144. 8. 75 e. yd. 9. 207 bbl. 10. 704 ed.

EXERCISE LV. PAGE 42.

1. 119. 2. 910. 3. 83. 4. 1331424. 5, 45. 6, 27. 7, 14839. 8, 811. 9, 41. 10, 23849.

EXERCISE LVI. PAGE 42.

1. 7469. 8. 23. 8. 631229. 4. 323608. 8. 15061. 6. 66. 7. 245. 8. 119025. 9. 767561. 10. 336.

EXERCISE LVII. PAGE 43.

1. 840 steps. S. 14666. S. 2380277. 4, 1249. S. 962556.
6. 179638. 7. 253440 in. S. 20063110804. S. 35643010.
10. 40100 at.

EXERCISE LVIII. PAGE 43.

1. 91199497. 8. 6006. 8. 1145548. 4. 6009. 8. 30008. 6. 615. 7. 80008. 8. 6004. 8. 1430780. 80. 2240 61.

EXERCISE LIX. PAGE 44.

1. 9036. S. 18 et. S. 95 cach. d. 2022 et. S. 200 et. 6. 950. 7. \$1830. S. 485 cheep. S. 11657307. 10. 5 yr.

EXERCISE LX. PAGE 44.

1. 2052. S. 18180 et. S. 95 et. S. 42. S. 10084. S. 960 et. 7. 72 et. S. 94860. S. 118. 10. 308.

EXERCISE LXI. PAGE 46.

1. 27 et. 8. 16 et. 8. 21 mi. 4. 661. 5. 6150. 6. 20 yd. 7. 31 dresses. 8. 1726 bu. 9. 11 hr. 10. 579600 lb.

EXERCISE LXII. PAGE 45.

1. 21 da. \$. 95 da. \$. 20 da. \$. 27 da. \$. 18 da. \$. 18 men. 7. 45 men. \$. 6 men. \$. 240 men. \$10, 225 men.

EXERCISE LXIII. PAGE 46.

1. 16, 20. 8. 20, 30. 3. 20 bu., 46 bu. 4. 42 yd., 58 yd. 5. 44, 50. 6. 13 yr., 15 yr. 7. 19, 28. 8. 111 votes, 129 votes. 9. 67 mi., 90 mi. 10. 193, 195.

4708.

9 de.

4839.

. 06.

3.

EXERCISE LXIV. PAGE 48.

1. 9458. 2. 181257. 3. 62570. 4. 264 mi. 5. \$16. 6. 240 ct. 7. \$6. 8. \$185. 9. 170, 10. \$46626.

EXERCISE LXV. PAGE 47.

1. 33148, . S. 5807 et. S. 10 et. d. 17. S. 47 et. S. 21450 et. 7. 19 gal, S. \$170. S. 2046 et. 10. \$166.

EXERCISE LXVI. PAGE 48.

1. 120 pieces.
 2. 150 pieces.
 3. 9 et.
 4. 21.
 5. 1800 et.
 6. 11 stacks.
 7. 302304 et.
 2. 500 A.
 9. 60 bu.
 10. 17 hats.

EXERCISE LXVII. PAGE 48.

1. 36405 bu. \$. 302878 et. \$. 23 lb. 4. \$2028. \$. Gain, \$161. \$. 38400 lb. 7. \$355 et. \$. 4860 et., 90 et. \$. 36 lb. 10. 1963.

EXERCISE LXVIII. PAGE 40.

1. 1500712. S. 148 mi. J. \$2277. J. 1863 et. J. \$2008.
S. 150 boys. 7. \$31104. S. 85 A., \$42. S. 132 bend. St. 114 mi.

EXERCISE LXIX. PAGE 50.

- 1. 726e.; 406e.; 506e. 2. 3006e.; 10090e.; 300000e.
- \$. 706e.; 1045e.; 8007e.; 10090e.; 2705e.; 40404e.
- 4. 10001e.; 100000e.; 10181e.; 100001e.; 7000770e.
- 6. 87175e.; 57540e.; 618472e.; 37884e.; 96709e.
- 6. \$7; \$86.84; \$449.68. 7. \$10.01; \$576.48; \$100.
- 8. \$270.10; \$470.06; \$74000.07. 9. \$970; \$20000.07; \$47100.71.
- 10. \$4708.41; \$10101.01; \$206006.09.

EXERCISE LXX. PAGE 51.

- 1. 32 far.; 496 far.; 1500 far.; 1804 far.; 3136 far.; 7840 far.; 28000 far.
 - #. 60d.; 852d.; 1200d.; 2802d.; 4428d.; 3664d.; 108108d.
 - \$. 140s.; 840s.; 1800s.; 8380s.; 977s.; 2012s.
 - 4. 264 far.; 460 far.; 504 far.; 579 far.; 948 far.; 9800 far.
 - 8. 6240 far. ; 4704 far.; 6752 far.; 5464 far.; 48963 far.
 - 6. 9d.; 180d.; 106dd.; 225d.; 250d.; 690d.
 - 7. 6a. 8d.; 14s.; 31s. 8d.; 150s. 5d.; 1474s. 1d.; 416s. 8d.
 - 8. £4; £38 4s.; £93 19s.; £228 7s.
 - 9. £3 4s.; £15 7s. 5d.; £30 18e.; £366 4s. \$d.
 - 10. £3 16s. 9d.; £8 0s. 2td.; £47 11s. 6d.; £82 4s. 8td.

EXERCISE LXXI. PAGE 54.

- 1. 32 oz.; 80 oz.; 464 oz.; 2048 oz.
 - #. 64000 oz.; 96800 oz.; 243200 oz.; 224015 oz.
 - 3. 2 lb. 4 os.; 30 lb.; 36 lb. 9 os.; 447 lb. 10 os.
 - 4. 2 t. 216 lb.; 41 t. 161 lb.; 11 t. 949 lb.; 24 t. 1852 lb. 9 oz.
 - 6. 84 in.; 116 in.; 351 in.; 1746 in.
 - 6. Ayd.; 12 yd. 2 ft. 8 in.; 104 yd. 1 ft. 9 in.; 495 yd. 2 ft. 10 in.
 - 7. 115. eq. in.; 2548 sq. in.; 6480 sq. in.; 288 sq. in.
- 8. 8 sq. yd. 6 sq. ft.; 97 sq. yd. 8 sq. ft.;
- 2 sq. yd. 7 sq. ft. 89 sq. in.; 136 sq. yd. 1 sq. ft. 15 sq. in.
 - 9. 5184 cu. in.; 8640 cu. in.; 15552 cu. in.; 209188 cu. in.
- 10. 13 ed. 104 cu. ft.; 45 ed. 8 cu. ft.; 76 ed. 36 cu. ft.; 754 ed. 29 cu. ft.

EXERCISE LXXII. PAGE 55.

- I. 8 pt.; 14 pt.; 193 pt.; 948 pt.
- #. 6 gal. 3 qt.; 190 gal. 1 qt.; 71 gal.; 1220 gal. 5 pt.
- S. 79 bu. 28 lb.; 1702 bu. 28 lb.; 1373 bu. 3 lb.
- 4. 24 pt.; 42 pt.; 62 pt.; 75 pt.
- 8. 2 gal. 1 pt.; 30 gal. 2 qt. 1 pt.; 961 gal. 0 qt. 1 pt.; 251 gal. 1 qt.

6. 425 sec.; \$2100 sec.; 496020 sec.

7. 5 da.; 49 da. 21 hr. 36 min.; 23 da. 3 hr. 33 min.; 9 da. 5 hr. 20 min. 41 sec.

8. 1440"; 46097"; 123319"; 615651".

9. 11° 40′; 15° 56′; 2° 8′ 9″; 21° 14′ 11″.

10. 1760 and 1856.

0.71.

far.;

0 in.

EXERCISE LXXIII. PAGE 88.

1. £83 12s. 9d.; £74 18s. 11d.; £819 2s.

2. 74 cwt. 64 lb. 3 os.; 127 t. 0 cwt. 72 lb.; 56 t. 1 cwt. 28 lb. 3 os.

3. 82 yd. 1 ft. 9 in.; 18 yd. 2 ft. 6 in.; 58 yd. 0 ft. 9 jm.

4. 16 bu. 2 pk. 6 qt.; 32 bu. 3 pk. 5 qt. 1 pt.; 133 gal. 2 qt. 1 pt.

5. 38 gal. 3 qt.; 32 da. 18 hr. 51 min. 56 sec.; 7 wk. 4 da. 2 hr. 45 min. 33 sec.

6. £3 %. 9d.; £19 %. 3d.; 4 ews. 22 lb. 10 oz.

7. 10 t. 15 ewt. 62 lb.; 8 yd. 1 ft. 5 in.; 47 yd. 1 ft. 3 in.

8. 28 bu. 1 pk. 7 qt.; 8 bu. 3 pk. 6 qt.; 2 qt. 1 pt.

9. 2 da. 18 hr. 8 min. 41 sec.; 1 wk. 5 da. 7 hr. 14 min. 45 sec.;

10. 30° 53' 49"; 31 c. yd. 18 c. ft. 1483 c. in.; 51 c. yd. 2 c. ft. 1488 e. in.

EXERCISE LXXIV. PAGE 56.

1. £06 9s. 2d.; £454 14s.; 136 ewt. 67 lb. 1 os.

2. 61 t. 13 ewt. 31 lb. 8 oz.; 211 yd. 2 ft.; 967 yd. 0 ft. 8 fm.

3. 23 bu. 0 pk. 1 qt. 1 pt.; 95 bu. 3 pk. 2 qt.; 34 gal. 0 qt. 1 pt.

4. 187 gal. 2 qt.; 159 da. 11 hr. 33 min.; 46 da. 13 hr. 34 min. 56 an 5. 123° 58′ 39″; 422° 17′ 20″; 86 c. yd. 22 c. ft. 967 c. in.

6. £20 9s. 5d.; £5 3s. 11d.; 7 ewt. 85 lb. 14 os.

7. 2 t. 10 cwt. 64 lb. 9 oz.; 12 yd. 1 ft. 11 in.; 9 yd. 0 11 in.

8. 4 bu. 3 pk. 6 qt. 1 pt.; 8 bu. 0 pk. 1 gal. 1 qt.; 15 gal. 2 qt. 1 pt.

9. 4 gal. 1 qt. 1 pt.; 164 hr. 26 min. 24 sec.; 187 da. 21 hr. 55 min. 57 sec.

10. 19° 15′ 42″; 125° 9′ 24″; 19 c. yd. 22 c. ft. 969 c. in.

EXERCISE LXXV. PAGE 57.

1. 13; 32. 2. 400; 35. 5. 49; 42. 4. 77; 720. 5. 325; 64. 6. 1856; 275. 7. 90; 35. 8. 2880; 156. 9. 78; 1680. 10. 1120; 308.

EXERCISE LXXVI. PAGE 57.

1. 4 ft. 8 in. 2. 504 pt. 3. 744 hr. 4. 131, 86 oz.

5. £116 16s. 3d. 6. £54 13s. 4d. 7. 11 ft. 6 in.; 6 ft. 6 in.

8. 107° 40′ 38″. 9. 353. 10. \$529.20.

EXERCISE LXXVII. PAGE 58.

2. \$27. 8. 1801. 3. \$104. 4. 8080 yd. 5. \$164475.

6. 343 min. 7. 37 lb. 14 on. 8. 15 t. 8. 3000 gal. 10. \$551760

EXERCISE LXXVIII. PAGE 58,

1. 45 t. 2. 60 specus. 3. 108. 4. 15 pages. 8. 42 mi. 60 rd 6. £110 10s. 7. £9 7s. 6d. 8. \$54.92. 9. 60 yd. 20. 15 et.

EXERCISE LXXIX. PAGE 59.

1. 95 gal. 2 qt. 1 pt. 8. 12 gal. 2 qt. 1 pt. 3. 278 bu. 36 lb.

4. 23 bu. 13 lb. 5. 5 min. 15 sec. past 8. 6. 4 lb. 4 cs. 16 dwt. 7. £3 17s. 10id. 8. 288 lb. 9. \$2919. 10. 15 lb.

EXERCISE LXXX. PAGE 61.

1. \$44.70. 8. \$158. 3. \$6778.50. 4. \$134.00. 8. \$297.45. 6. \$153.27. 7. \$17.81. 8. \$49.97. 9. \$2.56. 10. \$58.95.

EXERCISE LXXXI. PAGE 61.

1. \$290. 2. \$2.79. 2. \$7.25. 4. \$311.48. 5. \$221.81. 6. \$5.82.7. \$21.80. 8. \$42.70. 9. \$18.94. 10. \$71.91. 11. \$18.54.

EXERCISE LXXXII. PAGE 63.

1. 10 in.; 14 in.; 22 in.; 16 in. \$. 56 ft. \$. \$45. 4. 250 boards. \$. \$3.40. 6. \$700. 7. \$256. 8. 14080 yd. 9. \$1440. 10. 120 ft., 40 ft.

EXERCISE LXXXIII. PAGE 63.

. 1. 1224 aq. ft.; 1216 aq. ft.; 5616 aq. yd.

2. 9 A.; 10 A.; 15 A.; 42 A.; 15 A.; 19 A. 3. 18 sq. ft. 4. 77 sq. yd.

6. 230% sq. yd. 6. 200 sq. yd. 7. 112 sq. in. 8. 1056 sq. ft.

#. 2000 sq. ft. 10. 24 sq. ft.

EXERCISE LXXXIV. PAGE 64.

1. 18 ft. 8. 54 ft. 8. 40 rd. 4. \$290. 5. \$150. 6. 500. 7. 72 ft. 8. \$940. 9. 360 ft. 20. \$660.

EXERCISE LXXXV. PAGE 65.

1. 40 yd. 3. 60 yd. 3. 32 yd. 4. 70 yd. 5. 196 yd. 6. \$57.60. 7. \$13. 8. \$130. 9. \$24. 10. \$12.60.

EXERCISE LXXXVI. PAGE 65.

1. 6; 9. 2. 8. 3. 16. 4. 8. 5. 10. 6, 72 yd. 7. 48 yd. 8. \$58.80. 9. \$68. 10. \$110.

EXERCISE LXXXVII. PAGE 66.

1. 80 sq. yd. 8. 168 sq. yd. 8. 224 sq. yd. 4. 49.12.

8. \$40.02. 6. 82 sq. yd.; 91 sq. yd. 7. \$28.60.; \$26.20.

8. \$21; \$23. 9. \$30; \$41.50. 10. \$70.20; \$76.14.

EXERCISE LXXXVIII. PAGE 67.

1. 160 yd. 2. 288 yd. 3. 448 yd. 4. 96 yd. 5. 348 yd.

6. 82 yd. 7. 396 yd. 8. 144 yd. 9. \$5.85. 10. \$16.25.

EXERCISE LXXXIX. PAGE 68.

1. 9 ft.; 24 ft.; 24 ft.; 24 ft.; 40 ft.; 24 ft.; 12 ft. 2. 8300 ft.

3. 4200 ft. 4. 2220 ft. 5. 7680 ft. 6. 768 ft. 7. 1650 ft.

8._10000 ft. 9. \$300, 10. \$54 ..

EXERCISE XC. PAGE 60.

1. 2880 e. ft. 8. 210 c. ft. 8. 60 e. yd. 4. 210 c. yd.

5. 4032 lb. 6. \$40.50. 7. 13600 e. yd. 8. 109 c. yd. 1 c. ft. 9. 2376 e. ft. 10. \$1880.

i. 60 rd.

. 36 lb.

16 dwt.

.45.

\$5.33.

boards.

sq. yd. ft.

et.

EXERCISE XCI. PAGE 60.

1. 30 ed. 2. 63 ed. 3. 80 ed. 4. \$84. 5. \$216. 6. \$75.25. 7. 80 ft. 8. 5 ft. 9. 8 ft. 10. 224 ft.

EXERCISE XCII. PAGE 70.

1. 7 ft. 2. 11 ft. 3. 24 ft. 4. 3 ft. 8. 112 ft. 6. 18144. 7. 192 ft. 8. 40 ft. 9. 30 in. 10. 17 ft.

EXERCISE XCIII. PAGE 70.

1. 32 ft. 2. \$40.25. 3. \$1080. 4. 1120 lb. 5. 32 t. 6. 48.t. 7. 1760 c. yd. 8. \$792. 9. \$1440. 10. \$72.

EXERCISE XCIV. PAGE 71.

1. \$32.64. 2. 220 yd. 3. 3600 sods. 4. 8 ft. 5. 90 c. ft.

6. 33 mi. 7. 15 ft. 8. 9 ft. 9. 36 sq. yd. 10. 5 ft.

EXERCISE XCV. PAGE 72.

1. \$17; \$23. S. 19 yd.; 30 yd. S. 36; 48. 4. \$48.75; \$50.25. 6. \$27000; \$23000. 6. \$215; \$160. 7. \$425; \$371.

8. 271 mi.; 237 mi. 9. 395; 361. 10. \$4500; \$1250.

EXERCISE XCVI. PAGE 72.

1. \$5120; \$1280. S. 2064 bu.; 2311 bu. S. \$2726.

. 361 yd.; 242 yd. 6. 297; 315. 6. 462; 534.

. 24 ad. 39 c. ft.; 27 cd. 89 c. ft. 8, 9 A. 115 rd.; 10 A. 45 rd. . 4 mi. 275 rd. 10; 1 t. 8 cwt.; 2 t

EXERCISE XCVII. PAGE 73.

1. 30; 90. 2. 254; 508. 3. 28 yd.; 92 yd. 4. \$2450; \$9800 8. \$75; \$168. 6. \$145; \$462. 7. \$3450; \$10500. 2. 30 rd.; 90 rd 9. \$126. 10. 1240; 3737.

EXERCISE XCVIII. PAGE 73.

1, \$36; \$48. 2. 60 bu. oats; 150 bu. peas. 3, 17.
4. \$7800; \$11700. 5. 275; 230. 6. \$20; \$40; \$60. 7. 30; 45; 75
8. 6. 9. \$420; \$140; \$560. 10. \$10940; \$3020; \$2450.

EXERCISE XCIX. PAGE 74.

1. \$8; \$10; \$13. \$. 170 lb.; 152 lb.; 134 lb.
5. 150 yd.; 125 yd.; 160 yd. 4. 2400 lb.; 2200 lb.; 1800 lb.

5. 127 lb.; 100 lb.; 175 lb. 6. 60 mi.; 25 mi.; 40 mi.

7. 81 rd.; 45 rd.; 128 rd. 8. 256; 378; 452. 9. \$450; \$531; \$612 10. 180 bu.; 283 bu.; 160 bu. 11. 32 et.

12. 87 red, 94 blue, 105 white.

EXERCISE C. PAGE 75.

1. 1975. 2. 3683. 3. 184019. 4. 7, 10, 9. 5. 14, 11. 6. 43, 16. 7. 14 lb. 8. 48 yr. 9. \$119. 10. \$7095.

EXERCISE CI. PAGE 76.

1. 659 lb. 13 oz. 2. 256 mi. 160 rds. 3. \$204.75. 4. \$17.82 5. 35 ewt. 25 lb. 6. 12 lb. 9 oz. 7. 33 mi. 96 rd. 8. 45. 9. \$75. 10. 24 lb. 10 oz.

EXERCISE CII. PAGE 76.

1. \$82. 2. 7 ct. 3. 15 carats. 4. 40 ct. 5. 6 ct. 6. 200 bu. at 75 ct., 300 bu. at 70 ct. 7. 4 ft. 3 in. 8. 139 lb. 9. 1s. 7d. 10. 4s. 9d.

EXERCISE CIII. PAGE 77.

1. 272 fb., 2448 lb. 2. \$570940. 3. 2 oz. 4. 35 ct. 5. 22 yr. 5. \$25. 7. 7 ct. 8. 46 ct. 9. \$6.60. 10. 12 carata.

EXERCISE CIV. PAGE 78.

1. 2, 2, 3; 2, 2, 2, 7; 2, 2, 8, 7; 2, 3, 5.

2. 2, 2, 7, 7; 3, 7, 11; 2, 2, 3, 3, 7; 2, 2, 2, 2, 2, 2, 2, 3.

5. 2, 2, 3, 73; 2, 2, 3, 79; 2, 2, 263; 3, 853.

4. 3, 5, 78; 3, 7, 58; 7, 7, 23; 2, 2, 17, 17.

5, 2, 601; 2, 607; 2, 3, 7, 29; 5, 311. 6. 797, 821. 4. 2543, 2521. 9. 2273, 2839, 2417. 10. 3119,

: 40600.

.; 90 rd.

45: 75.

b. 1; \$612.

\$17.82.

9. 975.

9 lb.

. 22 yr.

1187.

EXERCISE CV. PAGE 78.

1. 2, 5; 5, 7. 2. 3, 7; 11, 13. 3. 7, 17; 2, 2, 3.

4. 2, 2; 2, 2, 3, 3, 2. 5. 2, 2; 5. 8. 30; 25; 275; 196; 443. 0. 2, 3, 5; 3, 5, 7; 5, 7, 11; 7, 11, 13; 11, 17, 19.

EXERCISE CVI. PAGE 79.

1. 180. 8. 5. 5. 6. 4. 120. 5. 4. 6. 1008. 7. 2400.

8. 900 bu. 8, 75 yd. 20. 40 da.

EXERCISE CVII. PAGE 80.

1. 14; 16; 13. 8. 35; 46; 42. 3. 72; 82; 4. 4. 9; 16; 7.

8. 25; 42; 42. 6. 9; 4; 78. 7. 78; 82; 11. 8. 9; 8; 13-

0. 32; 110; 14. 10. 91; 143; 328.

EXERCISE CVIII. PAGE 80.

1. 14 ft. ... 17 in. 3. 15. 4. 7 ft. 6. 2 ft. 3 in. 6. 13 ft. 7. 63 bu. 8. 41, 42, 45, \$10, or \$50. 9. \$124. 10. 26880 rails.

EXERCISE CIX. PAGE 81.

1. 18; 7; 251, S. 107, 311, 103. S. 52, Prime, 601.

4. 31, 947, 283: 8. Prime, 47, 811. 6. 8, 616, 884., 7. 1186, 13, 13.

8. 46, 21, 9. 9. 897, 1323, 1429. 10. 315, 19.

EXERCISE CX. PAGE 81.

1. 105; 8, 5, 7, 15, 21, 35, 105. \$. 2 da. 5 hr. \$. 1 mi. 37 yd. 4. 3 gal. 5. 117. 6. 29. 7. 25. 8. 19 men. 9. 7 os. 10. 126.

EXERCISE CXI. PAGE 82.

1. 24; 120; 120. 2. 75; 600; 720. 3. 315; 2652; 3705.

4. 360; 1260; 504. 5. 576; 600; 27720. 6. 1260; 8415; 16546530.

7. 10690; 17160; 205205. 8. 14280; 166320; 22770.

9. 1190595; 27945372; 885969. 10. 12018283514; 110250; 620810.

EXERCISE CXII. PAGE 83.

1. 120. 2. 360. 3. 85085. 4. 6485. 5. 48. 6. 148.

7. 1526. 8. 90. 9. 120 ft. 10. 60 gal.

EXERCISE CXIII. PAGE 83.

1. \$20. 2. 141 lb. 3. 94 lb. 4. 80. 5. 80 mi. 6. 365. 7. 62, 122, 182. 8. 600 bu. 9. 13, 14, 15, 16. 10. 1008000 gr.

EXERCISE CXIV. PAGE 84.

1. 4; 4; 4. 2. 4; 4; 4. 3. 4; 4; A. 4. 4; 4; 4.

5. Two-thirds; three-fifths; four-sevenths; three-elevenths.

6. Seven-twelfths; eleven-twenty firsts; mineteen-twenty seconds; seventeen-twenty afths,

7. Seventeen airty frets; eleven-twelfths; nineteen-thirt seconds; eleven-fifty firsts.

8. One inch is divided into 3 equal parts and 2 of these part are represented by # in.;

Or, I in. represents a third of 2 in.

Or, † in. represents the quantity which must be multiplied by to produce 2 in.

(All the other fractions are capable of similar interpretations.)
One foot is divided into 4 equal parts and 3 of these parts are represented by \$ ft.;

One acre is divided into 5 equal parts and 4 of these are represented by # A.;

A dollar is divided into 10 equal parts and 7 of these are represented by \$75.

9. One hour is divided into 9 equal parts and 7 of these are represented by \$\frac{1}{2}\$ hr.

One is divided in 12 equal parts and 11 of these are represented by †‡;

When the fraction is abstract it may have a fourth meaning. Thus, † may represent the ratio of 11 to 12 in., or the fraction that 11 in. is of 12 in., or the measure of 11 in. when 12 in. is the unit.

One is divided in 21 equal parts and 13 of these are represented by 11;

One is divided in 25 equal parts and 7 of these are represented by w.

10. One cord is divided in 7 equal parts and 5 of these are represented by ∮ ed.;

One ewt. is divided into 25 equal parts and 17 of these are represented by ## ewt.;

One pound is divided in 8 equal parts and 7 of these are represented by # lb.;

One ton is divided into 12 equal parts and 5 of these are represented by Tt t.

EXERCISE CXV. PAGE 86.

- I. 1; Y; Y; Y. . . . 2. Y; Y; Y; Y.
- 3. Y; Y; H; W. 4. Y; Y; Y; 41.
- 5. 440; 440; 450; 4650. 6. 2440; 4470; 4444, 2480.
- 7. 4181; sage1; sages; 1878s.
- 8. 18881; 4482; 49881; 144691
- 9. 11412, 17841; 148321, 141441
- 10. 227742; 24072; 240751; 210562.

PRACTICUIS. n-thirty EXERCISE CXVI. PAGE 86. 1. 4 boys. 2. 12 girls. 3. 30 fifths. d. 11 persons. o parts 8. 15 boys. C. #1; 44. 7. 42; 47. 8. #1; 47; 47; 40. 9. 18 mi. 10. 85 papile. ied by 3 EXERCISE CXVIII. PAGE 86. 1. 24; 24; 24; 2. #. 1; 2; 5; 5; 3; 5. 714; 5; 54; 54. 4. 94; 1611; 2011; 2011. 5. 514; 444; 615; 1311. 6. 4146; 2011; 1644; 1446. ations.) aris are 7. 20118; 9494; 31184; 34164. 8. 3344; 1004; 1044; 1044. 9. 2014; 45f gal.; 53f da.; 50f lb. 10. 7 M mi.; 34ff ed.; 21ff yd.; 68ft os. 000 APO EXERCISE CXVIII, PAGE 87. ESO 276 1. 841. 1. 921 bu. S. 19 mi. 4. 161 lb. 5. 8211 bu. 6. Latter by & lb. 7. 11 in.; 7 lb.; 25 oz. 8. 7 gal. ted about 9. 20 ft.; 16 ft. 10. \$19.75. EXERCISE CXIX. PAGE 87. esning. 1. to to to 2. to to to. restion 3. 11; 11; 11. 2 in. is 4. H; H; H. 5. H; H; &. 6. 11; 11; fr. 7. 11; A; Cl. 8. 11; 11; 11. poonted 9. H; H; A. 10. 11; 11; 11. sented EXERCISE CXX. PAGE 88. 1. 1; 1; 1. 2. 1; 1; 1. B66 870 3. 4; 4; 4. 4. 4; 4; 4. 5. 11; 11; 11. 6. 11; 11; 11. 018 OM 7. 11; 11; 11. 8. tei te; te. 9. H; A; H. 10. 17; 11; 11. repre-EXERCISE CXXI. PAGE 88. repre-1. 1: 11; 11. 2. 11; 11; 11. 3. 11; 11; 11. 4. 1; 1; 1. 5. 1v; 1; 1v. 6. 11; 11; 11. 7. 14; 11; 14. 8. 111; W; M. 9. 1; 1; 1. 10. 1; 1; 14. EXERCISE CXXII. PAGE 88. 7455 · 1. 1; 1; 1; 1. 2. 18: 4: 4: 4. 8. 4; 11; 14; 1. 4. 1; 1; 11; 11. 5. 1; 1; 1; 14. 6. 11; 14; 14; 14. 7. 1; 11; 11; 11. 8. 16; 1; 1111; 14. 9. A; H; I; 1. 100. 10. 111; H; H; H;

EXERCISE CXXIII. PAGE 80.

- 1, 1, 1; 11, 14; 12, 12. 2. 17, 17; 11; 14; 14, 17
- 3. 1, 1; 14, 15; 14, 15. 4. 11. 45; 11, 11; 11, 11.
- 5. 11, 11; 11, 11; 11, 11.
- 6. 111, Mr; 111, M; 111, M.
- 7. 14, 14; 14. 111; Th. 11.
- 8. 11, 11; 11, 11; 11, 11.
 - 9. 11, 11; 11, 11; A. A.
- 10. 11, 11; 14, 14; 11, 111.

EXERCISE CXXIV. PAGE 80.

- 1. 16, 16, 16; 11, 11, A.
- 2. 111, 14, 14; M, 111, 14.
- 8. the, the, the ite, the, the.
- 5. 44, 44, 41, 44; 11, 12, 11, 11.
- 6. 411, 411, 411, 411; A., 111, 174, 174.
- 7. AM, AM, 1811, AM; 111, 181, 111, AM.
- 8. At, 14, 14, 14; 111, 14, 14, 14.
- 9. M. M. M. M. H. H. H. K.
- 10. H, H, W, W; HI, HI, HI, W.

EXERCISE CXXV. PAGE 80.

- 1. Greatest, \$; least, \$; greatest, \$; least, \$.
- 2. Greatest, #; least, #f; greatest, #; least, #r.
- 3. Greatest, \$; least, \$\frac{1}{2}\$; greatest, \$; least, \$.
- 4. Greatest, A; least, &; greatest, &; least, \$1.
- The smallest being placed first the following is the order:
- 5. 11, 14, 11, 11; 14, 14, 14, 14.
- 6. 1, 1, 1. 11; 1, 11, 11, 11, 11.
- 7. A, H, A, H; A, A, H, H.
- 8. 11. 9. 11. 10. 11.

EXERCISE CXXVI. PAGE 90.

- 1. A; A; 1. 2. 4; A; H. 3. A; H; H.
- 4, 11; 11; 11. 5. 11; 11; 111. 6. 3; 211; 3.

14. 47. 1. 11.

7. 16; 49; 30. · 8. ve; 1; 1. 9. 1; 1: 1. 10. 288, 1024.

EXERCISE CXXVII. PAGE 90.

2. 4; 4; 4. 2. 14; 14; 4. 3. 14; 11; 11.

4. 2; 1; 2. 5. 1; 2; 17. 6. 14; 14; 27.

7. 111: 17; 24. 8. 2111; 11; 1111.

9. 111; 211; 2111. 10. 1111; 211; 1111.

EXERCISE CXXVIII. PAGE 91.

1. 16; 16; 11. 4. 11; 11; 11.

3. 166; 128; 1777.

4. 167; 168; 168; 168.

5. 164; 168; 168.

6. 1776; 168; 168.

7. 1776; 168; 168.

8. 168; 168; 168.

9. 168; 168; 168.

10. 168; 168; 168.

EXERCISE CXXIX, PAGE 91.

1. 111: 9. 311. 8. 1. 4. 4111. 5. 2111.

6. 241. 7. 3517. 8. 171. 9. 231. 10. 2618.

EXERCISE CXXX. PAGE 91.

1. 11. 9. 2911 A. 3. 11111 lb. 4. 571. 5. 11.

6. 1787. 7. 81. 6. 2111 mi. 9. 114 y gal.

10. 1821 mi.

EXERCISE CXXXI, PAGE 92.

1. \$; \$; \$. 2. \$; \$; 1. 3. \$; \$; \$.
4. \$; \$\$; \$\$\$, 5. \$; \$; \$.
6. \$\$; \$\$; \$\$

7. to; to; tt. 8. 141; 11; 11. 9. 14; 11; 11.

10. 11; 24; 44.

FXERCISE CXXXII. PAGE 92.

2. \$; \$\frac{1}{10}; \delta : \frac{9}{10}; \delta : \frac{1}{10}; \delta : \frac{3}{10}; \delta : \frac{1}{10}; \

7. 140; 110; 11. 8. 11; 11; 11. 5. 11to; 11; 11. 10. 111; Tiv; 100.

EXERCISE CXXXIII. PAGE 93.

1. \$50. 2. 12. 3, 100. 4. 11. 5. 100. 6. 14. 7. 11. 8. 11. 9. 11. 10. 10.

EXERCISE CXXXIV. PAGE 83.

- 2. 31; 34; 54. 2. 1; 172; 722. 3. 22; 522; 622. 4. 311; 447; 442.
- 5. 21; 211; 1111. 6. 141; 23 1; 201.
- 7. 144; 11; 10111. 8. 2611; 2011; 10%.
- 9. 1744; 3844; 3144. 10. 2341; 1274x; 1344.

EXERCISE CXXXV. PAGE 83.

- 1. 16† gal. 2. 18† yd. 3. 16†† mi. 4. 30†.
- 5. 495ft. 8. 159ft A. 7. 468f. 8. 137 9. 15f 10. 16411 t.

EXERCISE CXXXVI. PAGE 84.

- 1. 48; 14. 2. 31; 818. 3. 191; 41. 4. 6; 97.
- 5. 44; 511. 6. 111; 341. 7. 111; 2711. 8. 211; 77
- 9. 10; 114. 10. 811; 144.

EXERCISE CXXXVII. PAGE 94.

- 1. 97# lb. 9. 16# gal. 8. 54 lb. 4. 193#.
- 5. 33 mi. 6. Gained \$1 . 7. \$23 . 8. \$94 1.
- 9. 181 yd. 10. 8714 yd.

EXERCISE CXXXVIII. PAGE 95.

- 1. 11; 21; 11. 2. 34; 31; 41. 3. 411; 441; 411.
- 4. 15; 8; 21. 5. 6; 7; 12. 6. 16; 81; 31.
- 7. 10; 15; 30. 8. 15; 81; 21. 9. 41; 111; 91.
- 10. 28; 68; 93.

EXERCISE CXXXIX. PAGE 95.

- 1. 4; de; et. 2. de; de; ttr. 3. 21; 5fr; 4fr.
- 4. 24; 34; 94. 5. 1; 1; 1. 6. 4; 11; 21.
- 7. 1; A; A. 8. A; A; A. 9. A; H; M.
- 10. 811; 711; 511.

EXERCISE CXL. PAGE 96.

- 1. 4; 9; 8. 8. 4; 4; 11. 3. 11; 11; 11.
- 4. 11; 14; 11: 5. 1; 1; 4; 4. 6. 1; 61; 51.
- 7. 4; 1; 11. 8. 4; 14; 11. 9. 1; 1; 11.
- 10. 1: 14: 35.

EXERCISE CXLL. PAGE 96.

1. 201; 30%; 56%. 2. 301; 4214; 7211.

- 3. 4281; 56♣; 15681. 4. 1; ♣; ♣. 5. 15; 161; 91.
- 6. 1\(\frac{1}{4}\); 11; 20. 7. 1\(\frac{1}{4}\); 16\(\frac{1}{4}\). 8. 31\(\frac{1}{4}\); 2\(\frac{1}{4}\); 1.
- 9. \$17; \$1; 556 mi. 10. \$558; 324 oz.; 3 hr.

EXERCISE CXLII. PAGE 96.

1. 600 fy. 2. 61709. 3. 71fe. 4. 8} mi. 5. 618}. 6. 12\$ bu. 7. 01739j. S. 36 bu. S. 47 A. 10. 04.

EXERCISE CXLIII. PAGE 97.

1. \$1.66. 2. \$80000. S. 85 mi. 4. 37} ft. S. 365 mi.

6. \$105000. 7. 257\$. 8. 20100 men. 8. 210 pages. 10. \$65000.

EXERCISE CXLIV. PAGE 97.

1. 2); 34j. 2. 18; ft. 3. 17\$; 7. 4. 3\$; 88. 6. 4; 3\$.

6. 7; 20. 7. 10; 40. -8. 24; to. 9. 35\$; \$. 20. 1; 24.

EXERCISE CXLV. PAGE 94.

1. 185f mi. S. \$1012. S. 50f. 4. 32ff bu. S. \$17000f.

6. 10. 7. 37-M. 8. 49126 9. 943\$. 10. Gain, \$12.

EXERCISE CXLVI. PAGE 86.

1. 14, 16, 15. 8. 36, 55, 44. 8. 8\$, 14\$, 34\$. 4. 17\$, 31\$, 30\$.

5. 44, 5A, 6A. 6. 618, 718, 1181. 7. 58, 4, 71. 8. 14, 14.

9. 14, 21, 14. 10. 2, 1, 14.

A.

. 1544.

974.

41.

: \$14.

11: 74.

EXERCISE CXLVII. PAGE 90.

2. 18; 18, 18. 2. 18, 18, 16. 3. 14, 14, 14. 4. 8, 8, 4.

8. 19, 14, 16. 6. 3tr, 14, 1tr. 7. 21, 6, 8. 8. 21, 12, 24. 9. 148, 8, 2. 19. 78, 1A, 88.

EXERCISE CXLVIII. PAGE 90.

1 37t yd. 2. 8f mi. 3. 826t. 4. 17f mi. 5. 10 bags.

6. 12j et. 7. 29j hr. 8. 8jf. 9. 217j A. 10. 370j A. 11. 15} ot. 18. 32 da. 18. 43.66. 14. 20.

EXERCISE CXLIX. PAGE 100.

1. 74. 4. 2. 34, 34. 3. 217, 12. 4. 1, 15. 5. 84, 14. 6. 1, 211. 7. 41, 112. 8. 231, 16. 9. 10, 16. 10. 3611, 114.

EXERCISE CL. PAGE 100.

2. 1. 31. 8. 31, 30. 8. 54, 661. 4. 0, 11. 8. 11, 21.

8. ft, 24. 7. t, 5t. 8. 10ft, t. 9. 5tt, t. 10. tt, ff.

EXERCISE CLI. PAGE 101.

1. 58, 6. 2. 14, 14. 3. 14, 14. 4. 18, 14. 5. 14, 14.

6. 1, 14. 7. 21, 36. 8. 7, 1. 8. 11, 40. 10. 1, 2.

EXERCISE CLII. PAGE 101.

1. 1444. 1. 2. 1. 14. 1. 1. 15. 74. 6. 44. 7. 154. 2. 434. 2. 4. 10. 4.

EXERCIBE CLIII. PAGE 162.

1. †\$. 8. 4. 2. 6†\$. 4. \$\$. 5. 2. 6. 25. 7. 10\$. 8. \$\$. 8. 1\$\$; \$\$; \$\$.; \$\$. 10. \$.

ERERCISE CLIV. PAGE 102.

1. \$\frac{1}{2}\$; \$\f

EXERCISE CLV. PAGE 101.

1. 10e.; 3fd.; 4fd. #. 87f et.; 80 et.; 75 et.

2. 17 ewt, 60 lb.; 7 lb. 8 os. 14 os.

d. 218 rd. 1 yd. 2 ft. 6 in.; 3 yd. 2 in.; 2 ft. 6 in.

5. 128 eq. rd.; 22 eq. yd.; 2 eq. ft. 117 eq. in.

6. 96 e. ft.; 11 e. ft. 432 e. in.; 504 e. in.

7. 2 pk. 1 gal.; 1 gal. 14 qt.; 3 qt. 8. 3 qt. 1 pt.; 14 pt.; 34 qt

9. 4 da. 21 hr. 36 min.; 7 hr.; 25 min. 20. 40'; 288'; 16' 40'.

EXERCISE CLVI. PAGE 104.

1. 444546 in.; 196744 in.

8. 1 mi. 181 rd. 4 yd. 2 ft. 6 in.; 1 mi. 179 rd. 1 ft. 6 in.

3. 237600 in.; 1550% in. 4. 31637626 eq. in.; 3860136 eq. in.

5, 1 A, 58 eq. rd. 19 eq. yd. 6 eq. ft.; 2 A, 47 eq. rd. 9 eq. yd 3 eq. ft. 35 eq. in.

6. 16727040 eq. in.; 181868 eq. in. 7. 9600 lb.; 2800 os.

s. 145 rd. 2 yd. 1 ft. 6 in.; 96 sq. rd. 10 sq. yd. 108 sq. in.

9. 9 A. 120 sq. rd. 22 sq. yd.; 1 A. 16 sq. rd. 9 sq. yd., 8 sq. ft 10. 200 gal., 35 t.

EXERCISE CLVII. PAGE 104.

1. \$62.11; \$28.80. S. £1 5a. 3åd.; £1 2s. 8d.

8. 8 t. 12 cwt. 4 lb.; 1 t. 11 cwt. 46 lb.

4. 2 mi. 197 rd. 5 yd. 9 in.; 2 mi. 270 rd. 44 in.

8. 1 A. 185 rd. 22 yd. 8 ft. 5† in.; 2 A. 16 rd.

6. 2 ed. 59 eu. ft.; 10 ed. 60 eu. ft.

7. 8 bu. \$ gal.; 2 bu. 0 pk. 4 qt.

8. 5 gal.; 13 gal. 1 pt. 9. 23 hr. 20 min.; 5 hr. 26 min. 40 sec 20. 10° 30′ 12″; 14° 30′ 30″. EXERCIBE CLVIN. PAGE 104.

1. afe out. S. Lote. S. if bu. d. if rd. S. afe rd. a. t ps. 7. t co. 0. 11. 0. 1. 10. 10.

EXERCISE CLIN. PAGE 168.

1. 6 16. 2. viv. 3. 188 ml. 4. 15. 6. 16. 6. 16 on. yd. 7. 81. 8. 4 ml. 0. 111. 10. 15 A.

EXERCISE CLX. PAGE 166.

2. 34040585. S. 505 Ib. S. 160 qt. 4. 567504. S. 4820. 8040, 7. 6051.95, 8. 61837\$, 9. 644.20, 19. 6260.

EXERCISE CLXI. PAGE 105.

1. 118188 lb. 8. 31† ed. 5. 0150. 4. 08.84. 5. 0023.00. . 207 d. 7. 130000 min. 8. 1440 min. 8. \$21.51. 10. 2024 poles.

EXERCISE CLXII. PAGE 104.

1. 47 lb. 2. 36112 pt. 3. 5302 on. 4. 31 t. 5 owt. 5. 1800. 9489.85. 7. 1248 oc. 8. 40 et. 9. 189. 10. 46772 lb.

EXERCISE CLXIII. PAGE 106.

1. 22606 gr. 2. 161 gr. 2. 5 1/2 on. 4. 5184 gr. 5. 11006 gr. 10 1b. 1 ca. 12 dwt. 8 gr. 7. 28. 8. 874 lb. . 701 lb. 6 oc. 6 dwt. 5 gr. 10. 114ff lb.

EXERCISE CLXIV. PAGE 107.

1. 68360 in. S. 8064 in. S. 2 mi. d. 9462. S. \$422.40. 9509, 7. 10 hr. 17 min. S. 1584090 in. D. 506808 in. 0. 440 mi.

EXERCISE CLXV. PAGE 107.

1. 972. 2. 601.50. 2. 61.95. 4. 488 backete. 8. 326 pt. \$1.05. 7. 4. 8. \$510.30. \$. 2 qt. 10. \$137.741.

EXERCISE CLXVI. PAUE 100.

1. 22 da. S. 264 ft. S. 9. d. 44 ft. S. 9 ml. G. 220 hr. 500 da. 8. \$57.24. 9. \$47.25. 10. \$19.44.

EXERCISE CLXVII. PAGE 108.

1. 68 et. 2. 5 ft. 3. 8184. 4. 15. 8. 48 mi. 6. 48 hr. 4620 paces. 8. 43. . 9. . 24820. . 10. 811 mi.

EXERCISE CLXVIII. PAGE 100.

1. 6 lb. 4 os. 8 dwt. 12 gr. S. £200. S. 10 cwt. 80 lb. 1 os. 24 ft. 5. 990 yds. 6. 4 min. 16 sec.; 980 yd. 7. 22 yd. 54, 8, 980 lb. 10, 1271, ...

b. ; 19.

S. 14.

ŧ.

. 1 2} qt. 16' 40".

n. o. in. sq. yd.

in. 3 ag. ft.

EXERCISE CLXIX. PAGE 100.

1. 84 in. 2. 7 da. 3. 506 da. 4. 66 mi. 8. 75 et. 6. \$6050.50 7. 40f yd. 8. 60 ct. 9. 12 da. 20 hr. 20 min. 10, 4 yd. 1 ft. 3 in.

EXERCISE CLXX. PAGE 110.

1. 3 lb. 11 oz. 11 dwt. 6 gr. 2. 9. 3. 12 hr. 4. 110 da. 8. 36 hr. 6. 42. 7. 92028. 8. 12 spoons. 9. 5 mi. 10. £43 1s. 3d.; £6 8s. 9d.

EXERCISE CLXXI. PAGE 110.

1. 209 bu. 1 pk. 3 qt. 2. 1569 bbl. 3. A, 18 yd.; B, 19 yd. 4. 36 mi. 298 rd. 1 ft. 6 in. 5. 48 rd. 6. 84 yd. 7. 462. 8. \$13.50. 0. \$432. 10. 14f t.

EXERCISE CLXXII. PAGE 111.

1. \$7.50. 2. \$1.76. 3. \$96. 4. \$49. 6. \$19.12. 6. 27\ yd. 7. 27 lb. 8. 10 hr. 9. \$8.92\frac{1}{2}. 10. \$94.40, \$660.80.

EXERCISE CLXXIII. PAGE 111.

1. 48, 8 lb. 2. 32 lb. 3. 42 mi. 4. 24 yd. 5. 450 sheep. 6. 176 ft. 7. 58 A. S. 60 et. 9. \$12000. 10. 18 A.

EXERCISE CLXXIV. PAGE 112.

1. 288. 2. \$68. 3. 160\$ bu., 321\$ bu. 4. \$20\$. 5. \$6000. 6. 8\frac{1}{2} ft., 2079\frac{1}{2} gal. 7. \$28.76. 8. 100 A. 9. \$4070. 10. \$6250.

EXERCISE CLXXV. PAGE 113.

1. 50 A. 156 rd. 2. 7 ft. 9 in. 3. 8f ft. 4. 3 doz.

8. 18117 A., 20317 A. 6. 38 A. 911 rd. 7. 42240. 8. \$66.01.

9. 396 lots. 10. \$13459.56; James, \$3364.89; William, \$4486.52; daughter, \$1121.63; wife, \$4486.52.

EXERCISE CLXXVI. PAGE 113.

1. \$0. 8. 1. 8. 1 da. d. 36 da. 5. 16 da. 6. 41 da. 7. 10 da. 8. 11 da. 9. 21 da. 10. 11 da. 11. 21 da.

12. 51 hr. 13. 28\$ hr. 14. 61f da. 15. 24 da. 16. 3ff da.

EXERCISE CLXXVII. PAGE 116.

1. Nine-tenths; forty-five hundredths; seventy-five hundredths; eight hundredths.

2. Two hundred and seventy-five thousandths; eighty-seven thousandths; six thousandths; two hundred and nine thousandths.

3. Two, and six hundredths; seven, and one thousandth; ten, and seven hundredths; nine, and two hundred and seven thousandths.

4. Three thousand eight hundred and seventy-five ten-thousandihs; five hundred and sixty-two ten-thousandths; eighty-three ten-thousandthe; six ten-thousandths.

- 5. One, and six hundred and thirty-one thousandths; one, and three hundred and fifteen thousandths; forty-eight, and seven thousandths; eighty-seven, and six ten-thousandths.
- 6. Two hundred and one, and two hundred and one thousandths seventy-eight, and five hundred and sixty-seven theusandths; one hundred, and one thousandth; seven hundred and nice, and two hundred and twenty-four thousandths.
- 7. Six hundred and twelve, and six hundred and twelve thousandths; thirteen, and one hundred and eight ten-thousandths; seven hundred, and six hundred and twenty-five thousandths; five, and six thousand and six ten-thousandths.
- 8. Ten thousand, and one thousandth; one thousand, and one ten-thousandth; one hundred thousand, and one hundredth; one
- 9. Two hundred, and two thousand and six ten-thousandths; two thousand and two, and six thousandths; twenty thousand and twenty, and six hundredths; twenty, and two thousand and six hundred-thousandths.
- 10. Seventy-eight thousand nine hundred and sixty-five, and four hundred and thirty-two thousandths; seven hundred and eighty-nine, and sixty-five thousand four hundred and thirty-two hundred-thousandths; seven thousand eight hundred and ninety-six, and five thousand four hundred and thirty-two ten-thousandths; seven hundred and eighty-nine thousand six hundred and fiftyfour, and thirty-two hundredths.

EXERCISE CLXXVIII. PAGE 116.

- 1. 325.7. \$. 465.14. \$. 93.07. 4. .213. \$. 1000.0006.
- 6. 37.072. 7. .0718. 8. 340000.406. 9. 56008000.000056. 10. 70000000.000007.

EXERCISE CLXXIX. PAGE 117.

- 1. 961.15; 509.081; 1119.1817; 227.05. \$. 1605.50494.
- 3. 405.970973. 4. 9982.1237989. 5. 7449.098. 6. 892.842547.
- 7. 131.8562. 8. 170.63676. 9. \$508.85. 10. \$913.829.

EXERCISE CLXXX. PAGE 117.

- 1. 1006.6106. #. 251.8474. 5. 843.086. 4. 1965.0771.
- 5. 8574.1378. 6. 4679.1364. 7. 226.35187. 8. 4196.924.
- 9. 223.91522. 10. 4533.246.

0.50. 3 in.

yd.

d.

2:

;

EXERCISE CLXXXI. PAGE 117.

- 1. 282.405 A. S. 307222.086446. S. 363.536487.
- 4. 115.8125 yd. 5, 24.2675 t. 6. 25269.111506. 7. .42951308. 8. 6.5 t. 9. 188.122i37. 10. 48095.139823.

EXERCISE CLXXXII. PAGE 118.

- . 1. 4.17; 53.98; 14.231; 69.497.
 - £. 37.6211; 3.322; 4.10001; 19.7283.
 - s. 4.758; 1.8742; .0058; 5.665.
 - 4. 5.2311; 4.122. 5, .453; 55.0316. 6, 13.211; 16.9900, 7, 99.9990; 9.90.
 - 8. 81.4211; .12346. 9. 87.344; 8.405. 10. 384.9024; 903.9004.

EXERCISE CLXXXIII. PAGE 119.

- 3. 3.09; .7632; 2.786.
- 5, 4.2517; 1.255; .9999.
- 9. .1235; 25.1905; 2.46.
- 1. 3.544; 12.66; 10.565. 2. .7141; .2703; 4.3155.
 - 4. 70.4625; 2.524; 7.9933.
 - 6. 9.9995; .125; 21.325.
- - 20. 96.855; 4.4445; .99646.

EXERCISE CLXXXIV. PAGE 119.

- 1. 72.927. s. .1993. s. 264.9953. 4. 6009.9996045.
- 8. 999999.999999. 8. .017481. 7. 2999999.900001. 8. .000999.
- 9. 43,08997. 10. 6929.95993.

EXERCISE CLXXXV. PAGE 119.

1. 30.280965. S. 75.0665. S. 15.635563. 4. 16.6799884. 5. 49.156. 6. 4.162. 7. 81.143. 8. 9.7597. 9. 80.025. 10. 9.0897.

EXERCISE CLXXXVI. PAGE 120.

1. 228.475 A. 3. \$327.065. 3. 199.35 mi. 4. \$963.68. 5. 262.35 A. 6. .06 in. 7. \$111.58. 8. 29569.92 A. 9. 123.315 lb. 10. 73.73 ft. 11. .3. 18. 30.338 in.

EXERCISE CLXXXVII. PAGE 121.

- 1. 20.16; 30.24; 56.09. \$. 12.25; 156.21; 110.16.
- 3. 16.11; 1.501; 19.6875. 4. 00.125; .0945; .000243. 5. 76.845; .00063; 156.25. 6. 4.38496; .0372161; 152.2756.
 - 7. .00000081; .007224; .005621.
 - 8. .00004216; .C0015625; .005625.
 - 9. 28.3743; 5673.024; 60.025.
 - 10. 49.098049; .0010001; .27648.

EXERCISE CLXXXVIII. PAGE 121.

- 1. .435; .0676. 8. 506.4468; 35.4367519. 8. .013272; 32.5779. 4. 36.9; 1.7995, 8. 3.8; 1860.867. 6. 525; 92.7.
- 7. 11221.1; 54.706. 8. 0.06458; 279.29475. 9. .000000027; 4.8. 10. .1728: .082. a grant of the same of

EXERCISE CLXXXIX. PAGE 121.

- 1. 1284.56; 12845.6; 128456. . 8. 83.5175. . 8. .000019787.
- 4. .00865. 8. .005169. 6. 45; 450; 4500; 45000. 7. 421000.
- 8. 1144.90001605. 9. .68785. 10. .0000000000884.

EXERCISE CXC. PAGE 122.

- 1. 204.375 mi. 2. 453.125 lb. 3. \$7000. 4. 270.465 ft.
- 5. 864.86 ft. 6. 23.625 yr. 7. 436247.424 gr. 8. 500.628 mi.
- 9. 998.125 gal. 10. 297.25375.

EXERCISE CXCI. PAGE 122.

- 1. .4; 40; 50. 2. 200; 400; 30. 3. .016; 7.5; 8. 4. 34; 2.5; 15.
- 5. .2; 200; .0016. 6. 2480; .00025; 4000. 7. 42.8; 73.21; 2.78.
- 8. .85; .234; 4602. 8, 60000; .0075; .000436.
- 10. 42250; 4600000; 548.8.

EXERCISE CXCII. PAGE 123.

- 1. 14; 19.28. S. 185000; .00002. S. 52.416; .013352.
- 4. 40000; 24106.25. 5. 24.488; 31.8. 6. .0015; .0672.
- 7. .128; 115812.5. 8. 192; 825.26. 9. 1.099; 160. 10. .043; .135.

EXERCISE CXCIII. PAGE 123.

- . 1. 15.24. 2. 350000. 3. .413. 4. 330000. 5. .024.
- 6. 64753000000. 7. 12.345, 1.2345, .12345, .012345. 8. 10.5.
- 9. 127.4. 10. .075, .0075, .00075.

15 lb.

779.

EXERCISE CXCIV. PAGE 123.

1. 6.165 rd. 4. 320 rd. 5. 42 bu. 4. 144 bbl. 5. 87.5 bbl. 6. \$128.50. 7. \$27.5. 8. \$10800. 9. 15.75 bu. 10. 5.2 hr.

EXERCISE CXCV. PAGE 124.

- 1. w; it; i; i. 2. 1; 1; 1; 11.
- 3. 111; 10; 1; 110. 4. 11; 11; 10; 111.
- 5. 166; 161; 26; 260. 6. 166; 1660; 1660; 1660.
- 7. 21; 411; 71; 51. 8. 81; 91; 1211; 5111.
- 9. 61; 16t; 71; 111. 10. 51; 21; 711; 911.

EXERCISE CXCVI. PAGE 124.

- 1. .25; .75; .125; .375. £. .625; .875; .1875; .3125.
 - 3. .4375; .5625; .6875; .8125. 4. .16; .24; .44; .72.
- 5. .175; .425; .925; .825. 6. .144; .084; .888; .988.
- 7. 4.28; 3.725; 5.775; 7.975. 8. .072; 3.068; 5.04; 7.125. 9. .036; 5.04; 7.9875; 8.36. 10. .2192; .1616; .7066; .5936.

EXERCISE CXCVII. PAGE 125.

- 1. 15a. 984.; 15c. 88d.; £1 16c. 28d.
- 8. 83 lb. 4 ca.; 1 cwt. 74 lb. 14.4 ca.; 8 t. 17 cwt. 95 lb.
 - 3. 252 rd.; 80 rd. 4 yd. 1.2 ft.; 21 mi. 118 rd.
 - 4. 145 sq. rd. 6 sq. yd. 64.8 sq. in.; 141 sq. rd.; 18 A. 70 sq. rd.
- s. 25 on. ft. 456 ou. in.; 7ed. 112 eu. ft.; 9 eu. yd. 29 eu. ft. 432 eu. in.
 - 6. 3 pk. 1 gal.; 2 bu. 1 pk. 1 gal.; 5 bu. 1 pk. 1 gal. 3.2 qt.
 - 7. 3 qt. 1 pt.; 5 gal. 1.4 pt.; 7 gal. 3 qt.
- 8. 11 hr. 52 min. 48 sec.; 7 wk. 6 da. 3 hr.; 9 wk. 6 da. 15.hr .36 min.
 - 9. 58' 30"; 2" 50' 51"; 17" 23' 15".
 - 10. 3 ft. 9 in.; 17 rm. 17 qr. 12 sh.; 7 gro. 9 doz.

EXERCISE CXCVIII. PAGE 125.

- 1. £1.525; £7.68125.
- 2. 9.854 t.; 5.70375 t.
- 3. 7.1109375 mi.; 6.089 mi.
- J. 9.8 A.; 7.283 A.
- 8. 7.875 od.; 7.6875 eu. yd.
- 6. 7.8125 bu.; 5.890625 bu.
- 7. 27.875 gal.; 14.875 gal.
- 8. 3.55875 da.; 2.7725 wk.
- 9. 3.8775°; 17.12375°.
- 10. 5.8875 rm.; 24.75 gra.

EXERCISE CXCIX. PAGE 125.

1. \$3380. \$. 10.3826 ft. \$. \$59.375. 4. The latter, 8.875 cu. in. 8. 3.2 lb. 6. \$24.80. 7. 83.75 yd. 8. \$322.28. 9. 199218.75 os.

EXERCISE CC. PAGE 126.

1. \$414. 2. \$109.0625. 3. 75 sheep. 4. \$161.655. 5. 50. a. \$492.61875. 7. 3720. 8. \$53.25. 9. \$4. 10. 13.378 A.

EXERCISE CCI. PAGE 128.

- 1. 67.75 A. 2. 28 yr. 8. \$26484. 4. 7.89, 8.95. 8. \$10.32. a. Gain, \$846.875, \$12.50. 7. A., \$75.87; B., \$57.39. 8. 16.5.
- 9. 1585584 eu. ft. 10. 8.6328 mi., 9.1872 mi.

EXERCISE CCII, PAGE 127.

- 1. \$5. \$. \$96.768. \$. 29.83 in. 4. 2.7 ft. \$. 2.2968.
- 6. .5625; 33.75. 7. 15360. 8. 58 lb. 9. \$24.60. 10. \$192.78.

EXERCISE CCIII. PAGE 128.

- 1. 42.34. \$. 17.3. \$. 8.45, 5.65. 4. 26.1 ed., 24.65 ed.
- 5. 64 mi., 36.25 mi. 6. \$340.05. 7. \$18.8325. S. .7875.
- 9. 4 ft, 3.2 in. 10. 92.4 yd. 11. \$181.50, \$77, \$44. 12. 660 ft. 18, 3446.875 lb. 14, 41 da.

EXERCISE CCIV. PAGE :20.

- 1. 160; 160; 160; 160; 160.
- 2. 14; 14; 14; 16; 16.
- 3. 5%; 7%; 10%; 17%; 25%.
- 4. 51%; 71%; 101%; 121%; 171%.
- 5. (1) .05; .08; .1; .125; .2.
 - (2) 1; 1; 1; 1; 1.
- 6. (1) .11\dagger; .16\dagger; .375; .75; .875.
 - (2) 1; 1; 1; 1; 1.
- 7. (1) 100; 100; 100; 100; 100.
 - (2) 25%; 75%; 40%; 70%; 16%.
- 8. (1) 184; 184; 184; 184; 184; 184.
 - (2) 331%; 661%; 161%; 121%; 871%.
- D. A; 1; 1; A; A.
- 10. 1; 14; 14; 14; 1.

EXERCISE CCV. PAGE 130.

1. \$3; \$20; \$35.

eq. rd. cu. ft.

qt.

15 hr

ı. in,

5 os.

- 2. 16 A.; 20 A.; 12 A.
- 3. 15 words; 33 words; 54 cows. 4. 50 boys; \$374.50; 15 yd.
- 5. \$50; 187½ mi.; 45 hens. 6. 2 men; 2 yd.; 40e.
- 7. \$65; 50 A.; 55 men.
- 8. 30 yd.; 250 sheep; 30 cows.
- 9. \$302; 415 men; 216 books.
- 10. 79; 1456 yd.; \$1602.

EXERCISE CCVI. PAGE 130.

- 1. 20%; 10%; 25%. 8. 10%; 5%; 124%. 8. 50%; 124%; 44%.
- 4. 5%; 7%; 5\$%. 8. 12%; 7%; 5%. 8. 5%; 62\$%; 12\$%.
- 7. \$10; 5 A. 8. 24 lb.; 4 gal. 9. \$42; \$107. 10. \$90; 55 mi.

EXERCISE CCVII. PAGE 130.

1. 444 sheep. 2. \$103. 3. 225 bales. 4. 288 boxes. 5. \$216. 6. 480 A. 7. 120 lb. 8. 200 A. 9. 300., 10. 30 bu.

EXERCISE CCVIII. PAGE 131.

- 1. \$1400. S. \$7760. S. 120 A. 4. \$3375. S. \$29500.
- 6. 4930 sheep. 7. 231 girls. 8. 20277. 8. \$717.25. 10. 73%, 876 sheep.

EXERCISE CCIX. PAGE 131.

1. 661%, 2. 98%, 2. 80%, 4. 50%, 8. 20%, 6. 12%. 7. 25%. 8. 8%. 9. 331%. 10. 40%; 00%.

EXERCISE CCX. PAGE 132.

1. 70. 2. \$2509. 3. \$500. 4. 800 A. 5. 450 sheep. 6. \$4500. 7. 150 lines. S. \$1300. 9. 4500 sheep. 10. 450 pupils.

EXERCISE CCXI. PAGE 132.

1. 8290 bu. . 8. 6%. 3. \$72. 4. \$20. 8. \$12982.50.

6. 48002 lb. 7. \$125. 8. \$5400. 9. \$9000. 10. Lost, 121 %.

EXERCISE CCXII. PAGE 133.

1. 330 rd. \$. \$372. . \$. 10 lb. 4. 48 mi. 5. 2800 books. 6. 224 men. 7. 1880, 2021. 8. 111 %. 9. 18752. 10. 91 %.

EXERCISE CCXIII. PAGE 134.

1. \$112.50; \$216. \$. \$292; \$504. \$. \$106. 4: \$105. \$. \$180. 6. \$150. 7. 4\frac{1}{2}\frac{1}{

EXERCISE CCXIV. PAGE 135.

1. \$270, \$540, \$547.20, \$1051.65. \$. \$057.46. 3. \$10.26.

4. \$3.20. 5. \$25. 6. \$6\$. 7. \$500. 8. \$2.50. 9. 32\%. 10. 46%.

EXERCISE CCXV. PAGE 135.

1. \$25.50. \$. \$8.20. \$. 28%. 4. 46.19%. \$. \$20. 6. \$7.56. 7. \$490.96. 8. \$831%. 9. \$461.70. 10. \$357, 471%.

EXERCISE CCXVI. PAGE 136.

1. Profit, \$2; profit, \$8; loss, \$1.50; profit, \$1.50.

2. Gain, 331%; gain, 562%; gain, 20%; loss, 5%.

3. Profit, \$10; loss, \$40; gain, \$5.20; profit, \$150.

4. \$43; \$75; \$102; \$100. 5. \$100; \$200; \$60; \$72; \$60; \$96.

8. \$30; \$160; \$25; \$700. 7. 25%. 8. 15%. 9. 4%. 10. 42\$%.

EXERCISE CCXVII. PAGE 137.

1. \$1.89. 2. \$926.10. 3. \$38.28. 4. \$9612.50. 5. \$288.

6. \$2719.50. 7. \$60. 8. \$900. 9. 9000 bu. ±0. \$4.20.

EXERCISE CCXVIII. PAGE 137.

1. \$112. \$. \$8600. \$. \$204.70. 4. \$1007.50. 5. \$75.

6. 121%. 7. \$330. 8. 40%. 9. 35A. 10. \$160, \$208.

EXERCISE CCXIX. PAGE 138.

1. \$18; \$8.40; \$24.15; \$56.70; \$209; \$87.50.

#. \$12.50; \$16.10; \$24.40; \$40.50; \$42; \$10.50.

3. \$168.75. 4. \$115.92. 5. \$12.50. 6. \$19.38, 7. \$13.50.

8. 3%, 0. 11%, 10. 31%.

EXERCISE CCXX. PAGE 130.

94500

\$180.

65.

.56.

1. 3%. 2. 25%. 3. 35%. 4. \$14400. 5. \$8400. 6. \$2502.80. 7. 84 et. 8. \$7200, \$216. 9. 186 members. 10. \$3264.

EXERCISE CCXXI. PAGE 130.

1. \$150. 2. \$3650, \$146. 5. \$270. 4. 25000 yd. 5. 60000 lb. 6. 4100 lb. 7. 52000 yd. 8. \$3500. 2. \$367.75. 10. \$4000.

EXERCISE CCXXII. PAGE 140.

EXERCISE CCXXIII. PAGE 141.

1. \$16000. \$. \$2000. \$. \$20000. 4. \$14000. 5. \$420. 6. \$84787.50. 7. \$40000. 8. \$2040, \$5060. 9. \$75. 10. \$2500, \$3500, \$4000.

EXERCISE CCXXIV. PAGE 142.

1. \$54. \$. \$150. \$. \$19.50. 4. \$525. \$. \$652.50. 6. \$22. 7. \$18. \$. 14 mills. 9. 12\frac{1}{2} mills. 6. 17\frac{1}{2} mills.

EXERCISE CCXXV. PAGE 143.

1. \$2800. 2. \$2500. 3. \$544000. 4. \$101.60. 5. \$2500. 6. \$13000. 7. \$5675. 8. 62 mills. 9. \$25. 10. \$114.20.

EXERCISE CCXXVI. PAGE 144.

1. \$6, \$8, \$3, \$7, \$7, \$0. \$. \$0. \$. \$56. 4. \$340. \$. \$10. 6. \$5.39. 7. \$15.12. 8. \$38.88. 9. \$13.20. 10. \$4.6116.

EXERCISE CCXXVII. PAGE 144.

1. \$915.60. \$. \$1012.65. \$. \$2084.02. 4. \$674.01. \$. \$631.65. 6. \$425.656. 7. \$1859.04. \$. \$66. 9. \$1910.20. 10. \$1154.64.

EXERCISE CCXXVIII. PAGE 145.

1. 6%. 2. 7%. 3. 41%. 4. 62%. 5. 62%. 6. 53%. 7. 74%. 3. 41%. 9. 6%. 10. 6%.

EXERCISE CCXXIX. PAGE 148.

1. 1 yr. 8. 1½ yr. 8. 1½ yr. 4. 5 mo. 5. 9 mo. 6. 8 mo. 7. 115 da. 8. 1½ yr. 9. 150 da. 20. 75 da.

COURT PAGE 148.

1. 0540. 2.4005. J. 00 J. 8000. J. 8040. 7. 6006. Ø. 41005, Ø. 4219. 10. 42000.

EXERCISE CCXXXI. PAGE 146.

1. 8250. 2. 8465. 3. 8540. 4. 8572.50. 5. 81320. 6. 9408. 7. \$750. 8. \$1753. S. \$3650. 10. \$3213.

EXERCISE CCXXXII. PAGE 146.

1. \$136.10, \$826.10. 2. \$477.54, \$3977.54. 3. \$76.51, \$1326.51.

4. \$1724.65, \$6724.65. 5. \$11255.09. 6. \$5250. 7. \$960.

8. \$10000. 9. \$4.32. 10. \$124.05.

EXERCISE CCXXXIII. PAGE 148.

1. (1) \$250.

Tonouro, Oct. 27, 1900. Three months after date, for value received, I promise to pay John Smith, or bearer, the sum of two hundred and fifty dollars with interest at six per cent. per annum.

- (2) In the note under (1) substitute or order for or beaver.
- (3) In the note under (1) omit the words or bearer.
- #. \$250. Tonouro, Oct. 27, 1900. On demand, I promise to pay John Smith, or order, the sum of two hundred and fifty dollars for value received.
- J. \$250. Tonouro, Oct. 27, 1900. Three months after date, I promise to pay Thomas Harris, or order, the sum of two hundred and fifty dollars for value received, with interest at four per cent. per annum.

JAMES JOHES. TORONTO, Oct. 27, 1900. Three months after date, at the Bank of Commerce, here, I promise to pay Wm. Meadows, or order, the sum of fifty dollars, for value received, with interest at five per cent. per THOMAS JONES. .

6. \$751.875. 6. \$1485.15.

7. \$350.

Toronto, Ost. 27, 1900. At sight, pay to the order of the Bank of Commerce, the sum of three hundred and fifty dollars, and charge the same to the account of MYSELP.

To PORTER AND JONES, Moutresi.

EXERCISE CCXXXIV. PAGE 148.

| 1. De | y, July 30; | Term o | d Dissount, 80 da.; | Proceed | n. 0045 48 |
|-------|-------------|--------|---------------------|---------|------------|
| 2. " | Feb. 23; | 4 | " 70 da.; | 11 | |
| | | | 10 1001 | | 9799,22, |

5. " Nov. 24; " 45 da.; " 65679.42.

6. " Aug. 22; " 55 da.; " 6115.48.
7. 6325. 8. 6076. 9. 61926.70. 20. 61469.52

EXERCISE COMMIT. PAGE 150.

1.40000. 1.40000. 3.47023.50. 4.41548. 5.40000. 6,41750. 7.43263.50. 8.40750. 9.420400. 10.42000.

9406.

36.51.

00.

dred

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the

200

ars m.

EXERCISE CCXXXVI. PAGE 150.

1. \$700. 2. \$2500. 3. \$3500. 4. \$5600. 5. \$2300. 6. 5. 7. 10. 8. 6. 9. 28. 10. 15.

EXERCISE CCXXXVII. PAGE 180.

1. \$200. 2. \$240. 3. \$200. 4. \$100. 5. \$112. 6. 5\$%.
7. 44%. 3. 5%. 9. 54%.

EXERCISE CCXXXVIII. PAGE 151.

1. \$9100. 2. \$13310. 3. \$11340. 4. \$15570. 5. \$11495. 6. 60. 7. 70. 8. 220. 9. 500.

EXERCISE CCXXXIX. PAGE 151.

1. \$16000. \$. 124. \$. \$18000; 720. 4. 8%. 5. 7%. 6. 31%. 7. \$100. \$. \$640. \$. \$4925.

EXERCISE CCXL. PAGE 152.

1. 1144. 2. 834. 3. 2664. 4. 54%. 5. \$2400. 6. \$14264. 7. 50. 2. \$29400. 9. 5%. 10. \$6400.

EXERCISE CCXLI. PAGE 152.

1. \$1000; \$500; \$200. 2. \$3000; \$1500; \$1000; \$600; \$375; \$300.

3. 16 da.; 5 da.; 4 da.; 2 da. 4. 3 mo. 8. 10 mo. 6. 8 da.

7. 60 days after the debt is due. 8. 6 mo. 9. 62 da.

EXERCISE CCXLII. PAGE 153.

1. 6 mo.; 3 mo.; 4 mo. 2. 120 da. 3. 4 mo. 4. 5 mo.

5. Ap. 23. 6. 112 da. 7. 3 mo. 8. 70 da. 9. 8 mo.

EXERCISE CCXLIII. PAGE 184.

" 1. B, \$450; A, \$600. S. A, \$150; B, \$043. S. A, \$435; B; \$155.

d. A, \$65; B, \$130; C, \$60. S. A, \$984; B, \$400; C, \$1152.

e. A, \$2000; B, \$2400. 7. B, \$250; C, \$225.

#. A, \$1750; B, \$2125; C, \$1125. S. \$720.

10. A, \$2002; B, \$2420; C, \$2200; D, \$2000.

EXERCISE CCXLIV. PAGE 186.

1. A, \$17.50; B, \$22.50. S. A, \$285; B, \$450.

S. A, \$25; B, \$21; C, \$64. d. A, \$75; B, \$175; C, \$330. S. Equally.

6. A, \$2200; B, \$3000. 7. A, \$1225; B, \$675; C, \$1050.

S. 4 mo. S. \$1480. 10. A, \$8445.94; B, \$4054.65. 22. \$4800. 12. C, \$1605 +; D, \$1544 A; E, \$1050.

EXERCISE CCXLV, PAGE 156.

1. 2°=8; 2°=16; 3°=248. 8. 5°=125; 5°=625; 5°=3125.

8. (1)0=1; (1)4=1; (1)0=uffr.

4. (21) = 61; (81) = 3411; (41) 4 = 35211.

8. (.1)*=.001; (.08)*=.000027; (.05)4=.00000635.

6. $(.12)^{\circ} = .001728$; $(.15)^{\circ} = .003375$; $(2.5)^{\circ} = 26.0626$.

7. 2.2.2=8; 3.8.8.3=81; 4.4.4=64.

8. 8. 8=8; 8. 8. 8=84; 8. 8. 6. 6=848.

9. (.5) (.5) (.6) = .125; (.05) (.05) (.05) = .000125;

10. 28 × 21 = 514; 88 × 88 × 88 = 3488; 58 × 58 × 58 × 58 = 750118.

EXERCISE CCXLVI. PAGE 187.

1. 361; 2025; 1296; 8649. 8. 10201; 254016; 620636; 501264.

3. 5715.36; 2190.34; 9506.25; 63.3616. 4. 1; 11; 11; 11; 11.

3. 201; 5011; 901; 1601. 6. 720; 6859; 68921; 758571.

7. 1080801; 1831000; 129554216; 751089429.

8. 28872.625; 94.196875; 481890.304; 386.606673.

9. 4: 186; 1981; 1848. 10. 15\$; 144\$\$; 5671; 376\$\$.

EXERCISE CCXLVIII, PAGE 187.

1. 81; 125; 625; 4096. \$. .0081; .0225; 15.625; .085937.

3. 11; 11; 151; 3411. 4. 2025; 18894; 208512u; 111.

5. 32768; 40353607; 429981696; \$\frac{1}{2}\$. \$6. 12; 64; 216; 243. 7. 80; 15625; .512; 848. 8. 6th. 9. 256. 10. 24th.

11. 49126061. 18. 128787625000. 18. .000000000016.

14. 36°=(2.2.8.3)°=2.2.2.2.3.3.3.3=2°×3°. 16. 10 A.

EXERCISE CCXLVIII. PAGE 188.

1. 9; 11; 12; 16. 8. 27; 56; 64; 81. 8. 160; 314; 266; 527.

4. 4; 16; 17; 18. 5. 11; 18; 18; 18; 18; 18. 6. .1; .06; .00; .20.

7. .947; .005; .068; .16. 8. 12; \$; \$\$; \$.

ally.

9. 3.65; .102; .571; .00563. 10. 2.236; .707; .948; .004.

EXERCISE CCXLIX. PAGE 188.

1. 490. 2. 40). 3. 3202. 4. 24 yd. 5. 440 yd. 6. 200 rd. 7. 372 ft. 8. \$100. 9. 144 rd. 10. \$334.

EXERCISE CCL. PAGE 159.

1. 75 yd., 25 yd. 2. 220 yd., 44 yd. 3. 14 in. 4. 17 rd. 5. 1440 rails. 6. 280 rd. 7. 8030 yd. 8. 15 ft. 9. 221 yd. 10. 7712 yd.

EXERCISE CCLI. PAGÉ 150.

1. 6; 8; 9; 12. 4. 15; 16; 18; 21. 3. 25; 24; 28; 23.

4. 35; 40; 55; 56. 5. 17; 23; 20; 37. 6. 53; 59; 67; 71.

7. 101; 111; 160; 180. 8. 10; 10; 14; 14. 9. .1; .06; 11.6; 36.8. 10. .928; .4308; .2; 1.709.

EXERCISE CCLII. PAGE 100.

1. 25; .25; 1.23; 10.04. 2. 21; 91; 71; 71. 3. 36.2.

4. 5476 sq. ft. 5. 56454 sq. ft. 6. 17 ft. 7. 60 in. 8. 9.2 in.

9. 12 ft. 10. 15.75 in. 11. 87 ft. 18. 5 ft. 18. 12. 14. 36 ft.

EXERCISE CCLIII. PAGE 162.

1. 1521 eq. yd. 8. 29 eq. ft. 56 eq. in. 8. 1144 eq. ft.

4. 210 ft. 5. 2 ch. 40 l. 6. (a) 229 eq. in. (b) .54 A. (c) 26 eq. ft.

7. 5% sq. ft. 8. 16 rd. 9. 80 rd. 10. 960.

EXERCISE CCLIV. PAGE 163.

1. (a) 186 sq. ft. (b) 31914 sq. ft. (c) 548 A. (d) 314 A.

2. 50 in. 3. 57 in. 4. 92 rd. 5. 4300 sq. ft. 6. 2145 sq. yd.

7. 1715 aq. ft. 8. 554f aq. yd. 9. 203 aq. ft. 10. 56 ft.

EXERCISE CCLV. PAGE 163.

1. 44 in.; 66 in.; 11 ft.; 513 ft.; 733 ft.; 14 ch. 96 l.

8. 7 in.; 17t in.; 19t fk.; 1 eh. 71t 1.; 7. yd.; 21 yd. 7 in.

3. 244 min. 4. 111 rd. 1 ft. 10 in. 5. 5 ft. 6. 7. 7. 414 ft.

8. 84 yd. 9. 12 ft. 10 in.

10. 22 in.; 33 in.; 55 in.; 66 in.; 110 in.; 121 in.

EXERCISE COLVI. PAGE 104.

J. 960\$ eq. in.; 1805 eq. in.; 2000 eq. in.; 2004 eq. in.; 2000 eq. in.; 2004 eq. in.; 2006 eq. in.; 7. 200.00 yel. S. 277\$. A. 210 sq. in. St. 0000\$.

EXERCISE COLVII. PAGE 166.

1. (a) 86; (b) 880; (c) 1730; (d) 684.

8. (a) 500; (b) 1200; (c) 44; (d) 146.

8. (a) 486; (b) 700; (c) 200; (d) 205. 4. 20 ml. 5. 25 ft.

e. 274 ft. 7. 20.78 in. 8. 11.18 ft. 8. 10 ft. 10. 654.60.

EXERCISE CCLVIII. PAGE 165.

2. 924 on. in.; 34ft on. in.; 14 on. ft., 197 on. in.; 68 on. ft., 165 on. in.

#. 121¢ eq. in.; 60¢ equ in.; 35s'e eq. ft.; 100s'e eq. ft.

s. 314 on. ft.; 804 oq. ft. d. 1314 on. ft.; 1814 oq. ft.

s. 20 in.; 4ff ou. ft. s. 0412. 7. 10f ft. s. 25f ft.; 17 ft.

0. 20.00 in. 20. 1660 mal.

EXERCISE CCLIX. PAGE 100.

1. (a) 0f on. ft.; (b) 115f on. ft.; (c) 385 on. ft.; (d) 123ff on. ft. s. (a) 20% aq. ft.; (b) 122 aq. ft.; (c) 220 aq. ft.; (d) 1824 aq. ft.

s. 5ff en. yd. d. 906. S. (a) 31ff eq. ft.; (b) 151f eq. ft.;

(e) 297 eq. ft.; (d) ?96 eq. ft., 101 eq. in. 6. 91f eq. ft.

7. 824.75. 8. 111. 0. 1 yd. 10. 148 au. ft.

EXERCISE CCLX. PAGE 100.

1. 106 en. ft. s. 2700 en. in. s. 75 eq. ft. d. 22 eq. ft.

8. \$83.75. 6. 19250 ett. in. 7. (1) 86\$ aq. ft.; (2) 33 ft.

s. 80.51 yd. 9, 80f on. ft. 20, 61 in.

EXERCISE CCLXI. PAGE 167.

1. (a) 154 sq. in. (b) 381 sq. in. (c) 616 sq. in. (d) 2464 sq. in.

8. 824.64. 3. 14 ft. 4. 132 ft.

8. (a) 906† eu. in. (b) 7941† eu. in. (c) 1437† eu. in. (d) 179† eu. in.

6. 4661 en. ft. 7. 12f en. ft. 8; 4 in. 9. 110602. 20. 2541.

EXERCISE CCLXII. PAGE 167.

1. 22.0 ft. 2. 28 yd. 2. 68 yd.; 267 eq. yd. 4. 391 ft.

8. 75 ft. 6. 43.3 sq. ft. 7. 32 ft. 8. 98 yd. 8. 820 in.

EXERCISE CCLXIII. PAGE 100.

1. 43 ft. 8. 242 yd. 8. 022\$, 4. 25. 6. 28 ml. 6. 4.24 ft. 7. 140 rd. 8. 4 ft. 8, 80001 lb. 49, 83.30.

EXERCISE CCLXIV. PAGE 100.

1. 14 ft. S. S in. tiles. S. 136 ft. d. 706 eq. ft. S. 170 ft. 6. 14175 eq. ft. 7. 5544 eq. ft. 6. 79194 eq. ft. 9. 160 eq. ft. 10. 346j eq. in.

EXERCISE-CCLXV. PAGE 100.

1. 80 ft. 80 ft. 8, 5 A. 8, 8282 eq. ft. 4. 28 eq. ft. 5. 80 rd.; 120 rd.; 80.44 rd. 6. 1560a q. in. 7. 05 ft., 66 ft.; 69 ft. s. 72 ft. s. 2046 eq. in.; 4376 eq. in. 20. 112} ft.

EXERCISE CCLXVI. PAGE 170.

1. 63 ft. S. 306 sq. ft.; 385 sq. ft. J. 316.05 yd. J. 3630 mea. 8. 4900 ft. 6. 40 rd., 20 rd. 7. 2.73 ft. 8. 12 ft. 9. \$28.32. 10. 482.

EXERCISE CCLXVII. PAGE 170.

1. 52 ft. 2. 10.30 yd. 3. 23.54 eh. 4. 3} eh. 5. 56 yd. 6. 42 ft. 7. 414.12 ft. 8. 21.213 ft. 9. 292† aq. ft. 10. 48† c. ft.

EXERCISE CCLXVIII. PAGE 171.

1. 38} sq. ft. 8. 34.64 in. 3. 27.71 in. 4. 27} ft.; 20 ft. 8. 1925 lb. 6, 864. 7. 193000 shet. 8. 343 dos. 9. 12 in. 10. 48 as.

EXERCISE CCLXIX. PAGE 173.

1. Thirty-seven, and five-tenths metres; twelve, and seven-tenths contimetres; forty-eight, and three-tenths millimetres; seven, and eight hundred and sixty-five dekametres; nine, and seven-tenths decimetres.

2. (1) 466 cm., (2) 45.60 dm., (3) 4.560 m.

s. (1) 18.7 m., (2) 18700 mm., (3) 1870 cm. d. 1897009.424 m.

S. 780.48 m.; 11.08 mm, S. 92.206 m.; 290.18892 m.

7. 640 leaves. 8. 27600 times. 9. \$76.56. 10. 7.6375 mi.

11. \$655705. 19. 28000 times.

EXERCISE CCLXX. PAGE 174.

1. 287.6345 hectares. 2. 37856 ares.

3. 57596 sq. em.; 5759600 sq. mm. 4. 2341700 sq. m. S. 542 sq. em.

6. 3020303 sq. m. 7. 112 ares. 8. 32.64 sq. m. 9. 62.50.

10. 200500 brieks.

74.

EXERCISE CCLXXI. PAGE 174.

1. 72.5 mt. 2. \$432.50. 3. 25800 1. 4. 23.875 e. m. 5. 2.604 m. 6. 1.40 c. m. 7. 30 cm. 8. 300 Hl. 9. \$275.31. 10. 8 ct.

EXERCISE CCLXXII. PAGE 175.

1. 5037 g.; 508.7 Dg. 2. 3078 mg.; 30.75 dg. 5. 8079006.5 cg.

4. 2.756 Kg.; 275600 ag. S. 7.28 l. 6, 4750. 7. 264.6 Kg.

8. \$420.15625. 9. 810 mg. 10. .00504.

EXERCISE CCLXXIII. PAGE 176.

1. (a) 70.25 m.-(b) 808.7 l. (c) 15.908 a. (d) 27000.37 g.

2. 594 Kg. 3. 47250 Kg. 4. 2100 coins. 5. 388 g. 6. 110 at.

7. 225 france. 8. 33 Hl. 9. 650 g. 10. 200 m. 11. 50 et. 12. 190 mi. 13. 477 times. 14. 13.44 rolls,

EXERCISE CCLXXIV. PAGE 177.

1. .\$; .4\$; .96; .766. 2. .4; 142857; .285714; .428571.

3. .571428; .714285; .857142; .076923.

4. .230760; .884615; .692907; .68. 8. .83; .583; .9318; .9285714.

6. .9428571; .954; .89285714; .15990.

7. .7063; .4166428571; .54861; .164773.

8. .44200760; .721158846; .1392045; .360962.

9. .20238096; .8270; .140766; .5050678.

10. .170138; .696789772; .86207856142; .20145.

EXERCISE CCLXXV. PAGE 178.

7. 111; th; th; th; th. 8. 11; th; th; 11.

9. 11 itt; 211; 711. 10. 411v; 51tr; 711x; 51.

EXERCISE CCLXXVI. PAGE 178.

1. 6.60244. J. 2.3060941229258. J. 9.4860; 14.0636727.

4. .82457; .82147. 5. .73231777. 6. 1.590; 6.893. 7. 339; .429.

8. .4675; .350649. 0. 63; 10. 10. .54175; 7.805,

EXERCISE CCLXXVII. PAGE 178.

1. 10.5. 2. .42. 4. .161; .03. 6. 33.142857. 7. £2 00. 81. 8. 3 t. 8 cwt. 35.3 lb. 9. 6 mi. 92 rd. 1.6 yd. 10. 69 t. 868.8 lb.

EXERCISE CCLXXVIII. PAGE 179.

1. Those which in their lowest terms have 2's and 5's, or 2's or 5's as the prime factors of their denominators.

2. When reduced to lowest terms, each denominator has only 2's and 5's, or 2's or 5's as its prime factors.

3. to, 1; 1, 3; 11, 5; 100, 3.

4. Because their denominators have other factors than 2 or 5.

S. 1, 1; 17, 1; 18, 1; 11, 3; 14, 5.

6. 7.456. 7. $(.005 \times .04) \times .(005 \times .04) = .0002 \times .0002$.

8. To multiply by 10, 100, 1000, &c., move the point 1, 2, 3, &c., places to the right.

To divide by 10, 100, 1000, &c., move the point 1, 2, 3, 40., places to the left.

9. .13.

EXERCISE CCLXXIX. PAGE 179.

1. \$3780. 2. 9215 ou. ft. 3. \$132, \$247.50, \$275. 4. \$100. 5. .0078125. 6. 33 mi. 7. .405 hr. 8. 164 %. 9. .00129.

EXERCISE CCLXXX. PAGE 180.

1. 1. 2. 1 da. 3. 31 da. 4. 14.7 da. 5. 1.

6. A, 27 da.; B, 54 da. 7. A, 19f da.; B, 9f da.; C, 39f da. 8. 4f da.

9. 18 da. 10. 41 hr. 11. A, 36f da.; B, 73f da.; C, 110 da.

13. 15 da. 13. 32 hr. 14. 11 hr. 15. 8 horses.

16. A, 31 da.; B, 31 da.; C, 51 da. 17. A, \$1.10; B, \$1.

EXERCISE CCLXXXI. PAGE 181.

1. 12 min.; 24 min.; 30 min. \$. 18 min. \$. 16 4 min. past 3. 4. 16 min. past 6. 5. 32 min. past 6. 6. 24 min. past 5.

7. 24 min. past 6 and 41 min. past 6.

8. (a) 43 min. past 8, (b) 27 min. past 8, (c) 10 min. past 8.

2. 40 min. past 9; 54 min. past 10; 12 o'clock.

10. 23 min. past 5.

EXERCISE CCLXXXII. PAGE 182.

1. 13 min. past 4. S. 19 min. past 3. S. 3123 min. past 6.

4. 120 da.; 44 min. past 11; 14 min. past 12. 5. 75 da.

6. 36 min. past 6 a.m., Friday. 7. 54 min. past 5.

8. 51 min. past 9 p.m. on Saturday, and 571 min. past 8 p.m.

9. 3 p.m., May 8. 10. 434111 min. past 9 p.m.

EXERCISE CCLXXXIII. PAGE 182.

1. 44 ft. 2. 34 mi. 3. 221. 4. 71 sec. 5. 14 min. 94 me. 6. 8 hr. 7. 334 mi. 4. 71 yd. 9. 3244. 10. Gains 10 14 min.

EXERCISE CCLXXXIV. PAGE 183.

1. 224, 141; d. 4 mi. d. 8 mi. d. 4 hr. 5. 44 mi. 6. 2 mi. 7. 45 min. 8. 3 mi. 9. 5 to 1. 20. 21 hr.

EXERCISE CCLXXXV. PAGE 184.

1. 14 mi. 8. 45 mi., 36 mi. 8. 114 yd. d. 45 mi. 8. 11 min. 8. 306 ft. 7. 944 yd. 8, 22 mi. 9. 234 mi. 10. 68 mi. 12. 68 hr.

EXERCISE CCLXXXVI. PAGE 188.

. 1. \$1.92, S. 325, 175, 125. S. \$630. 4. 74; 2s. 8id. S. 17. 6. 23. 7. £16 6s. 8. 1980. 9. 2 hr. 24 min. 10. 200 lb.

EXERCISE CCLXXXVII. PAGE 185.

1. 144 min. S. Men, \$12.50; women, \$8; boys, \$5.25. S. 7 bbl. 4. 1022. 8. 75 yd. 6. 32 da. 7. 17 mi. 8. \$80.

9. 110 sheep; 140 pigs. 10. \$51.

EXERCISE CCLXXXVIII. PAGE 186.

1. \$12900. S. 128 gal. S. \$672. 4. 790 apples. S. \$75.

6. £140. 7. \$97.50. 8. 223 sec.

9. John, \$680; Thomas, \$176; Henry, \$22. 10. 56 et.

EXERCISE CCLXXXIX. PAGE 187.

1. \$27. 2. 26 ft. 6 in. 3. 4 ft. 1 in. 4. 15 et. 5. 2686 rails. 6. 20, 21, 22, 22. 7. 182. 8, \$60. 9. 7875 shingles. 10. 150 lb.

EXERCISE CCXC. PAGE 187.

1. \$00, \$60. 2. 3 mi. 3. 87 da. 4. Latter, 51 ct.

5. \$20.0246. 6. \$8460. 7. \$870, 6%. 8. \$2.50. 9. 19 da.

EXERCISE CCXCI. PAGE 188.

1. \$900, \$1350, \$1800. 2. \$36. 3. Gain, 72 et. 4. 230400 A. 8. 49.90 rd., 37.48 rd. 6. \$2.50. 7. 100 ft. by 73 ft. 3. 4821.25. 9. 4354. 10. 47.50.

EXERCISE CCXCII. PAGE 180.

1. A, 30 ct.; B, 36 ct.; C, 40 ct. 2. 160 leaps. 3. \$2450.

4. 130} sec. 5. \$500. 6. 80c. • 7. 12 yd.

8. 900 lb. at 7 ct.; 1100 at 10 ct. 9. 248 yd.; 62 yd. 10. \$449.

EXERCISE CCXCIII. PAGE 139.

1. 396 ft. 2. \$329. J. Divisor, 547; Quot., 3233. 4. \$4\$. 6. \$23.59. 6. A's rate is to B's as 79 to 60. 7. 400036220 post-holes. S. A, \$482; B, \$216; C, \$1296. S. \$1880.

10. 1000: 0450.

EXERCISE CCXCIV. PAGE 190.

1. 294; 84. 8. 8900, 8750. S. \$200. 4. 10. 5. \$400. 6. 4240; 5 yr. 7. 4 in. 8. 300 leaps. 9. 9 hr. 10. 24 mi.

mi.

min.

hr.

17.

bbl.

He. Ιb.

25.

EXERCISE CCXCV. PAGE 191.

1. 04.80. 1. 8%, 9%. 8. 814%. 4. 3000A bu. 5. 224. 6. 60 mi. per hr. 7. 16† da. 8. 821† cu. yd. 9. 5% da. 10. A, \$776.16; B, \$693; C, \$630; D, \$600.

EXERCISE CCXCVI. PAGE 192.

1. 495 bu. 2. 24 ft. by 18 ft. by 12 ft. 3. 4.5 cu. ft. 4. Gain, \$14. 5. 8000 oranges. 6. 54s.; 56 cs. silver; 160 cs. gold. 7. \$2480. S. 11 mi. per hr. S. 30 min. past 4 a.m. 10. \$217.80.

EXERCISE CCXCVII. PAGE 193.

1. 1152 sq. ft. 2. 4%. S. 11. 4. 14.625 in. 8. 11; .675. J. 14.288 to 1. 7. 482 et. S. 431. 9. \$1.80. 10. 190.

EXERCISE CCXCVIII. PAGE 193.

1. 272 rd. 2. 771. 3. 24 ct.; loss, 4%.

4. Length, 34 ft.; width, 26 ft.; height, 12 ft. 5. 4f mi.

6. 3675\$ t. 7. \$441. 8. 68 yr.; 35 yr. 9. 567 leaves. 10. 104 da.

EXERCISE CCXCIX. PAGE 194.

1. 213 plants. 2. \$4500. 3. 22 mi. 4. 100 lb. 5. 28 et. 6. \$3625. 7. \$4000.

8. .384 in. (Note, their length and width being equal.)

9. 164.7114 in. 10. A, \$1035; B, \$1656; C, \$2025.

EXERCISE CCC. PAGE 195.

1. 2 to 5. 2. 13 min. past 4, or 30 min. past 4. 3. \$40. 4. 5 yd. 5. \$1.02; 80 ct. 6. \$3250; \$2600. 7. 28311 ft.

8. 3 to 2. 9. 21 ft. 10. \$1600; 15 mo.

EXERCISE CCCI. PAGE 196.

1. 1. 2. B, \$2.901; A, \$5.001. 5. 10 mo. 4. 10 in. 5. \$3.

6. 90. 7. 3 hr. 8. 525 lb., 496 lb., 390 lb.

9. \$2100, \$1750, \$1050, \$700. 10. B, by 50 yd. in 41 min.

EXERCISE CCCII. PAGE 197.

1. 141.4 eq. ft. 2. A, \$600; B, \$780; C, \$180; D, \$2000.

3. \$2000; \$1296. 4. 4%; 41%. 5. 60 et. 6. 32 men. 7. 151 mi.

8. 962500. 9. 111 min. past 12. 10. 49 fc; 40f.

PART II.

Solution of Certain Problems.

Norg.—In the following solutions the multiplier is usually written to the left of the multiplicand and is to be read TIMES.

EXERCISE LX. PAGE 44.

1. The factors of 35 are 5 and 7.

As the last remainder is 6 the second divisor must be 7;

First quotient= $(7 \times 72)+6=510$; Number= $(5 \times 510)+2=2552$.

Number of yards in first piece = 155 = 80;
 Price of 1 yard of second piece= 155 c. = 20c.

EXERCISE LXII. PAGE 45.

8. Number of men to do the work in 45 da.=60;"

" 1 da,=45×60;

Number discharged=(60-54) men=6 a

10. Number of men to do 1 work in 36 da.=25;

6.6

1 da.=36×25:

1 " 12 da = 36×25

3 " 12 da. $=\frac{3\times36\times26}{12}=225$.

EXERCISE LXVII. PAGE 48.

It is clear that the quantity to be bought is the least number of pounds which added to 17385 pounds will make the result contain.
 pounds.

17385-68=255 and 45 remainder. Quantity to be bought=(68-45) lb.=23 lb.

EXERCISE LXXVI. PAGE 87.

10. Weight of wool from 1 sheep=7 lb. 8 os.;

"" 2 " =2×(7 lb. 8 os.)=15 lb.;

" 360 " =(\$\frac{1}{2}\$\times 15\$) lb.;

=2700 lb.=27 ewt.

Value of 1 ewt. of wool=\$19.60;

" 27 " =\$(27×19.60)=\$529.20.

ly

EXERCISE LXXVIII. PAGE 58.

7. Cost of building (25—30) yd., or 5 yd.=12s. 6d.;

1 yd.=\frac{12s. 6d.}{5} = 2s. 6d.

75 yd.=75 \times (2s. 6d.);
=£9 7s. 6d.

EXERCISE LXXIX. PAGE 59.

Between noon on Monday and 8 p.m. on Wednesday are 56 hours.

Time gained in 8 hr.=45 sec.;

1 hr.=\frac{4}{2} sec.;

56 hr.=(56\times\frac{4}{2}) sec.=5 min. 15 sec.

The clock will show 8 hr. 5 min. 15 sec.

9. Quantity of hay eaten = (120×20×7×20) lb.;

= \frac{120×20×7×20}{2000} \tau.=168 \tau.;

Quantity of oats eaten = (120×20×7×10) qt.;

= \frac{120×20×7×10}{32} \text{bu}.=5250 \text{bu}.;

Cost of 168 t. hay = \frac{168×8}{6250×\frac{160}{160}} = \frac{1344}{1575};

Cost of hay and oats = \frac{120}{2000} \text{cost} = \frac{120}{100}

EXERCISE LXXXII. PAGE 63.

8. Perimeter of lot=(2×60+2×144) ft.=408 ft.;

Number of post holes=4f4=68;

Cost of digging 1 hole=5e.;

"" 66 " =(68×5)e.=\$3.40.

f. Number of rods in 1 mi.=220;

'' fence=2×220=640;

Length of wire used=(5×640) rods;

Weight of wire used=(5×640) lb.;

Cont of 1 lb.=8e.;

Cont of (5×640) lb.=(5×640×8)e.=2256.

EXERCISE LXXXIII. PAGE 63.

9. Area of surface within the outside boundary of the path = (140×70) sq. ft. =9800 sq. ft.;

Area of rectangular plot= (180×80) sq. ft. =7890 sq. ft.;

.'. area of path= (9800-7800) sq. ft.=2000 sq. ft.

10. Average width of beard=\frac{19\times 18}{2} in.=16 in.;

Area of board=(18\times 12\times 16) eq. in.;

=\frac{18\times 12\times 16}{144} eq. ft.=24 eq. ft.

EXERCISE LXXXIV. PAGE 64.

6. Width of lot=\frac{1600\times 9}{240} ft.=60 ft.;

Perimeter of lot=(2\times 240+2\times 60) ft.=600 ft.;

Cost of fencing 1 ft.=25c.;

600 ft.=(600×25)e.=\$150.

10. Area of farm=*ff*a.=80a.;
Width of farm=\frac{80 \times 160}{300} rd.=64 rd.;

Perimeter of farm=(2×200+2×64) rd.=528 rd.; Cost of fencing 1 rd.=\$1.25; '' 528 rd.=528×\$1.25=\$660.

EXERCISE LXXXV. PAGE 65.

1. Area of room= (94×15) sq. ft.= $(94 \times 15 \times 144)$ sq. in.; ... Length of earpet= $\frac{94 \times 15 \times 144}{36}$ in. = $\frac{24 \times 15 \times 144}{3 \times 12 \times 36}$ yd.=40 yd. Or, Area of room= (94×15) sq. ft.; Length of earpet to cover (3×3) sq. ft.=1 yd.; 11 11 (24 × 15) sq. ft.= $\frac{24 \times 15}{3 \times 3} \times 1$ yd.=40 yd.

EXERCISE LXXXVI. PAGE 65.

Width of room= (18×12) in.; No. of strips in width= $\frac{18\times12}{36}$ —6. Length of room= (27×12) in.; No. of strips in length= $\frac{27\times12}{36}$ —9.

EXERCISE LXXXVII. PAGE OG.

4. Area of coiling= (24×18) sq. ft. = $\frac{24\times18}{9}$ sq. yd.;

Cont of plastering 1 sq. yd.=19c.;

6. Perimeter of room=(2×27+2×18) ft. =90 ft.;
Area of entire walls=(90×10) sq. ft. =900 sq. ft.;

Area of 3 doors=(3×7×4) eq. ft. =84 eq. ft.; Area of 3 windows=(3×6×3) eq. ft. =54 eq. ft.; Area of 1 window=(1×6×4) eq. ft. =24 eq. ft.

Area of doors and windows=(84+54+24) sq. ft. =162 sq. ft.;

(1) Area to be plastered=(900-162) sq. ft. =82 sq. yd.; (2) " =(900-81) sq. ft. =91 sq. yd.

EXERCISE XC. PAGE 60.

8. By drawing a diagram of the foundation it will be seen that two of the walls are 60 ft. long and two of them 32 ft. long.

Length of walls=(2×60+2×32) ft.=184 ft.; Cubic content of walls=(2×8×184) c. ft. =2944 c. ft.; =100 c. yd. 1 c. ft.

EXERCISE XCI. PAGE 60.

10. No. of cords in the pile= $\frac{2441}{105}$ =105. Cubic content of pile= $\frac{105\times128}{5\times12}$ ft.=224 ft.

EXERCISE XCII. PAGE 70.

f. Length of wall=193 ft.;

By drawing a diagram of the foundation the following will be readily seen:

Length of the two side-walls=(2×00) ft.;

Remaining length of wall=(192-190) ft.=72 ft.;

Length of end-wall=(194+4) ft. = 40 ft.;

... Width of barn=40 ft.

EXERCISE XCVII. PAGE 73.

- 7. Value of first+(3 times value of first+\$150)=\$13050;
 ... 4 times value of first=\$(13950-150);
 ... =\$1450;
 ... =\$3450;
 ... =\$3450;
- 9. It is easily found that A owns 72 a. and B 48 a. Value of A's land=\$(72×84);

 B's "=\$(72×84);

 ... value of 1 a.=\$\frac{72×84}{48}=\$126.

EXERCISE XCVIII. PAGE 73.

6. \$1+\$2+\$3=\$6.

Every time \$6 is divided, the first gets \$1; the second, \$2; and the third, \$3.

- 9. When B receives \$1, A receives \$3, and C \$4 out of \$3.

 Share of A=\frac{1\frac{1}{2}}{2} \times \$3 = \$420;

 B=\frac{1\frac{1}{2}}{2} \times \$1 = \$140;

 C=\frac{1\frac{1}{2}}{2} \times \$4 = \$560.
- 10. Value of first house=2 times value of other two;
- 3 times value of other two houses=\$16410;

value of first house=2×\$5470=\$10940.

```
(Value of third+6570)+value of third=45470;
            .'. 2 times value of third=#(5470-570)==$4900;
                             teond=#(3450+570)=42626.
                EXERCISE XCIX. PAGE 74.
                Value of first=value of first;
   1.
                                r + +42+43;
                        thirds
                         all=3 times value of first+$7;
           e value of first+$7=$31;
                  ***
                           =8(31-7)=836;
                  second = $(8+2) =$104
               " third =$(10+3)=$13.
           Length of second=length of second;
                       first= 10 " +25 yd.;
                               24 7 76
                                         +25 yd.+19 yd.;
               44
                        all=3 times length of second-69 yd.;
. . 3 times length of second +00 yd.=444 yd.;
             " =(414-60) yd.=375 yd.;
. . 3
                   4.6
                            =414 yd.=125 yd.;
                  first
                             , =(125+25) yd.=150 yd.:
                             '=(150+19) yd.=169 yd.
                 .third
 11. If instead of 5 bu. of oats, 5 bu. of wheat had been bought,
the cost would have been (5×33)c. more.
     Hence, cost of 13 bu, of wheat=$(6.80+1.65)=$8.45;
              " 1 " = \\e.
                           oats=(65-33)e. =32e.
 12.
               (Red+White) marbles=192;
(Blue+White)
... (Red+Blue+White+White)
               (Blue+White) = 199;
```

and (Red+Blue+White)

=301:

=286:

Red =192-106=87; Blue =199-195=

... White = 105;

EXERCISE CH. PAGE 76.

Cook of 500 bm. — (500×73)e.=30000e.;

500 bm. @ 70e.=(500×70)e.=35000e.;

Difference from real cost= 1000e.;

Grantity of the dearer kind increases the cost by So.

Quantity of the dearer kind=1400 bu. =200 bu.;

chaper '' =(500-200) bu.=200 bu.

EXERCISE CHI. PAGE 77.

Cost of 4 lb. © 330.=1200.;

1 3 lb. © 350.=1050.;

2 lb. © 410.= 250.;

3 lb. =3150.;

1 lb. =4140.=350.

9. As the number of men are in proportion to 1, 4, and 10, we may suppose 1 man receives \$13 per week; 4 men, \$9; and 10 men, \$5.

Hence, wages of 1 man @ \$13=\$13;

4 men @ \$0=\$36;

10 " @ \$5=\$50;

11 15 " =\$00;

EXERCISE CVIII. PAGE 86.

7. As the loads are to be as few as possible, they must be as large as possible.

441=3×3×7×7; 567=3×3×3×3×7; 315=3×3×5×7; Hence, G.C.M.=3×3×7=63; Mumber of bushele in a lead=63.

EXERCISE CIX. PAGE 81.

10. Find the G.C.M. of 12200 and 44100;

18280)44100

39699

4410) 13230 13230

Next find the G.C.M. of 4410 and 118125; This is readily found to be 315. Find the G.C.M. of 720100 and 912220.

| 730100 | 1 | 013.50 |
|--------|----|--------|
| 772020 | 4 | 720100 |
| 59890 | 4 | 190230 |
| 36160 | 3 | 211200 |
| 10720 | 1 | 18060 |
| 1,5000 | 13 | 16790 |
| 760 | 2 | 1330 |
| 700 | | 1520 |
| | | . 100 |

The G.C.M. of 190 and 211100 is easily found to be 19.

EXERCISE CX. PAGE 81.

1305=3×5×7×13; 1785=3×6×7×17; G.C.M.=3×5×7=105.

To find all the common measures, form as many series as there are different prime factors, making I the first term of each series and multiply these together.

1, 3 1, 5 1, 3, 5, 15 1, 7 1, 2, 5, 15, 7, 21, 25, 165.

5. If the number will divide 2000 and leave 11, it will be contained exactly in 2000—11, or 1989.

Similarly, the number will be contained exactly in 2708-17, or 2001;

The G.C.M. of 1989 and 2001 is 117.

EXERCISE CXIR. PAGE 83.

9. 43680=2×2×2×2×2×3×5×7×13.

These can be readily arranged into four consecutive numbers as follows:

18; 7×2; 5×3; 2×2×2×2, or 13, 14, 15, 16.

EXERCISE CXLV. PAGE 96.

Cost of 500 cords=#(500×21) =\$14371;

Bum received for 752 cords=#(752×41) =\$292;

(500-752) cords=4242 cords:

Hum received for 424} cords=\$(424\delta \in) =\$2121\delta;
Total received=\$(200\delta + 2121\delta) =\$2440\delta;
Gain=\$(2140\delta - 1437\delta) =\$1012.

8. No. of yards sold at a gain=\$ of 150=100;

less=\$ of 150=50;

Gain on 100 yd.=\$(100×\$) =\$00\$;

Loss on 50 yd.=\$(50×\$) =\$0\$;

Not gain=\$(00\$-\$)=\$00\$.

s. Part ewned by the third=(1-f-1)=1; Where of third=1 of \$0000-00125.

EXERCISE CL. PAGE 100.

The following is the generally received usage respecting the signs of operation in arithmetic:

- I. The operations indicated by "of", X, and + should be performed before adding or subtracting.
- II. The operations indicated by × and + should be performed in the order in which they coour.
- III. The operation indicated by "of" should be performed before that indicated by +. In this case custom makes a distinction between × and "of."

EXERCISE CLIV. PAGE 102.

8. Reduce 33t, 67t, 70t to equivalent fractions with a common denominator.

206-454; 674-442; 705-451;

As the grain is to go into the smallest number of bags, the bags must be the largest passible.

The G.C.M. of 270, 860, and 567 is 27.

Hence, the G.C.M. of \$\frac{4}{2}\$; \$\frac{4}{2}\$, and \$\frac{4}{2}\$ is \$\frac{4}{2}\$.

Each will soutain \$\frac{4}{2}\$ bu., or \$\frac{2}{2}\$ bu.

\$3\frac{2}{2}\$=\$10\$; \$67\frac{1}{2}\$=\$20\$; \$76\frac{1}{2}\$=\$21\$;

Hence, number of bage=\$10+20+21=51.

EXERCISE CLUL PAGE 105.

8. Weight of 1 lb. Avoirdapois—7000 gr.;
1 lb. Troy ==8700 gr.;
1 gr. is vote of 7000 gr.;
.'. 8700 gr. is \$155 of 7000 gr.;
\$1500-100.

EXERCISE CLXIV. PAGE 107.

7. 61 mi. 224 rd.=19744 rd.; Time to walk 22 rd.=1 min.; '' 1 rd.=½ min.; '' 19744 rd.=(19744×½) min.=10 hr. 17 min.

EXERCISE CLXVI. PAGE 100.

1 hr.=(60×60) sec.; 20 mi.=(30×6000) ft.; Distance the train goes in (60×60) sec.=20×5000 ft.; 1 sec.= $\frac{30×5200}{60×60}$ ft.=44 ft.

EXERCISE CLXVIII. PAGE 100.

EXERCISE CLXXI, PAGE 110.

5. B's part exceeds A's by (13-14), or 15 of web;
15 of web, or 5 of web=5† yd.;
.'. the web=(6×5†) yd. =83 yd.;
A's part=(15 of 33) yd.=13† yd.;
B's part=(15 of 33) yd.=19† yd.

5. Width of first field=
$$\frac{15\times160}{80}$$
 rd.=30 rd.;
Length of second $^{11}=\frac{9\times160}{20}$ rd.=48 rd.

EXERCISE CLXXIII. PAGE 111.

- 5. Mumber sold to drover my of sheep:
 - remaining = of sheep;
 - sold to neighbor of i of sheep;
 - remaining now = f of t of sheeps of sheep;
 ... f of sheep=100 sheep;
 - sheepmf of 100 sheep=450 sheep.
- f. Length of read=(2×5280) ft.:

Rise of road in 10 ft.- i ft.;

.'. Rise of road in (2×5200) ft.=(2×528×3) ft.=176 ft.

- 9. Part received by wife = t of estate:
 - remaining __i
 - " received by eldest son = f of f of estate;
 - " remaining now = t of t " = ty estate;
 " received by daughter = t of th " = ty
 - · to estate=\$750
 - ... * estate=#(16×750)=#12000.

EXERCISE CLXXIV. PAGE 112.

- S. If the first field yields I share of 462 ha.; the second field yields 2 shares of 462 bu.;
 - .'. 8 shares=482 bu. 1.
 - ... 1 " = Aga bq. = 1609 bu.=yield of fret; and 2 " = (2×1609) bu.=3214 bu.=yield of second.
- 8. Share of first =12} a.;
 - secondard of the land;
 - third will a.+! of the land;
 - all = 25 a.+2 of the land;
 - of the landw26 a.t.
 - the lands (4×25) s,=100 s.

EXERCISE CLXXV. PAGE 113.

9. As the lots are to be square, the length of each must be the G.C.M. of 2012 rd. and 412 rd.

The G.C.M. of 2014 rd. and 414 rd. is # rd.;

Number of lots on the length $=\frac{2011}{44}=44$;

breadth= 413 == 0

Total number of lots=44×9=206.

EXERCISE CLXXVI. PAGE 113.

```
2. Part A does in 1 de. - of work:
    ... " A .... 2 de. ... ... ...
        11 2 10 10
    15 M B 16 M 1 2 B day
       " A and B do in 2 da .= (1+1) of work = 1 of work;
             Work to be done=(1-1) of work=1 of work.
               Part A and B do in 1 da .= (i+i) of work
  .10.
                                     = of work:
                    Part yet to be done=(1-1) of work
                                     =H of work;
     Part of work A, B and C do in 1 da = (1+1+1) of work
                                     =Ak of work:
   Time for A, B and C to do Al of work=1 da.:
                    14.34 1 3 4/2 = W da. :
                                  =(\frac{1}{4}\times\frac{1}{4}\times) da.=1\frac{1}{4}\times da.
  11. Part A and B do in 1 da .- de of work:
      " A " C " " =} "
      " 2 men of A's strength, 2 men of B's strength, and 2
           men of C's strength do in 1 day
                           =(+++++) of work;
      " A, B and C do in I da .- | of (1+++1), or 14 of work;
      C does in 1 da. m (Ab - 16), or We of work;
  Time for C to do ris of work=1 da :
  a com the off and
          C " 444 " =(360×1/2) da.=21/1/ da.
 13. Time for 5 men to do the works:20 hr.;
   .. " 1 man " =100 hr.:
        part 1 " does in 1 hr. = ris of work:
Similarly, " 1 woman " "
                                = 141
1 boy 46 . 16
Hence, part I man, 2 women, and 3 boys do in 1 hr.
```

=(18+18+18) of work;

Time to do yis of work=1 hre;

" ## ## =(200×\$) hr.=28\$ hr.

EXERCISE CXCVII. PAGE 125.

| "£.790635 | .790025 of £1=.790025 of 20s. |
|--------------|--|
| a. 15.812500 | =15.8125 a. |
| 12 | .8125 of 1s.=.8125 of .2 d.
=9.75 d.; |
| d. 9.750000 | .75 of 1d.=.75 of 4 gr. |
| gr. 8.00000 | =2 qr.; |

EXERCISE CXCVIII. PAGE 125.

| | TAGE 120. |
|-----------|--|
| 1 12)6 d. | 6d.=fys. =.5e.; |
| 20)10.50. | 180,06. |
| - | 10s. 6d.=10.5s.; |
| £1.525. | $10.54. = \mathcal{L}\frac{10.5}{20} = \mathcal{L}.525;$ |
| 4 | 10 % _ 610.0 |
| | 20.00, -2 90 =2.000; |
| | Dance Otion on |
| | Hence, £1 10s. 6d.=£1.525. |

EXERCISE CC. PAGE 126.

9. Let 1 man get 1 share, then
1 youth gete .525 shares;
Shares of 6 mee and 11 youths=6×1 share+11×.525 share;
=11.775 shares=\$47.10;
... 1 share =\$47.10
-\$47.10
-\$44.10

EXERCISE CCI. PAGE 124.

3. Distance the stream flows in 60 min.=(2.5×5280) ft.

Onbie soment of stream 2640 ft. long, 125.125 ft. wide, and 4.8 ft. deep=(2640×125.125×4.8) cu. ft.=1585584 cu. ft.

EXERCISE CCIL. PAGE 127.

6. Expressing each of the numbers as ten-thousandths, we must find the G.C.M. of 22500, 38750, and 28125 ten-thousandths.

| 5) | 22500, | 23750, | 28126 |
|----|--------|--------|-------|
| | 4500, | 6750, | 5625 |
| 5) | 900, | 1850, | 1125 |
| 5) | 180, | 270, | 225 |
| 9) | 36, | 54, | 45 |
| | - da - | . 6. | . 5 |

Hence, the G.C.M. is (5×5×5×5×9) ten-thousandthe, or .5625. The L.C.M. is found in a similar way.

EXERCISE COM. PAGE 128.

11. Let C receive 1 share:

then B receives 1.75 shares :-

[1.5×(1+1.75)] shares, or 4.125 shares;

(1+1.75+4.125) " or 6.875 44

.1. 6.875 shaream \$202.50:

303.50 6.875 =644 =C's share:

1.75 of 844=\$77 =B's

1.5 of \$(44+77)=\$181;50mA's

23. Cable contents of first stick=(32.5×2.5×1.126) c. ft.; " = (21.75×1.875×1.25) e. ft.;

Weight of (\$2.5×2.5×1.125) e.ft;=-1387.5 lb.;

1 e. ft. = 4987.5 fb.;

21.75×1.875×1.25×4387.5 " (21.75×1.875×1.25) c.ft.:

32.5×2.5×1.125

=9446.875 Ib.

EXERCISE COXI. PAGE 132.

At of 250 a. = 52.5 a. :

All of 350 a. = 87.5 a. :

Afr of 360 a. == 210 a. :

Cost of 52.5 a. @ \$28=\$1470.00;

. . . 87.5 a. @ 425== \$0002.50;

210 a. @ 040==68400.00: Total cout 413982.50.

7. Selling price of 1st piano=| if of \$250 == \$325;

2nd " = | 18 of \$250 = \$350;

3rd " = ff of \$250 =\$200;

Selling price of all=0875.

Net gain=4(875-750)=4125.

9. Sum deposited = if of fortune;

" withdrawn = 18 of (18 of forence);

remaining = 100 of the of fortune its of fortune; 100, A of fortune=05760;

" == 16 of \$6760==\$8000

EXERCISE CCXIV. PAGE 138.

and second " $=\frac{107\frac{1}{2}}{100}$ of 1880=2021.

First remainder=# of \$875; Second " = 16 of \$875=\$270.

d. Part of marked price remaining after deducting the discount is 1th of marked price.

House, We of marked price=\$2.72;

" =\\ of \$2.79=\$8.20.

D. Part of price remaining after first discount

=
$$7\%$$
 of eat. price;
second discount
= 7% of 7% of eat. price;
= $\frac{67.5}{100}$ of eat. price;
Hence, single discount = $\left(\frac{100}{100} - \frac{67.5}{100}\right)$ of eat. price
= $\frac{32.5}{100}$ cf eat, price
= 32.5% .

EXERCISE CCXV. PAGE 136.

- Selling price—its of marked price;
 But " "=\fit of \$0;
 ... its of marked price—\fit of \$2;
 ... " =\fit of \fit of \$2.29.
- 6. Gain=At of cost=\$1.40; ... "=\frac{1.40}{25} of \$1.40=\$5.60; Selling price to gain 25%=\frac{13}{25} of \$5.60=\$7.56.

EXERCISE CCXVII. PAGE 137.

- 6. Loss=18* of cost=\$55.50; .'. '' = 18* of \$55.50 =\$2775; .'. Selling price=\$(2775-55.50)=\$2719.50.
- 9. Lose on 1 bu.= 10 of 72e.= 10e.;

 Quantity on which the is loss=1 bu.;

 10. "= 129600×5 bu.= 2000 bu.

EXERCISE CCXVIII. PAGE 137.

- 5. 115 of cost of 10 cows=9690;

 '' 1 cow = 10 of 115 of 9690;

 Belling price to gain 25%=155 of 15 of 115 of 9690=975.
- Buying price— No of market price;

 Solling "=\fit ""

 Sain on No of market price— No of fee of market price;

 1 = 100 × 100 × 50

 85 × 100

 35 //;

 Gain per cent. = 35 //.

Or, if the market price is \$100, the buying price is \$85 and the selling price is \$115;

** gain on \$65=\$30;

** \$100=\$\frac{100 \times 30}{85} = \$25\frac{1}{17}\$

** gain=35\frac{1}{17}\$

EXERCISE COXEX. PAGE 138.

reds bought-(6×50×30) m.; 66 . 66 =(6×50×30×35)0.;

== (18; of 6×50×30×25)e.=\$13.59

III en \$15756-

EXERCISE CONG. PAGE 130.

s. Sum received for the goods=(500×21×28)e.=49415; Commission=\$(\$415-1834.50)=\$00.50;

Commission on 89415-880.50:

.". rate=31%. .

Commission=18, of sum received; Suin sont to owner 15 " rife of sum received \$6064;

Agent's commission-the of \$7200-\$216.

EXERCISE CCXXI. PAGE 18

If sum invested==\$100

6102; . sum invested out of \$102 mg100;

Quantity bought for 34e.=1 lb.;

3000000.=
$$\frac{2000000\times3}{10^{-11}}$$
 lb.=60000 lb.

Sum collected: If of \$1260 == 4045; Commission=yty of \$045 im\$47.25; Jum received by creditor=\$(945-47.25)=\$607.75.

Auctioneer's commission=150 of value of goods; Sum remaining the " "

Com. at 4% on \$8500=\$140;
... sum remaining after the austicement took out his first commission =\$3040;

EXERCISE CCXXII. PAGE 140.

5. Dam insured—† of \$87500—\$30048; Premium on \$80048—\$303.93;

EXERCISE CCXXIII. PAGE 141.

4. vir of sum insured = \$67.50;

Sums received-\$14000.

6. Premium received==z5v of \$25000--\$262.50; Loss by company==\$(25000--262.50)==\$24737.50.

10. \$65000 | \$25000 | \$40000 | \$10000 | \$2500; Linkility of later | | \$10000 | \$2500; '' 2nd= | | \$10000 | \$2500;

" " 3rd-10006 of \$10000-\$6000.

EXERCISE CCXXV. PAGE 143.

3. Tax= $\frac{3\frac{1}{4}}{1000}$ of value of property;

6. Bum remaining after deducting cost of collecting

EXERCISE CCXXIX. PAGE 148.

Time for which the interest is yest principal=1 yr.;

-4ª TT. 1 #4 == 180 of 440 yr. -11 yr.

EXERCISE CCXXXII. PAGE 146.

20. Principal=88000

Interest 1st half yr.=\$ 400

Amount-88400

Interest 2nd half yr.=# 430

Amount-08820

Interest 3rd half yb. 441

Amount=#40361

Interest 4th half yr. == \$ 463.05

19724.05

19000,00

Compound interest=\$1734.06

Simple =2×16×0000=01000:

The compound interest is greater by \$(1734.05-1600), or \$194.05.

EXERCISE COXXXIII. PAGE 148.

Pass of draft=\$750 The of \$750-\$ 1.875 Cost of draft-\$751.875,

6. \$101 will purchase a draft for \$100;

66 . 66. 1500×100 . 81500 , or for \$1485.1485.

EXERCISE CCXXXIV. PAGE 148.

3 mo. from April 17 is July 17; 1.

Add 8 days of grace; " 20mdate of maturity;

No. of days between May 1 and July 20 is 80 mterm of discount; Interest on \$657 for 80 days at 8 % = reft of yeur of \$657

=811.58;

Proceeds of note=\$(657-11.52)=\$645.48.

- 7. Bank discount—} of you of face value—it of face value;

 Not proceeds—## of face value —#318.50;

 .'. face value—## of #318.50—#325.
- 9. The note falls due on Nov. 29. No. of days from Aug. 26 to Nov. 28=05; Interest on \$1962.45 for 95 da. @ 7%=\$25.75...; Proceeds=\$1963.46-\$25.75=\$1926.70.
- 10. The note falls due on July 21.

 No. of days from May 8 to July 21=74;

 "Interest on \$1006.74 for 74 do. @ 6%=\$12.97...;

 Proceeds of note=\$1006.74-\$12.97=\$1063.77.

EXERCISE CCXXXV. PAGE 150.

- 8. No. of dollars of stock in 75 shares—\$(75×50) —\$2750; Value of \$100 stock—\$200; .'. " \$2750 " —\$100 of \$200—\$9750.

EXERCISE CCXXXVI. PAGE 180.

- 1. \$84 money will buy \$100 stock; \$668 " " \\A ef \$100 stock, or \$700 stock.
- 7. \$200 money will buy \$100 stock; \$5200 " " ** *** of \$100 stock, or \$2000 stock. Now \$200 stock=1 share; ... \$2000 " = ***** of 1 share=10 shares.

EXERCISE CCXXXVII. PAGE 180.

- 1. Income from investing \$136=5;
 ... ** ** \$5300=\$120 of \$5=\$300.
- 6. Income from investing \$125=\$7;
 ... ** *** \$100=\frac{125}{125} of \$7=\$6\frac{2}{5};
 ... rate=5\frac{2}{5}.

EXERCISE CCXXXVIII. PAGE 151.

1. Sum invested to produce 45 !neome==\$130;

6. \$13 income is obtained from \$150 stocks

. . . . " 40° of \$100 !

Now, 850 stock=1 share;

.'. 00000 " malgie of 1 sharem

DIERCISE COUCUR, PAGE 1

J. The of stock-01200;

" miffor \$1200-\$12000; No. of shares-1990-720,

9. Amount of stocks-for of \$500-\$5000;

Value of \$100 " = \$006;

" =- YHY × 100)

EXERCISE CCXL. PAGE 183.

9. Income from \$126--- (5)

\$1-\$1\$1-\$.64; 6115 ·

Honor, the first is the better invests

A's income will of \$600

of B's stock=9400;

" = 100 of \$400 =\$6400.

EXERCISE CCXLII. PAGE 183.

1. (a) 100×2- 200 300×4=1300

900×7=1400

: 400×8==3200

1000 16000

The interest on \$100 for 2 mo. equals the interest on \$200 for 1 me. The interest on \$300 for 4 mo. equals the interest on \$1200 for 1 mo., ote.

Equated timews mo.

Hence, the interest on \$1000 for the equated time equals the interest on \$6000 for 1 mo.

The principle upon which this solution depends is, that the interest of the money, the payment of which is delayed beyond the time it is due, is equal to the interest of that which is paid be-. fore it becomes due.

2. The debt is due in 90 days.

1000 is paid 30 days before it is due.

Hones, the remaining 6000 should be retained for 30 days after the dobt is due, or should be paid in 130 days.

7. \$x0=0 \$x4=1 \$x6=9 1 |94

Equated timeway mo.

EXERCISE COXLIN. PAGE 164.

EXERCIBE CCXLIV. PAGE 188.

3. 25×5=125
The cent of pastering 35 cover for 5 mo. is
25×3=105.
the cent of pastering 35 cover for 5 mo. is
the cent of 125 cover for 1 mo., etc.
The rent should be paid in proportion to
125, 105, and 270.

A's there of sent=100 of \$100-\$25;

B's " "=100 of \$100-\$21;
C's " "=100 of \$100-\$24.

5. 4000×12=40000 3000×10=30000 5000×12=60000 3000×9=18000 150000

A's share— 1990 of \$1200—\$000. B's " = 1990 of \$1200—\$000.

7. 18500×12=120000 7500×12== 90000 18500× 8==100000 21500 224000 A's share-18888 of \$0150-\$1225; B's " = #### of \$6180-\$675; " -141919 of \$0100-\$1000.

#, \$150 × 19-27000.

The product of B's capital and his time must be A's, or 27000.

D's time=WWF-st.

Hence, B joined A 4 me, before the end of the year.

16. The partnership was formed on April 1, 1906,

4500×15-07500] 1600× 7=10000

5500×10-66

4000× 5-200

2000 X 12 m 30 5000× 3=15000

C's sharem MANA of 04

EXENCISE COL. PAGE 1/

6. Area of field=(122.5×100) eq. redu=(1225×16) eq. reds, Hence, 4× (No. of vaite of width) ==1925×10] (No. of units of width) =1225×4; No. of units of width=1/1225×4=25×2=70; .", length=4×70 rd,=200 rd.

EXERCISE COLIL PAGE 100

14.

Width-width: Reight-f width:

Longth-f width:

1×1×1 (No. of units of width) == 13824:

No. of units of widther \$ 18694-24;

.'. width=34 ft; and length-f of 24 ft.-26 ft.

EXERCISE CCLIII. PAGE 162.

8. Longth of plot including walk=(75+8) ft.;

" = (00+8) ft.; ## Width

" =(83)(66) sq. ft.=5646 sq. ft.;

Area of plos- (75×60) eq. ft.=4500 eq. ft. ; .'. area of walk= (5006-4500 eq. ft. =1144 m. ft.

EXERCISE COLV. PAGE 163.

4. Ofrequence of larger wheel=(\$\psi\$\times 43) in.=133 in.; " " maller " =(4×25) in.=110 in.

ee gained in 1 revolution=22 in.; " 1000 - " == == == == == 10000 in. 1

12)22000 in. 1 8)1888 ft.-4 in.1 84) 611 yd, -0 ft. 1

> 111 rd. -- 1 rd. : 111 rd. i yd. 0 ft. 4 in.=111 rd. 1 ft. 10 in.

EXERCISE CCLVL PAGE 184.

8; Area of circle=(3.85×160) eq. rd.=616 eq. rd.; .. 4×2 = 616:

.'. r =16, and diameter=30 rd.

.'. eireumference=(4×28) rd. =88 rd.

9. Area of larger circles: (4º×18°) aq. in.; smaller " =(4×17°) sq. in.;

... difference of area =(4×36×1) ag, in.=110 aq. in.

EXERCISE CCLXIL PAGE 107.

A. Longth of side of let square-14s in. -187 in: " 2nd " mafa in. m84 int

Sum of areas=(187°+04°) og. in.

=42005 eq. in.;

filde of square 1/ 42025 in. ==205 in; Perimeter= (4×205) in.=830 in.

Area of one fold=(945×1844) sq. yd.; 945 × 1344 Shorter side of others yd.=1190 yd. 1124

EXERCISE CCLXIII. PAGE 108.

10. 260 + 440 + 750 770;

Area of triangle= / (770×420×230×20) sq. yd. =46200 sq. yd.=-\ffa.

Now, rest of 44 a. = 001.50:

" " 1 a. = // of 651.50-48.30.

EXERCISE CCLXIV. PAGE 100.

S. The quantity of water passing through the pipes is in pro-

The areas are proportional to the squares of the measures of their like dimensions.

House, the areas of the pipes are proportional to 0, 9, 16.

The two whose areas are proportional to 0 and 0 are equivalent to one whose area is equivalent to 15.

Honor, the two pipes would carry more than the single one.

d. Bailing of pend and walk=30 ft.;

Area of " " =(4×301) sq. ft.;

10. Length of elreumference-\VXdiamotor;

.'. difference between cir.und diam.=\x "

.. 4×diameter=45 in.;

. diameter f of 45 in. - 21 in.

Area of circlem[4*×(4*)*] eq. in: =246; eq. in.

EXERCIBE COLXV. PAGE 180.

 Draw the figure and it will be at once seen that B E C and A E D are similar triangles and have the sides about the angles E B C and E A D proportional.

House, 40 : 16+A B :: 22 : A B;

... 40×A H=16×80+83×A E;

.. 8XA B-16X82:

A Books

Longth of B E=(64+16) A .- or A.

Again, 46 : 18+D B :: 38 : D E.

.. 40×D B-18×89+83×D E;

.. 8XD B-18X83;

... D E=72;

Longth of E 0=(72+18) ft.=90 ft.

7. Draw the figure.

The following will be apparent:

Distance from end of shorter side to perpendicular=26 ft.;

langer " " == 33 ft.

(Shorter side+3)*-35*=(shorter side)*-35*; ... 6×shorter side=32*-35*-3*; ... shorter side=45+3 =65; Longer side=65+3 =68; Perpendicular=y'(05*-35*)=60.

EXERCISE CCLXVI. PAGE 176.

1. Since 4× (radius) == 346400

Longth of standing part=/(287°-290°) ft.=63 ft.

6. Area of field=(5×100) eq. rd.=000 eq. rd.; Sum of longth and broadth=00 rd.;

Resolve 200 into factors whose sum shall be 60. These are evidently 40 and 20.

Longth=40 rd.; breadth=20 rd.

8. 64 gal.=1 c. ft.;

.... 4500 gal.= 4500 of 1 e. ft.=730 e. ft.;

Area of equare tank=\(\frac{230}{144}\) ft. =144 eq. ft.;
Length of side=(1/144) ft. =12 ft.

10. Area to be painted— 120×60 eq. ft.— 120×60 eq. yd.;

Cost of painting $\frac{120\times60}{9\times2}\times80$. =632.

EXERCISE CCLXVIII. PAGE 171.

7. Cubical content of platers (2×4×4×4) e. in.
Cubical content of each shots: (£×4×16×16×16×16) e. in.

No. of shot= 3×4×4×4 1×4×16×16×160×160

Area of Iron in the end of cylinder—(\$\times \psi \times 6^0) e. in.;

=(\$\psi \times 12 \times 6^0) eq. in.;

=(\$\psi \times 12 \times 2) eq. in.;

Longth of cylinder— \$\frac{4\times 4\times 6\times 6\t

10. The subical content of spheres vary as the cubes of their like dimensions.

Hence, the weight of the smaller sphere would be 1/4 of 78 on., if they were composed of the same material.

Actual weight of smaller sphero-| | of 14 of 75 oz. - 48 oc.

EXERCISE CCLXXVII. PAGE 179.

S. He vulgar fraction in its lowest terms can be expressed as an exact decimal unless it can be transformed to one which has 10 or rame power of 10, for its denominator.

Now, no number can by multiplication be made a power of 10 unless it is composed of factors each of which is 2 or 5.

Thus, 4 can be made into a power of 10 by multiplying it by

125 can be made into a power of 10 by multiplying it by 2×

40 can be made into a power of 10 by multiplying it by 5×5.

Such numbers as 6, 11, 12, 9, 44, 7 cannot be made into powers of 10 by multiplication, and hence \$, \$\delta\$, \$\delta\$ cannot be reduced to exact decimals and hence will form repeating decimals.

EXERCISE CCLXXVIII. PAGE 179.

- 1. See Exercise CCLXXVII.
- 2. 11 11 ... 11
- 3. When a valgar fraction in its lowest terms is reduced to an exact decimal, the number of figures in the desimal part is expressed by the greatest number of times that either the factors 2 or 5 coours in the denominator.

- d. See Exercise CULXXVII.
- 5. 6=2×3, here there will be 1 figure in the non-repeating part; 18=2×3×3, here there will be 1 figure in the non-repeating part;

20-23:5×8, here there will be I figure in the non-repeating

26-2×2×2×3, here there will be 3 figures in the nexrepeating part;

\$6-2×2×2×2×2×3, here there will be 5 figures in the non-

The number of figures in the non-repeating part is determined in the same way as the number of figures in an exact decimal, viz., by the number of times the factors 2 or 5 course in the denominator.

#. 7.45049—7.450—.00048; 7.457—7.45049—.00062;

Honor, 7.45646 is more meanly represented by 7.456.

9. Since .0915 is represented by 1;

EXERCISE COLXXIX. PAGE 179.

f. Elder son's share—fif of property=if of property;
Sum remaining—if of property;

.'. younger son's shares—if of if of property;
'. difference between the shares—(if—if of if) of property;

=(if×if) of property;

... ## of property=#\$1900;

.'. proporty-188 of \$1980-\$7200;

.'. elder son's share--- of \$7200 =60780.

2. Area of surface of water-(65%×48%) sq. ft.; Cubical content of 3 ft. in depth-(8×63%×48%) c. ft.=9215 c. ft.

J. 14-24-15-611;

Share of $A = \frac{1\frac{1}{3}}{6\frac{1}{13}}$ of \$654.50=\$132;

" D= 21 of 1651.50-1967.50;

" C= 35 of \$651.50-\$275.

4. \$ of \$ of monoy=010; " = \$ of \$ of \$10=\$100.

```
#. 18+8+#A=9H;
                         211×4+49=11×4×11=.0010130.
                                                             .4. is-11.
                       Bonninder of journeys of distance;
                                          · . . . .
                                                                                                             com(15×8) ml.:
                                                                 " =(4 of $ of 3) mi.=88 mi.
                                                                     Area of field-(73.9×160) og. rd.;
                                                             Longth of sidemy (72.9×100) of.=100 rd.;
                            Distance to be walked-4×100 rd.;
     Time to walk (8)×300) stimi hr.;
     ... at 41 (4×100) rd. = 4×100 hr. = .005 hr.
                S. Lot him buy 2 lb., 2 lb., and 3 lb., respectively.
                                Cost pulse=(1×20+3×201+8×201)s.=200je.;
                     Solling prico=[(1+3+8)×40]e.
           Gain on 2005c.—(240—2005)c.
                                                                                        100
2066 of 30je,=16/je.;
                                          .. gain=164.5.
                                today of miles.
                           100-100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 10
                                                                                                                                   LAURE PAGE 1866
                                                                                                                                                                -1-f ment-if men
                                                                the decrease of the Benefit of the state of 
                                              A door's weeks in I do.:
                                            B # 3 # # 1 104
                                     A. B. and Can 9 40 41 1 da.s.
... A. B, and Cdot " 44 & do.
        S. Part A. B. and C do in I da. - f work;
                                        Acad B " " " (++1) weeks;
                                                                    Past C does " =(1-1) " =1 "
                                                  me for C-to do A work=1 do.;
```

MILETTONS. Or, L.C.M. of 4), If and 11 is 80. A, B, and C do the week 72 times in 90 da.; A done " '20 " 10 de-1 1. 16 . 11 . 25 . 11 . 20 da. 1 .. 0 " " 27 " 90 da.; 4. Since A's working power is & of B's; .', A will require I of B's time to do the same week Time for B=124 da.; .. " " A=f of 12f da.=14.7 da.

5. If B takes 7 days to do the work, .. B does of the work in 1 day and A " | " " 1 day; and A " it " 1 day; .'. A's working power is it of B's working power, as Ale 11 11 is fof B's

6. Past which A and B do in 1 day= to of work; M's part of this is I share; Afg 44 44 2 charce; .'. 3 chance of week;
.'. 1 " " = j of it of works of works B's part; " =A of week=A's part. B does of weak in I day, ... the whole work in 54 days; A " # " 1 day, .. " 27 "

7. Time for A, B and C together to do the works of 21 da.

Part of week which A, B and C do in 1 day= fs work; If C does I share of this;

BHARRA

Hence, 7 times C's work in 1 day=A work; On the 1 of mit of A work

Hence, C would do the whole work in 122 da., or 391 da.

As A door twice as much each day as C;
A will require † of 20† days, or 19† da.
As B door four times as much each day as C;
B will require † of 20† days, or 9† da.

Time to begin work=(12-7) days, or 4) days from the com-

s. Part which A does in 12 days-if work;

11 11 B 11 6 11 = 1 11

" C " 4 " =(1-1f-fs) work=f work;
" C " 1 day =1 of f work=fs) work;

... time for C to de all the work=18 days.

10. Time for 1 man to de the work=75 hr.;

Part which I man does in I hr. -/ weeks

the matter & boy to the land of the

.'. part which 3 men and 45 boys do in 1 hr.=(4-44) week

.'. time for 8 men and 48 boys to do all the week- 4 hr.-4j hr.

11. Part of the work done by A, B and C in 1 daywer's work. The parts done by A, B and C are as 1, † and ‡, or as 6, 2 and 2.

Hence, part done by A in 1 days fr with works fr of week;

.', time for A to complete the week-4s da. = 30f da. :

Time for B '1 '1 '1 '1 =(3×30) da.=75) da;
'1 '1' C '1 '1 '1 =(3×30) da.=110 da.

28. Time for A to do the whole work= $\frac{1}{2}$ of 12 da.=13 da.; Fart of work done by B in $\frac{1}{2}$ da.= $\left(1-\frac{15i}{16}\right)$ of work

=-fs of work;
... " B in 1 da.=-f of ȳs of work;
=-fs of work;

.'. time for B to do all the work=15 da.

13. Part which A and B tagether do in 1 hr.=\(\frac{1}{2}\) of work;
\(\frac{1}{2}\) part which B alone does in 1 hr.=\(\frac{1}{2}\) of work;
\(=\frac{1}{2}\) of work;

.'. time for B to do all the west-44 hr. -22 hr.

Work done by A in † hr == of fr of work in 1 hr.;

Work done by A in † hr == of fr of work=fr of work;

Work done by A and B in 22† min.=fof (fr+f) of work;

Part of work to be dead by the three=(1-A-1)of work

15. Since 2 herecom3 mules;

.'. 6 horses and 5 mules—(0+5) mules; liew 7 tens are drawn by 14 mules; .'. 1 t. is 46 by 2 66

and Dit. is " by g "

Hones, 12 mules must work along with 7 mules to do the work; But 12 mules=(\$ of 12) houses=8 horses.

16. A, B and C do, respectively, it, it and it of work in 1 day. If each one had worked as long as C, they would do (1+i++ of it) of work, or (1+i+ib) of work.

Work done by A, B and C in 1 day-(rb+rb+rb) of work;

Time for A, B and C to do (1+1+10) of wark= 1+1+10 da.

17. A door of and B sh of work in 1 han;

Time to do the whole western 1 he, milt he.;

Or, A carms 210 71 c., or 25 fc. per hr.; B " 210 84 c., or 25 fc. per hr.; Time each works=[1+(A+A)] hr.=\{\frac{1}{4}} hr.; ... sum corned by A=(\frac{1}{4}\times20)c. ==\(\frac{1}{4}\times20\). ==\(\frac{1}{4}\times20\).

EXERCISE CCLXXXI. PAGE 181.

Norn,-In teaching clock problems the dial of a clock should be studied until it becomes close that the minute hand gains

55 minute-spaces in 60 minutes of time,

or, 11 minute-spaces are gained in 12 minutes of time,

er, 1 minute-space is " " 1 1 " "

Much oral drill should be given to accustom the pupil to recognize the position of the hands, i.e., to tell how many minute-spaces separate them.

2. 11 minute-spaces are gained in 12 min.;

... 16} " " " " 16 × 12 min., or 18 min.

3. At 3 the minute-hand is 15 minute-spaces behind the hour-hand.

Time to gain 11 minute-spaces-12 min.;

.. " " 15 " " $=\frac{15\times12}{11}$ min.=16A min.

Hence, the time is 164 min. past 3.

4. To be at right-angles the hands must be 15 minute-spaces apart. At 6 o'clock they are 30 minute-spaces apart. Honce, 15 minute-spaces must be eaught up by the minute hand.

Time to gain 11 minute-spaces-12 min.;

. " " 15 " " = 15×12 min.=16/4 min.

Hence, the time is 16A min. past 6.

5. At 6 e'clock the hands are 30 minute-spaces apart.

Time to gain 30 minute-spaces $\frac{30\times12}{11}$ min. =33 Å min.

Hence, the time is 32A min. page 6.

6. At 5 o'clock the hands are 25 minute-spaces apart.

To be 3 minute-spaces apart 22 minute-spaces must be mined.

Time to gain 22 minute-spaces $\frac{29 \times 13}{11}$ min. =24 min.

Hence, the time is 24 min. past 5.

7. At 6 c'clock the hands are 30 minute-spaces apart.

To be 8 minute-spaces spart either 22 or 38 minute-spaces must be gained.

Time to gala 22 minute-spaceous 22×12 min.=26 min.

" " 38 " " = MX19 min.=41 min.

Hence, the time is elizer 26 min. or 41 ft min. past 6.

8. In (a) 40 minute-spaces have to be gained.

Time to gain 40 minute-spaces $\frac{40\times12}{11}$ min. =43 $\frac{1}{11}$ min.

In (b) (40-15) minute-braces have to be gained.

Time to gain 25 minute-spaces $\frac{25 \times 12}{11}$ min. $=27 \frac{1}{11}$ min.

In (e) (40-20) minute-spaces have to be gained.

Time to gain 10 minute-spaces $\frac{10\times12}{11}$ min. =10\frac{1}{2} min.

9. At 9 the hands are 45 minute-spaces apart.

Time to gain 45 minute-spaces $\frac{45\times19}{11}$ min.=40 $\frac{1}{11}$ min.

At 10 the hands are 50 minute-spaces apart.

Time to gain 50 minute-spaces $\frac{50\times12}{11}$ min. =54% min.

At 11 the hands are 86 minute-spaces apart.

Time to gain 58 minute-spaces $\frac{55\times12}{11}$ min.=60 min.

16. If the hour-hand moves a certain distance, the minute-hand moves 12 times as far;

Honor, 1 distance +12 distances=25 minute-mass;

... 1 distance = {} = 0

Hence, the time is (25-214) min. part 5, or 23/4 min. past 5.

EXERCISE CCLXXXII. PAGE 182.

1. 48'= M of 60 minute-spaces=8 minute-spaces;

At 4 o'clock the hands are 20 minute-spaces apart;

Hence, (20-6) minute-spaces must be gained;

Time to gain 12 minute-spaces $\frac{12\times12}{11}$ min.=13 $\frac{1}{11}$ min.

#. 18°=-jih of 60 minute-spaces=3 minute-spaces;
To be 8 minute-spaces apart for the 2nd time after 2, (15+3)
minute-spaces must be gained.

Time to gain 18 minute-spaces $\frac{16\times19}{11}$ min. $=10\frac{1}{11}$ min.

8. If the hour-hand moves forward 1 distance from the figure 6, the minute-hand moves forward 13 distances from the figure 12.

Hence, 13 distances—1 distance=30 minute-spaces;

Hence, the minute-hand is $1\frac{1}{12}$ minute-spaces past the figure 6, The time will be $(30+1\frac{1}{12})$ or $31\frac{1}{12}$ min. past 6.

J. In 24 hours the clocks are 15 sec. apart; Time to be ‡ min. apart=24 hr.;

... " " 30 min. " =30×4×34 hr.=130 da.;

Time lest in 190 da. \$\pi\$120\times 0 00. \$\pi\$16 min. Hence, the time is 44 min. past 11. Time gained in 190 da. \$\pi\$120\times 7 000. \$\pi\$14 min. Hence, the time is 14 min. past 12.

. S. Time in which the clocks are 2 sec. apart=13 hr.;

.. " " " 10 11 200 " " = 200 × 15 hr. =75 da.

6 Time to lose 5 sec.=34 mia.;

... " " 17 min=17×00 of 24 min.=3 da. 9 hr. 26 min.;

3 da. 9 hr. 36 min. from 9 p.m. Monday is 36 min. past 6 a.m. on Friday.

7. From 12 o'clock to 5 o'clock are 200 min.; 200 min., on watch=0 hr. of true time:

.. 200 " " -\$\$\$ of 5 hr. of true time=5 hr. 5% min.

3. Time in which the clocks are 8 min, apart=12 be.

. " " =0; min, of 13 hr.

23 hr. from noon on Friday is 9 p. m. on Saturday. Time gained is 26 hr.—†‡×2 min=5‡ min.; Hence, the time is 5‡ min. past 9 p. m. Saturday. Time lest in 23 hr.—†‡×1 min.—2‡ min.; Hence, the time is 57‡ min. past 8 on Saturday.

A. From a quarter to 11 p. m. on May 2 to 0 a. m. on May 7 are 1655 hr.

Time to lose 9} min.=100} hr.;

16f hr. from a quarter to 11 p. m. on May 2 is 3 p. m. May 2.

19. From noon on Theoday till 10 p.m. Saturday are 106 hr. Now, 1443\$ min. on the watch=1440 min. true time;

Honor, the time is 9 hr. 43444 min.

EXERCISE CCLXXXIII. PAGE 182.

1. Distance gone in (00×60) sec.=(30×5300) ft.:

Distance gone in 1 sec.=80 ft.;
 Distance gone in (00×00) sec.=(00×00×80) ft.=34 fr mi.

8. Distance gone in 11 sec.=22 rd.; Distance gone in (00×00) sec.= $\frac{00\times00}{11}$ of 23 rd.=23\frac{1}{23} mi.

4. Time to move (30×1760) yd.=(00×60) sec.;

8. Time for eeach to go 2 mi. - A of 1 hr.;

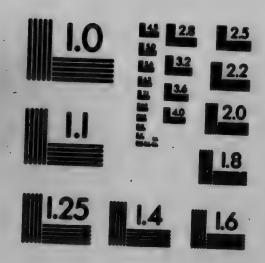
6. Time for A to gain | mi.=1 hr.;

7. A and B approach each other at the rate of (4½+8½) mi. per hr. Time to approach 8 mi.=1 hr.;

Distance A goes in 7t hr. = (7t×4t) mi.=32t mi.



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8. A runs 1760 yd. while B runs 1680 yd. and C, 1673; .". B runs 1680 yd. while C runs 1673 yd.; .. B " 1760 yd. " C " titt of 1673 yd., or 1752f yd.; Hence, B can beat C by (1760-1752#) yd., or 7# yd. in a mile. 9. A can run 1760 yd. while B can run 1788 yd.; 1760 yd. ·C 1749 yd.; .'. B 1738 yd. 1728 of 1749 yd. or, 172711 yd.; Hence, A can give C (1760-172711) yd. or, 3211 yd. start in a mile. 10. When the hands of a clock move correctly, they coincide every To coincide every 65 min. A min. must be gained. Gain in 65 min.= A min.; " 1440 min.=1440 of h min.=10148 min.

EXERCISE CCLXXXIV. PAGE 183.

1. Greater No. + Less No. = 365;
Greater No. - Less No. = 83;
... twice greater No. = 365 + 83 = 448;
... greater No. = 448 = 224;
and twice less No. = 365 - 83 = 282;
... less No. = 248 = 141.

Rate down stream=7 mi. per hr.;
 in still water=(7-11) mi. per hr.=51 mi. per hr.;
 up stream=(51-11) mi. " =4 mi. per hr.

Rate down stream per hr.=4 mi.;

"" =2 mi.

Rate in still water+rate of stream=4 mi. per hr.

"" =2 mi.

"" =2 mi.

"" =2 mi.

"" = mi. per hr.

4. Rate up stream per hr.=\frac{10}{2\frac{1}{2}}\text{mi.}=4 \text{ mi.};

"in still water " = (4+1\frac{1}{2}) \text{mi.} = 5\frac{1}{2} \text{ mi.}

"down stream " = (5\frac{1}{2}+1\frac{1}{2}) \text{mi.}=7 \text{mi.}

Time to row 7 \text{mi.}=1 \text{hr.}

"" 3\frac{1}{2}\text{mi.}=\frac{3\frac{1}{2}}{7}\text{of 1 hr.}=\frac{1}{2}\text{hr.}

Hence | the distance=1 mi.; .'. the distance=2 mi.

7. Rate in still water=4 mi. per hr.;

down stream=(4×11) mi. per hr.=51 mi. per hr.;

... rate of stream=(51-4) mi. per hr.=11 mi. per hr.;

... " up " = $(4-1\frac{1}{2})$ mi. per hr.=2\frac{1}{2} mi. per hr.

Time to return $1\frac{1}{2}$ mi. up stream= $\frac{1\frac{1}{2}}{2}$ hr.= $\frac{1}{2}$ hr.

1 mi. on the canal=1 hr.:

to starting place=(1+1) hr.= hr.

8. Rate per hr. up stream=2 mi.; down " =6 mi.:

Time to go 1 mi. up and back=(+++) hr.=+ hr.

Distance the man goes and returns in \$ hr.=1 mi.;

2 hr.= $\frac{2}{3}$ of 1 mi. =3 mi.

the distance 9. Rate down per hr.= the distance

the distance; .'. rate in still water+rate of stream=

and rate in still water-rate of stream= the distance;

```
.'. twice rate in still water 5 times the distance
                                                                                                                                                  5 times the distance
                                             Again, twice rate of stream the distance
                                                                                                       " .. _the distance
                    Hence, the rate in still water is to rate of stream as
       5 times the distance is to the distance, or as 5 to 1.
               10.
                                       Rate per hr. up stream
                                                                     " in still water=(21+11) mi.=4 mi.;
                                                                                    down stream=(4+11) mi. =51 mi.
               Time to row 5; mi. down stream=1 hr.;
                                                                                            a = \frac{12}{51} of 1 hr. =2\frac{1}{2} hr.
                                                            12 mi.
                                                        EXERCISE CCLXXXV. PAGE 184.
            1. Distance skated against the wind in 50 min.=6 mi.;
                                                                        " " " 60 " = ## of 6 mi.
                                                                                                                                                                    =71 mi.
                                 Rate of skating in calm+rate of wind=10 mi. per hr.;
                                                                                                 " _ " =7} mi. per hr.;
                                                                                         ... twice rate of wind=(10-71) mi. per hr.;
                                                                                                             ... " 10-71 mi. per hr.
                                                                                                                                                                    =1f mi. per hr.
            2. Sum of the rates in 5 sec.=(110+88) yd.;
                                               66 \times 60 = 60 \times
Difference of the rates in 45 sec.=(110+88) yd.;
                                                                                     per hr.=\frac{60\times60}{45} of 198 yd.=9 mi.
      Rate of faster+rate of slower=81 mi.;
                  " " =9 mi.;
                                . . twice rate of faster=90 mi.;
                                                 .. " =10 mi.=45 mi.;
             Again, twice rate of slower=(81-9) mi.;
                                                 ., " =14 mi,=36 mi,
```

3. Rate of first train per sec.=45 of 1 of 5280 ft.=44 ft.; Sum of rates of the trains per sec.=(44+40) ft.=28 yd.; Distance gone in 1 sec.=28 yd.

4. Rate per 4 sec.=88 yd.

Rate per hr. = \frac{60 \times 60}{4} \text{ of 88 yd.=45 mi.}

8. Distance the freight is ahead $=\frac{51}{60}$ of 38 mi.

Distance the express gains per hr.=19 mi.

Time to gain 19 mi.=1 hr.;

.'. time to gain 136 of 38 mi.=136 of 38 of 16 hr.=16 hr.

6. Distance the train goes in 10 sec. $=\frac{10\times30\times5280}{60\times60}$ ft. =440 ft.

" man " " $=\frac{10\times3\times5280}{60\times60}$ ft.=44 ft.

440 ft. is the sum of the length of the train and 44 ft.;

... length of the train=(440-44) ft.=396 ft.

Or, distance gained by the train in 1 hr.=27 mi.=(27×5280) ft.;

.. " " 10 sec. = $\frac{10 \times 27 \times 5280}{60 \times 60}$ ft. =396 ft.

7. Distance the train goes in 20 sec. $=\frac{20\times25\times1760}{60\times60}$ yd. $=\frac{2190}{50}$ yd.

yd. is the sum of the length of the bridge and the length of the train;

... length of the bridge=(2200-150) yd.=944 yd.

8. Distance the man goes in 10 sec. $=\frac{10\times4\times1760}{60\times60}$ yd. $=\frac{176}{60}$ yd.

Distance the train goes in 10 sec. = (88+174) yd.;

... " " 1 hr.= $\frac{60\times60}{10}$ of $(88+\frac{170}{10})$ yd. =22 mi.

9. Distance the man goes in 8 sec. $=\frac{8\times5\times1760}{60\times60}$ yd. $=\frac{110}{50}$ yd.;

Distance the train goes in 8 sec. = (110-174) yd.;

10. Distance the man goes in 15 sec. =
$$\frac{15 \times 4 \times 5280}{60 \times 60}$$
 ft.=83 ft.;

'' train '' 15 sec.=(352+88) ft. =440 ft.;

'' '' '' 9 sec.=\frac{1}{15}\$ of 440 ft. =264 ft.;

'' man '' 9 sec.=(852-264) ft. =88 ft.;

'' '' '' '' '' '' '' 1 hr.=\frac{60 \times 60}{9}\$ of 88 ft.=6\frac{1}{2}\$ mi.

11. Distance the train goes in 10 sec.=(88+44) yd.=132 yd.;

11.
$$\frac{60 \times 60 \times 132}{10}$$
 yd.=132 yd.;

12. Time for train to go 180 mi.= 144 hr.=61 hr.

EXERCISE CCLXXXVI. PAGE 185.

- 1. Length of the first piece=\frac{140}{140} yd.=36 yd.;

 Cost of 1 yd. of the second piece=\frac{4}{140}c. =\frac{1}{140}c.
- 8. No. in first bag = $\left(\frac{625-25}{2}+2\right)=325$; No. in third bag = $\frac{300-50}{2}$ = 125; No. in second bag=125+50 = 175.
- 3. Sum spent in 10 yr.= $$(6\times700+4\times500)=$6200;$... income for 1 yr.= $$^{6200}=$620.$
- 4. £288 4s. 11d.=276716 far.; £3 17s. 10\d.=3737 far.: 276716 far.\div 3737 far.=74 and 178 far. remaining; 178 far.=3s. 8\d.
- 8. 5e.+10e.+25e.=40e.; No. of each= $\frac{680}{40}$ e.=17.
- 6. No. is the G. C. M. of (365—20), (546—17) and (1140—13);
 G. C. M. of 345, 529 and 1127 is 23.
- 7. Share of B and C=£40 2s. 8d.

 '' A and C=£29 10s.;

 .'. shares of A, B and twice C's=£69 12s. 8d.;

 But, '' A, B and C =£53 6s. 8d.;

 .'. C's share=£16 6s.

```
Perimeter of field=2×(120+30) rd.=4950 ft.:
  No. of boards to go once round=4719=330:
.. " " 6 times " =6×330
                                                    =1980.
                               16×12=24;
  9. No. of furrows in 16 ft.=
    Time to plough 1 furrow=6 min.;
               11 24 11
                            =(24\times6) \text{ min.}=2 \text{ hr. } 24 \text{ min.}
 10. Value of ducks=(8×75)e. =600e.:
  Value of chickens=(13×50)e.=650e.:
                                  1250g.;
    No. of pounds bought for $1=16:
             64
                          $124=124\times16=200.
             EXERCISE CCLXXXVII. PAGE 185.
  1.
                           61 gal .= 1 e. ft. :
                       ... 500 gal. =\frac{500}{61} e. ft.
                                                   =80 e. ft.:
                      No. of e. ft.=(8\times6\times4) e. ft.=192 e. ft.
  Time for 80 c. ft. to enter eistern=60 min.:
                                    192×60 min.
         192 e. ft.
                                                   =144 \text{ min.}
             Share of boy =1 share:
                                 " +25e.;
                      woman=1
                66
                                   6.6
                      man
                             =1
                                      +50e.:
          Shares of 7 boys = 7 shares:
                    8 women = 8
                                    " +200e.;
                                    " +500e.;
                   10 men
                            =10
                                   " +700e.;
                               25
         ... 25 shares+700e.=2575e.;
                 ... 25 shares=(2575-700)e.=1875e.:
                  ... 1 share =\frac{1875}{16}e. =75e. =boy's share:
                1 share+25c.=$1.00
                                          =woman's share;
                1 " +50e.=$1.25
                                            =man's share;
  Money received by boys =7 \times 75e.
                                            =$5.25:
                     women =8 \times $1.00
                                            =$8.00;
                           =10 \times $1.25
                     men
                                            =$12.50.
  3. L.C.M. of 250e, and 175e,=1750e.:
  No. of barrels to cost 1750e. =\frac{1750}{480}e. =7.
  4. Dividend=7469 \times 728 + 19 = 5437451:
```

 $(5437451 \div 411) \div 5320 = 1022.$

8. Distance A runs further than B=25 yd.; but distance A runs 1 yd. "B=3 yd.; B=25×3) yd.=75 yd.

6. No. of hours for 30 men to do the work=240; "B=0×240; "B=0×240×10; "B=0×24

7. No. of miles= $\frac{7480\times12}{5280}$ =17.

8. Price paid for 1 a.=\$\frac{744}{144} = \frac{46}{15};

Sum received for 30 a.=30\times \frac{475}{1500} = \frac{42250}{1500};

45 a.=45\times \frac{4500}{1500};

Sum for which 45 a. must be sold=\$(7800+300-4500)=3600; Price for which 1 a. must be sold=\$\frac{242}{12}=\$30.

9. If all were sheep he would have received \$(250×8), or \$2000; Every time a pig is sold this sum is reduced by \$2. \$(2000—1720)=\$280.

To reduce \$2000 to \$1720 there must be *\frac{20}{4} pigs sold, or 140 pigs. Hence, there were (250—140) sheep, or 110 sheep.

10. Let cost of 1 vest =1 vest;

Then '' 1 cost =1 vest+\$1.25;

'' 4 vests=4 vests;

and '' 5 costs=5 vests+\$6.25;

cost of 4 vests and 5 costs=9 vests+\$6.25=\$33.25;

cost of 9 vests=\$27;

'' 1 vest =\$3;

'' 1 cost =\$4.25;

'' 12 costs=\$51.

EXERCISE CCLXXXVIII. PAGE 186.

1. Each time he paid \$4.50 he owed \$8.

No. of times he paid \$4.50=\frac{\$7200}{\$4.50} =1600;

... sum owed=\\$(1600 \times 8)=\\$12800.

Cost of 128 gal.=#(128×1.70) =#217.60;

Sum to be realized=#(217.60+33.40)=#251;

No. of gals. sold=251;

Quantity of water added=(251-128) gal.=123 gal.

```
8. Cost of 9 horses and 7 cows=$1200;

" 6 " " 13 " =$1200;

" 15 " " 14 " =$2400;

and " 18 " " 39 " =$3600;

" cost of 25 " =$1200;

" 1 cow =$48.
```

The cost of 9 horses=\$(1200-7×48)=\$864; ... " 1 horse =\$96; Cost of 3 horses and 8 cows=\$(3×96+8×48)=\$672.

=720.

No. of apples in second lot= (90×8)

6. Sum received for the tea= $60\times40\times3s$. 6d.=£420; Gain=£(420-280)=£140.

7. No. of eards in the pile=
$$\frac{60\times8\times8}{128}$$
;
Value of the wood= $\left(\frac{60\times8\times8}{128}\times3.25\right)$ =\$07.50.

8. 23 hr. 2 min. 36 sec.=82956 sec.;
46 hr. 8 min. 55 sec.=166135 sec.;
The G. C. M. of 82956 sec. and 166135 sec. is 223 sec.

Description of the property of the propert

10. No. of quarts raised=\(\frac{60 \times 240}{240} = 2880\)

"bushels "=\frac{241}{241} = 90.

Sam received for 90 bu. = 5040e.

. .. 1 bu.=488e.=56e.

EXERCISE CCLXXXIX. PAGE 187.

1. Area of room= $(18 \times 19 \times 162)$ sq. in.; Length of Carpet= $\frac{(18 \times 12 \times 162)}{27}$ in.= $\frac{18 \times 12 \times 162}{36 \times 27}$ yd.=36 yd. Cost of earpet= $(36 \times 75)e$.=227.

#. Length of rope=2×4 ft.+2×(3 ft. 2 in.)+4×(2 ft. 8 in.)
+1 ft. 6 in.;
=8 ft. +6 ft. 4 in.+10 ft. 8 in.+1 ft. 6 in.
=26 ft. 6 in.

3. Aggregate height of 6 boys=6×(4 ft. 5 in.)=26 ft. 6 in.

11 4 boys=4×(4 ft. 7 in.)=18 ft. 4 in.;

" 2 boys=8 ft. 2 in.;
... average of a boy=4 ft. 1 in.

4. 12 apples=10c.;
.'. 3 apples or 2 oranges=2 of 10c., or 23c.;
.'. 4 oranges or 5 lemons=2×23c., or 5c.;
.'. 15 lemons=3×5c., or 15c.

5. G.C.M. of 1080 ft. and 1375 ft.=11 ft.; Perimeter of field=(2×1089+2×1875) ft.=4928 ft. No. of rails to go 1 time round=4918=448.; " 6 times "=6×448=2688.

6. 212520=2×2×2×3×5×7×11×28.;
These arranged to make 4 consecutive numbers become, 2×2×5, 3×7, 2×11, 23.

7. L.C.M. of 3, 4 and 5=60:
... least number possible=60+2=62.;
62 is not a multiple of 7:

 $2\times60+2=122$. This is not a multiple of 7; $3\times60+2=182$. This is a multiple of 7;

.'. least number of marbles=182.

10. Cubic content of ear =
$$(33 \times 8 \times 6)$$
 e. ft.; bale= $(3 \times 2 \times 1 \frac{1}{7})$ e. ft.; No. of bales in ear= $\frac{33 \times 8 \times 6}{8 \times 2 \times 1 \frac{1}{7}}$ =176. Weight of 176 bales=26400 lb.; 1 bale = $\frac{24 + 82}{1}$ lb.=150 lb.

EXERCISE CCXC. PAGE 187.

1. As the farms are of equal size one farm must cost # of \$19500 and the other # of \$19500.

f of \$19500=\$7800, and f of \$19500=\$11700.

2. The L.C.M. of 10 ft. and 12 ft.=60 ft.

In going 60 ft. the front wheel turns 1 time more than the hind

Distance in which the front wheel turns 1 time more=60 ft.: 66 66 264 " " =(264×60) ft. 44 =3 mi.

No. of days idle to lose \$18.20
$$=$$
 $\frac{$18.20}{$1.40}$ =13.

No. of days he worked=
$$100-13$$
 =87.
4. Perimeter of lot= $(2\times120+2\times90)$ ft. =

=420 ft.:

Area of walk and lot=
$$[(120+9)\times(90+9)]$$
 sq. ft.=12771 sq. ft.;

No. of eq. yd.=
$$\frac{1830}{9\times4}$$
= $\frac{4}{19}$;
Weight= $(\frac{4}{19}\times8)$ lb.;
Cost= $8(\frac{613\times8}{12}\times\frac{4.90}{100})$ =\$20.0248.

- 6. Injured goods=i of i of goods=i of goods;
- ... value of & of uninjared goods=\$1680;

7. Interest on the principal for 4 yr.=\$(1339.30-1131)=\$206.80;

'' '' 5 yr.=\$ of \$206.30 =\$261;

Hence, the principal=\$(1131-261) =\$670.

The interest on \$670 for 5 yr.=\$261:

... " 100 " 1 yr.=
$$\frac{100 \times 261}{870 \times 5}$$
 =\$6;

Hence, the rate=6%.

9. 60 men are to do the work of 150 men for (40-34) da. Time for 150 men=6 da.;

... " " 60 " =
$$\frac{150 \times 6}{60}$$
 da.=15 da.;

Hence, the 60 men must begin work (34-15) da. after the commencement, or 19 da.

EXERCISE CCXCI. PAGE 188.

1. Use remaining after paying legacy duty= % of \$4600-\$4000; 2+3+4=9;

Share of first - f of \$4050-\$800;

" third -# of \$1650-\$1800.

No. of horses A No. of cattle;

H of " " =85;

... " = # of 85=60;

and " horses-A of 60-25.

If all had been horses the sost would have been $\$(60\times8)$ more than \$2560, or \$2000.

Hence, value of 85 horses=\$2060;

·· " 1 " -**ff*-+36.

5. No. of bushels of barley=### =63;

Value of 63 bu.=(63×46)e. =\$28.96.

No. of bushels of rys—4ff4 . =54; Value of 54 bu.=(54×55)e. =420.7

Value of 54 bu.=(54×55)e. =\$29.70. Farmer's gain=\$(29.70-28.98)=720.

4. No. of seres represented by 4 sq. in.=640:

... " (48×30) sq. in,= $\frac{48\times30\times640}{4}$

=23040.

δ. 10 a. 268 sq. rd.=1868 sq. rd.;

Area of field, 4 rd.×8 rd.==12 sq. rd.;

The first field is 1992 times as large as the second.

Hence, the length of the first field is 1191 times 4 rods; and the width " " 1191 " 3 rods;

6. Selling price=A of cost price:

. of cost price+50c.=188 of cost price;

.. 100 of cost price=50c.;

7. Length of wall= $\frac{8550}{10\times21}$ ft.=342 ft.;

By drawing the figure, it will be seen that $2 \times length + 2(length - 24 \text{ ft.} -5 \text{ ft.}) = 342 \text{ ft.}$:

```
.'. length +length-29 ft.=171 ft.:
                       \therefore 2 \times length = (171 + 29) ft. = 200 ft.
                        · · · length=
                                                =100 ft.
                       and breadth=(100-24) ft.=76 ft.
8. \frac{667}{100} (of father's money-$128.50)=$128.50;
... } of father's money-$85}=$128.50;
      .'. } of father's money=$214.16};
          .'. father's money= of $214.16
                                           =4321.25:
          or, f of remainder=$128.50;
              .'. remainder=$192.75:
          ... father's money=$(192.75+128.50)=$321.25.
9. Interest for 1 yr. 9 mo.@6%= of rest of note;
            .'. amount of note=### of note
                                             -- $391.17 :
                       .'. note=197 of $391.17 =$354.
10. Wages for 12 mo. = 8 sheep+$180;
           " 7 mo.=8 sheep+$80;
           " 5 mo.=$100;
           " 1 yr. =\ of $100=$240;
    Value of 8 sheep=$(240-180);
          of 1 sheep=$1-871.
            EXERCISE CCXCII. PAGE 189.
 1. In 1 day A and B earn 452c. or 66c.;
            A and C " 100c., or 70c.;
            B and C " ** or 76c.;
```

1. In 1 day A and B earn 41 c. or 66c.;

" A and C " 10 c., or 70c.;

" B and C " 41 c., or 76c.;

" A, B and C " 66+70+76 c., or 106c.;

" C earns (106-66)c., or 40c.;

" B " (106-70)c., or 36c.;

" A " (106-76)c., or 30c.

2. 5 of hare's leaps=2 of hounds;

but the hare takes 4 leaps while the hound takes 2;

- ... 1 hare's leap is gained every 2 leaps of the hound;
- ... 80 hare's leaps is gained every (80×2) leaps, or 160 leaps of the hound.
 - A's selling price=\(\frac{110}{150}\) of cost to A;
 B's '' '' =\(\frac{110}{150}\) of \(\frac{150}{150}\) of cost to A;
 \(\frac{110}{150}\) of \(\frac{150}{150}\) of \(\frac{130}{150}\) of \(\frac{130}{150}\).

4. The faster train gains (21-16) mi., or 5 mi. per hr. Time to gain (5×1760) yd.= (60×60) sec.:

.. " (184+135) yd.=
$$\frac{319\times60\times60}{5\times1760}$$
 sec.=130\(\frac{1}{2}\) sec.

8. Value of house=8}×value of lot;

.'. 8} value of lot+value of lot=\$4750;

6. Since 100 of cost=\$2771;

...
$$\frac{188}{188}$$
 of cost= $\frac{108}{18}$ of \$2771=\$332.80;
... cost of 1 bu.= $\frac{24448}{188}$ c. =80c.

7. Distance travelled=($\frac{28}{18}$ of 4×5280) ft.; Area cut=($2\frac{1}{11}\times4840\times9$) sq. ft.;

... width
$$\text{eut} = \frac{2.1 \times 4840 \times 9}{10.000} \text{ ft.} = 30 \text{ ft.}$$

8. Cost of sugar=\$(160+13) =\$173; Cost at 7e.=\$140:

Difference from actual cost=\$(173-140)=\$33;

Each pound bought at 10c. increases this price by (10-7)c., or 3c.

9. Divide the field in four square fields by dividing the length into 4 equal parts and drawing lines parallel to the ends through the points of section.

Then, area of each square field=15178 sq. yd.=3844 sq. yd.;

... width of the large field=
$$\sqrt{(3844)}$$
 yd. =62 yd.;
... length " = (4×62) yd. =248 yd.

10. L.C.M. of ‡ yd., 1 yd., 1½ yd. and 1½ yd.=15 yd.;

Length of each strip=1 yd. =20 vd.:

EXERCISE CCXCIII. PAGE 189.

1. Distance the train gains in 1 hr. =27 mi.;

" " 10 sec.=
$$\frac{10\times27\times5280}{60\times60}$$
 ft.=396 ft.;

Hence, length of train=396 ft.

#. The cf \$450=\$27;
Sum to be divided according to capital=\$(450-27)=\$423;

Capital=\$(4900+1400)=\$6300;

A's share=# of \$428 =\$329.

3. The successive multiples of the divisor are 1641, 1094, 1641 and 1641.

The G.C.M. of 1641, 1094, 1641 and 1641 is 547. Hence, the divisor is 547 and the quotient 3233.

4. The difference between a gain of 7% and a loss of 17% is

... oost=\$\frac{100\times 1}{24} = \$4\frac{1}{2}.

8. Cost of (25 cows+25 calves)=\$(427.75+308.50)=\$731.25; Cost of 25 calves=\$(25×5.75) =\$143.75; '' 25 cows =\$731.25-143.75) =\$587.50; ... '' '' 1 cow =\$\frac{587.50}{25} =\$23.50.

6. When B was supposed to win he ran 1760 yd. while A ran 1738 yd.;

Hence, A's rate is to B's as 1738 is to 1760; But 1760 represents f of B's actual rate;

... f of B's rate=1760; ... B's rate=1320.

Hence, A's rate is to B's as 1738 is to 1320, or as 79 to 60.

7. Number A and B can dig=68;

B and C ______ =62;

all together " =98;

L.C.M. of 36, 32, 30, 68, 66, 62 and 98-409036320.

8. Gain 100 of \$4860 \$1944:

Let what B gets=1 share;

Then A gets=2 shares;

and C gets=6 shares;

. 9 shares=\$1944;

.'. 1 share =\$ 216=B's share:

and 2 shares 432=A's

and 6 shares=\$1296=C's

Rate on the dollar=
$$\frac{86.26}{1150}$$
e.=716. =71%.

After paying the tax there remained 921% of income;

.. income =
$$\frac{100}{924}$$
 of \$1554 =\$1680.

EXERCISE CCXCIV. PAGE 190.

1. $2016=2\times2\times2\times2\times2\times3\times3\times7=2^{\circ}+2^{\circ}\times3^{\circ}\times7$:

... to become a perfect cube it must be multiplied by
$$2\times3\times7^2$$
, or by 294.

The cube root of $2^{\circ} \times 2^{\circ} \times 3^{\circ} \times 7^{\circ} = 2 \times 2 \times 3 \times 7 = 84$.

Hence, first sum is to second as 54 is to 45, or as 6 is to 5.

$$(\frac{112\frac{1}{2}}{100}, \frac{90}{100})$$
 of cost=\$45;

4.
$$\frac{(.201-.102)^{\circ}}{(.201)^{\circ}-(.102)^{\circ}} = \frac{(.201-.102)(.201-.102)}{(.201+.102)(.201-.102)} = \frac{.201-.102}{.201+.102} = \frac{.201-.102}{.201+.102} = \frac{.099}{.308} = \frac{.33}{101}.$$

Fair gain= 40 of cost;
Unfair gain=2 os. for every 14 os. sold
= of goods;

Sum realised for \dagger of goods \Rightarrow of \dagger of cost \Rightarrow of cost;

Total gain \Rightarrow of cost \Rightarrow 240;

.'. cost \Rightarrow 0 of \$240

6. Interest at 1% for the given time=\$(336-330)=\$6;
... 18% =16×\$6 =\$96;
... principal =\$(336-96) =\$240;
Interest on \$246 for 1 m at 0...

Interest on \$240 for 1 yr. at 8%=\$19.20; . Time for which \$19.20 is interest=1 yr.;

$$\frac{96}{19.20} \text{ of 1 yr.} = 5 \text{ yr.}$$

7. Cubic content of sphere $\frac{1}{3} \times 6^{3}$ c. in.;

Area of iron in end of cylinder= $\pi \left[(6\frac{1}{2})^2 - r^2 \right]$; Cubic content of cylinder= $8\pi \left[(6\frac{1}{2})^2 - r^2 \right]$;

Hence, radius of opening=# in.;
Thickness of iron=(6\frac{1}{2}) in.=4 in.

8. 2 hound's leaps=3 hare's leaps;

Now while the hound takes 2 leaps=4; hare's leaps;

Now while the hound takes 3 leaps the hare takes 4; Hence, ½ leap is gained each time the hound takes 3 leaps;

9. $8\frac{1}{10} + 5\frac{1}{10} = 13\frac{6}{10}$;

Time the fire is burning= $\frac{5\frac{1}{10}}{13\frac{6}{10}}$ of 24 hr.=9 hr.

10. Since the time is inversely proportioned to the rate and the supposed time is ‡ of the actual time;

... if the actual rate is 3 the supposed rate is 4, 1 more than the actual rate;

```
Now, 1 mi. per hr. slower would make the rate 2. L.C.M. of 3 and 2 is 6;
1 hr. is the difference in time to walk 6 mi.;
4 '' '' 24 mi.
```

EXERCISE CCXCV. PAGE 191.

```
1. ...Selling price per gal.=\frac{120}{150} of $3.20=$3.84.

After 20% has leaked away \frac{10}{100} of a gal. remains;

... selling price of \frac{150}{150} of gal.=$3.84;

... '' '' 1 gal. =\frac{100}{150} of $3.84=$4.80.

2. 1% of $2700=$27;

Interest on $(2275+2700) at lower rate=$(425-27);

... interest on $100 at lower rate=$\frac{100 \times 396}{4975} =$8;

... lower rate=8%;
```

... gain per cent. =
$$\frac{100 \times 10^{\frac{1}{4}}}{33}$$
 = $31\frac{9}{11}$.

$$\cdots \qquad = e^{\frac{500\times4\times44.07}{12\times3}}$$

No. of bu. at
$$80c. = \frac{500 \times 4 \times 4407}{80 \times 12 \times 3} = 3060 \text{ Å}$$
.

5. A received ## of the votes; B received ##;

$$24 \times 124 = 2976$$
. No. who did not vote=3200-2976=224.

No. who did not vote=3200—2976=

In 28×4 ft., one wheel turns 3 times more than the other.

Distance to turn 3 times more=88 ft.:

```
7. Time for 1 man to do the work=10 times the time;
             16 1
                         4.6
                                 " =7 times the time and 49 da.;
                             6.6
   ... 10 times the time
                             4.6
                                 " =7 times the time and 49 da.;
               44
                                 " =49 de.:
                             44
               66
   .'. 1 time
                         66
                             44"
                                 66
                                     =4 da.=16 da.
    Or, 7 men+3 men do 1 work in 1 time;
    .'. 7 men
                      do de work in I time:
    . 7 men
                      do & work in 7 days:
                      de 11 work in 7×10×7 da., or 16¢ da.
    .'. 10 man
   8. Area of part within the circumference of path
                                        =(4'×149°) sq. yd.;
                              noth
                                        =(44×145°) sq. yd.;
                            Area of path=\(\frac{4}{2}\times (149^2-145^2) sq. yd.
                                        =(44\times294\times4) sq. yd.;
                      Quantity of gravel=(4×4×294×4) c. yd.
                                       =821# c. vd.
   9. In 1 da. A does to of the work; B, tr; and C, tr.
      Work done by B in 1 da = (1 × 1) of work of work;
                   C " 2 da,=(2×13) of work = 15 of work;
   Hence, if B and C worked as long as A, they would do
                      (1++++) of work:
Time to do (\frac{1}{16} + \frac{1}{12} + \frac{1}{18}) of work=1 da.;
                                 1+1+4
          (1+1+4)
                                10+10+10 da. =5 da.
 10. Let D's share=1 share:
              " = | | share;
          C'a
               " = 114 of 124 share;
         B's
               " = 158 of 158 of 188 share;
  Hence, (1+188+188 of 188+188 of 188 of 188) share=$2699.16;
    or, 14886 share=$2699.16;
        .'. 1 share=12000 of $2699.16=$600
                                              =D's share;
                          188 of $600=$630 -C's
                          119 of $630=$603
                                              =B's
                          118 of $693=$776.16=A's
              EXERCISE CCXCVI. PAGE 192.
 1. Let quantity raised the second yr.=1 share;
   thon
                 44
                       4.6
                            first yr.=14 "
                             both vr.=## "
                                                    =3105 bn.:
                           ... 1 share=1f of 3105 bu. =1350 bu.;
    Quantity raised more the first yr.=100 of 1350 bu.=405 bu.
```

f. Area of walls=4152 sq. yd.=112 sq. yd.=1008 sq. ft.: Let height=1 height; breadth=14 "" length=2 perimeter=(4+3) heights=7 heights: Area of walls=[7×(No. of units of height)*] sq. ft. =1008 ag. ft.: .'. (No. of units of height) =144: No. of units of height=12. Hence, height=12 ft.; breadth=18 ft.; length=24 ft. 3. 621 lb.=1 cu. ft. of water: 7.112×62} lb.=1 eu. ft. of iron; ... 1 lb. = $\frac{7}{7.112 \times 62\frac{1}{4}}$ eu. ft. of iron; ... 2000 lb. = $\frac{2000}{7.112 \times 624}$ eu. ft of iron=4.5 eu. ft. nearly. 4. Sum received from \$5000 stock=\$600 of \$110=\$5500; \$7600 " = 100 of \$115=\$8740; Income from \$(5500+8740)=\$\frac{14240\times4\frac{1}{2}}{220}=\$720: Original income from \$5000 stock=\$250: \$7600 " =\$456: Gain in income=\$720-\$(250+456)=\$14. 5. Buying price per orange=fe.: Selling " " " = ie.: 4.6 =(1-1)e.=1e.;No. of oranges to gain Ac.=1; $1200e = \frac{1200 \times 20 \times 1}{2000} = 8000$ Value of 1 lb. gold=£46 14s. 6d.: Value of 18 lb. gold+18 lb. silver=£896 8s.; Value of 18 lb. gold=£841 ls.: ... value of 18 lb. silver=£55 7s.: .. " " 1 os. " =5ls. Value of 18 lb. of gold=£841 1s.; Value of 18 lb. of mixture=£637 7s.: £203 14s. Each pound of silver reduces the value by £46 14s. 6d.—£3 1s. 6d.

No. of pounds of silver=

No. of pounds of gold=18-41 =131.

£203 14s.

£43 13a.

```
7.
               He of I cost=#11 cost:
              He of the cost= ## cost;
      Aff of (1-f-A) cost=1118 cost:
               Selling price=1444 cost:
                       Gain=## cost=#217;
                    ... cost=#4000×217
              Time to row 30 mi. up=time to row 50 mi. down;
  .'. time to row 30 mi. up and back=time to row 80 mi. down;
             .'. rate of rowing down=ff mi. per hr.
                                   =6f mi, per hr.;
           Time to row 80 mi. down=time to row 18 mi. up;
.'. time to row 30 mi. down and back=time to row 48 mi. up;
               ... rate of rowing up=## mi. per hr.
                                   =4 mi. per hr.;
  Rate in still water+rate of stream=6f mi. per hr.;
              11 _ 11
                           " =4 mi. per hr.;
               ... 2 × rate of stream=2f mi. per hr.;
                    . ... " =1} mi. per hr.
 9. If the time past 3 p.m. is represented by 4;
 then " " 1 a. m. will be represented by 1;
 ... the time between 3 p.m. and 1 a.m. will be represented by 3;
 The time between 3 p.m. and 1 a.m. is 10 hr.
 If 3 represents 10 hr.;
 ... 1 will represent 3 hr. 20 mir
 Hence, the time is 3 hr. 20 min. pust 1 a.m., or 4 hr. 20 min. a.m.
10. Since the width is # of the length;
      ... t of area=1 of f a.
                                            = t a.;
        f a.- 1 a.=100 sq. rd.:
            Width=(\sqrt{100}) rd.
                                            =10 rd.:
```

EXER ISE CCXCVII. PAGE 193.

Area to be painted=[(20+24)×51×2] sq. yd.=484 sq. yd.;

=12 rd.:

=\$217.80.

Length=f of 10 rd.

 $Cost = (484 \times 45)e.$

```
#. Selling price of the hay=$(1000×20) =$20000;

.'. commission=$[20000-(18325+875)]=$800;

Commission on $20000-$800;

'' $100=$4;

.'. rate=45.
```

3. Wine remaining after the 1st drawing off=‡ of eask;

'' '' 3nd '' =‡ of ‡ of eask;

'' '' 3rd '' =† of ‡ of ‡ of eask;

'' '' 4th '' =‡ of ‡ of ‡ of eask

= 11x of eask.

6.
$$25.\dot{1}8\dot{5}\times13\frac{7}{47}=25\frac{7}{47}\times18\frac{7}{7}=\frac{30\times410}{37}$$

$$61.375\times5\frac{1}{47}=61\frac{1}{47}\times5\frac{1}{47}=\frac{491\times25}{37}$$

$$80\times410\quad 491\times25=\frac{1}{27}=\frac{1}{47}$$

$$=.67\dot{5}$$

6. 2 lb. of standard gold = 1860s.;
.'. 1 '' '' = 984.5s.;
.'. 1 '' pure '' = 12 of 984.5s. = 1714s.
1 lb. of standard silver=66s.;
.'. 1 '' pure '' = 12 of 66s. = 2210s.;
.'. 1 lb. of gold : 1 lb. of silver :: 1114 : 1112, or as 14.288 : 1.

7. $\frac{112\frac{1}{4}}{100}$ of cost price=45c.; ... '' = 40c.; Cost of 1500 lb.=(1500×40)c.=\$600; Selling price= $\frac{1}{12}$ of \$600 =\$720; Sum now realised=(360×45)c.=\$135; '' to be '' =\$(720-135) =\$685; Selling price per lb.= $\frac{1}{1}$

```
iff of i cost =iff of cost;
            iff of i cost -iff of cost:
            A of A costs Al of costs
.'. (188+188+196) of cost=$600;
       .'. eost of 260 yds. == | 118 of 8860;
       .'. cost of 1 yd. =ytu of 1888 of $500=$31.
  9. Length of side of square field= / (40×100) rd.=80 rd.;
          Perimeter of square field= (4×80) rd.
       Breadth of rectangular field-
       Perimeter of
                                  =3224 rd.:
     Difference in length of fences=2f rd.:
         " eost " = (2$×81)e.=$1.80.
  10. Income from $1000 in 3% stock=#30;
              " new investment =$40;
                 .'. The of new stock=$40;
                       · # " = #500.
           Sum invested in $500 " = No of $1000=$950:
         · · · · · ** $100 ** =$****$190;
               .. price of new stock=190.
             EXERCISE CCXCVIII. PAGE 193.
 1. 27 a. 48 sq. rd.=4368 sq. rd.;
 Taking A of 4368 sq rd. away will leave a field equal to a square;
    11 of 4368 sq rd .= 2704 sq. rd.;
  Side of square field= / 2704 rd.
       Width of field=52 rd.:
       Length
                " =# of 52 rd.
    Perimeter '' = (2 \times 84 + 2 \times 52) \text{ rd.} = 272 \text{ rd.}
     #. Cost of $18300 stock @ 75=$13725;
         Interest on $18725 @ 8%=$1006:
                     Total outlay=$14823;
 Income from $18300 stock @ 3%=$549:
                      Net outlay=$14274;
   Sum received for $18300 stock=$(14274-122);
         ... selling price of stock=14112=771.
```

3. It is evident that 10c., the difference between the two prices, must be divided into two parts proportional to 20c. and 30c.

Smaller part=f of 10e. =4e.;
Selling price=(20+4)e.=24c.

What cost (20-30)e. is sold for 48e.; .'. less on 50e =2e.; " " 100e,=4e.; .'. loss per cent.=4. . 4. Let height=number of units of height: Number of units of area in one side=406; * 66 - 66 Number of units of length= " of breadth= 406 × 312 312 .'. (height)* 884 .'. beight=12; Length=44-34; Breadth=W=26. 8. Time for the first to go 3 mi.=# hr. 12 mi.= =2# hr. : Time for him to complete the journey=(2++1) hr. =3 h hr.; Distance the second goes in 3 hr.=(3 ×34) mi.=104 mi.; has yet to go=(15-10‡) mi.=4‡ mi. 6 a.=(6×43560) eq. ft.; Quantity of ice=(6×43560×1) ou. ft.: Weight of 1 cu. ft. of water=1000 cs.; Weight of (6×48560×1) on, ft. of ice= 4 of 6×43560×1×1000 on, =36754 t. 7. 114 of 4 cost=48 cost; 188 of + " =+48 " 7th of \$4 " = 1888 " Sum received=(##+##+###) cost=### cost; Not gain- A cost =\$15.40; ... cost=\$ 630×15.40 =8441. 8. A's age : B's age :: 9 : 5;

.'. A's age= o.' B's age;

.'. A's age-23=1º of (B's age-23);

But A's age-23 : B's age-23 :: 10 : 3;

```
.". A's age=23+4 of (B's age=33);
.'. 23+4 of B's ago-4f-1 of B's ago;
   .'. (1-1) of B's age-761-23;
            .'. B's age-44 of 534-25:
           and A's ago-1 of 35 -61.
  9. Since the weight of 1728 cu. in. = (1215×5760) gr. :
  . 41 41 11 45
                         1
                             ** == 4050 gr.;
                            1 gr. = 56 sq. in.:
                       .'. 4050 gr.=(4050×56) sq in.;
               .". number of leaves 4050×56
 10.
             5 men= 15 boys and 9 men=27 boys;
           4 women=8 boys and 15 women=30 boys;
           ... 5 men, 4 women and 3 boys =26 boys;
          and 9 " 15 " " 18 " =75 ";
     Time for 26 boys to do: I work
                                       = 150 da. :
                     11' 1 11
                                         26×150
                                           75
                                        2×26×150
         46 78 44 44 9 46
                                            75
```

EXERCISE CCXCIX. PAGE 194.

=104 da.

- 1. Since † cir.+diam.=60 ft. and the cir.=\psi \times \diam.;
 ... † of \psi \diam.+\diam.=60 ft.;
 ... \diam.=\frac{1}{2} \of 60 ft.

 Area of semicircie=(† of \psi \times \psi \times \psi) eq. ft.

 =213\frac{1}{2} \text{ eq. ft.;
 ... No. of plante=213.
- ## A's selling price = 100 of cost;

 B's '' = 100 of 100 of cost;

 C's '' = 100 of 100 of 100 of cost;

 .'. 100 of 100 of 100 of 100 of 100 of 100 of 43786.75 = 44500.
 - S. Rate down stream per hr.=4† mi.+rate of stream;

 "up "=4† mi.-rate of stream;

 ". 4† mi.+rate of stream=8 (4† mi.-rate of stream);

 ". 4×rate of stream=9 mi.

 ". rate of stream=2† mi.

d. The quantity of each kind must be inversely proportional to the prices, i.e., to 48c. and 60c., or as 4 to 5;

7. Sum received by creditors
$$-\frac{62\frac{1}{3}}{100}$$
 of \$5000 -\$3125;

Weight of 1 eu. ft of iron=(7.492×62.5) lb.;
 Weight of 1 eu. ft. of cedar=20 lb.;

.'. iron weighs $\frac{20}{7.492 \times 68.5}$ of an equal bulk of eedar;

Thickness of cedar of a certain wt .= 9 in.;

10.

... " iron of same wt.
$$\pm \frac{20}{7.492 \times 62.5}$$
 of 9 in.=.384..in.

Difference in lengths=225 (
$$\sqrt{3}$$
-1) in. =164.7114..in.

```
B's capital=$(16000-1280)=$14720;
$(9200+14720+18000)=$41920;
A's share=$1555 of $4716 =$1025;
B's '' =$1555 of $4716 =$1656;
C's '' =$1555 of $4716 =$2025.
```

EXERCISE CCC. PAGE 195.

1. | 155 of cost=\$4.32; ... cost=| 155 of \$4.32=\$3\$; Wine at \$3 sold for \$3\$ gains \$\$, or \$\$\$; \$3\$ '\$3\$ loses \$\$\$;

To make the gain and loss equal 6 dos. at \$3 must be mixed with 15 dos. at \$3\$, or 2 doz. must be mixed with 5 dos.

2. By drawing the triangle it will be seen that the angle between the hands is 45°.

45°= 11 of 60 minute-spaces=71 minute-spaces. At 4 o'clock the hands are 20 minute-spaces apart.

To be 7‡ minute-spaces apart (20-7‡) or (20+7‡) minute-

Time to gain 12½ minute-spaces=(12½×½) min.=13½ min.;
" 27½ " =(27½×½) min.=30 min.

Supposed cost=10. "+\$13;

Supposed selling price=10. "+\$13;

... 166 of 100 of cost=10. "+\$13;

... (1-100) of cost=\$13:

4. A cost of 90 gives a width of 1 yd.;

6. Cost of 11 lb. @ 88c.=968c.;
Increased cost due to 4 lb. of better kind= 88c.;
... cost of 11 lb. of poorer ''=880c.;
... '' 1 lb. of '' ''=80c.;
... '' 1 lb. of better ''=(80+22)c.=102c.

6. The of cost of lst=\frac{10}{100} of cost of 2nd;
\text{... cost of lst=\frac{1}{4} of cost of 2nd;}

```
... t of cost of 2nd+cost of 2nd=$5850;
                                " =f of $6860=$2800;
                     and
                                lst={ of $2600=$3250.
           Sum of areas=(2321) aq. ft.+(231) aq. ft.;
                       = refffer og. ft.;
         Length of side= / 1272 ft .= 1777 ft .= 23311 ft.
    #. The L.C.M. of 1830 and 350=6650;
   Time for 175 men and 240 boys=1230;
                      · 48 · =6650;
                      44 1005
                              " = 350;
            444
                    *** 1984
                 **
                             ** =6650.
      Hence, 35 men and 48 boys=10 men and 1884 boys;
         .'. 665 men and 912 boys=603 men and 1005 boys;
                      .'. 62 men =93 boys;
                        or 2 men=3 boys.
   Hence a man's work : boy's work : : 3 : 2.
                    Area of room=49 sq. yd.;
       Cost of 49 sq. yd. of earpot=$(49×2.40)
                                                   =$117.60;
Artual cost of carpet and oil-cloth=$00.60;
Each yard of oil-cloth reduces the price by (240-96)c., or by 144c.;
                 Area of oil-cloth= 1700 sq. yd.
                                                  =184 sq. yd.;
                   Area of carpet=(49-182) aq. yd.=802 aq. yd.;
         Length of side of carpet=(1/301) yd.
               Width of oil-cloth=21-161 ft.
                                                  -21 ft.
 10.
                  A's profit for 6 mo. =$(1200-960)=$240;
                     12 mo.=$480;
. A's stock and profit at end of 12 mo. =$(960+480) =$1440.
     Stock to produce $1440 in 12 mo.=$980;
                      $2440 in 12 mo.=$\frac{2400 \times 960}{2400 \times 960}
                                          1440
                                     =$1600 = B's stock.
                            C's profit=$(1040-640)=$400.
          Time for $1600 to gain $800=12 mo.;
                                      1600×400×12 mo.
                                         640×800
                                    =15 mo.
```

EXERCISE CCCI. PAGE 196.

1. If the train passes 1 pole per minute the true speed per hr. 60×60 1760 mi.=2 mi.:

Approximate speed=2 mi.:

. error= de mi.

Now, in mi. is it of ## mi.

2. 50×1e.=25e.: 88-25e.=87.75:

Cost of 1 lb. of B's= The. =911a. : " A's=(911+1)e. =104e.;

A's share=(50×10 to)c.=\$5.00\$; B'a " =(30×911)e. =\$2.901.

3. Interest on \$1300 for 1 yr. @ 34% =\$45.50: ** 41790 6.6 66

5%=000.50: Total interest for 12 mo.=\$135:

Time for which \$136 is interest=12 mo.:

112.50×12 135

4. Diameter of plate=1/(6°+8°) in.=10 in.

the of & cost=112 cost:

tan of a cost the cost: ... 488 cost=188 cost-\$21;

. . zła cost=\$21;

.". cost=490 of \$21:

and cost of 1 yd .= ziz of 494 of \$21=\$3.

Not income= for of riv of stock=\$1140; Stock=100 of 100 of \$1140=\$40000;

Cost of \$40000 stock=\$36000:

7. Part done by James in 1 hr.= i of i

John " 1 hr .= + of 1 of 1=1:

4.6 . 44 Charles " 1 hr.= ** of 1 = 1;

all 1 hr.=4.

Time to do & of work=1 hr.:

e " all the " =3 hr.

8. 5× 7=25

8×11==33

2×13=26

```
Weight of 1st metal=## of 1410 lb.=525 lb.:
      " 2nd " = 11 of 1410 lb.=495 lb.;
           " 3rd " =## of 1410 lb.=890 lb.
   9. 180 of 1st sum=180 of 2nd=10 of 3rd=10 of 4th;
         .. 1st sum= f of 2nd=2×3rd =3×4th;
   .'. 1st sum++ of 1st, ×+ of 1st, ++ of 1st=$5600;
                               .'. 1st sum=# of $5600=$2100:
                                  2nd " = t of $2100=$1750:
                                  3rd " = of $2100=$1050;
                                  4th " = 1 of $2100=$700.
                Time A runs 1 mi. = \frac{5280 \times 12}{270 \times 48} \text{min.} = 48 \text{min.}
  10.
       Distance B runs after 4 min.=(63360-4×300×44) in.
                                  =10560 in.:
              Time to run 10560 in. =\frac{10560}{320\times44} min. =$ min.;
          Time for B to run a mile=4f min.:
... B wins by [(4f-4f)×270×48] in.=50 yd.
               EXERCISE CCCII. PAGE 197.
             Area of triangle=1/(48×25×19×4) sq. ft.
  1.
                            =301.993376 sq. ft.
  Area of equilateral triangle=(16×16×1/3) eq. ft.;
                            =443.404 . . sq. ft.;
           Difference of area=141.4 . . sq. ft.
  2. A's share= to of D's:
           " = to of A's=to of to of D's=rea of D's;
           " =(10+160) of D's=100 of D's;
  ... (1+100+180+188) of D's share=$3560;
           ... D's share=192 of $3560=$2000:
              A's " = of $2000 =$600;
                   " = 100 of $2000=$780;
              B's
                  " = 180 of $2000=$180.
  S. Helling price of first lot=$1875 + \frac{62}{100} of selling price;
   .: 934 of "=$1875;
         11 =18 of $1875 =$2000;
```

... price of second lot=| of \$1200=\$1296.

```
Interest on $34000 for 1 yr. at | 5 == $170;
 .'. the interest on $(34000+14000) for 1 yr. at lower rate=$1920;
         ss ss 8100
                               " 1 yr. " " =0111 =06;
                                  .'. rate=4% and 44%.
         Cost price of the mixture=|| of 66c. =55c.;
   8.
              Price of 2 lb. of tea=(2×55)e. =110e.:
       Price of 1 lb. of better kind=(110-50) c.=800.
   6. No. of days' work for 1 man=24×No. of men;
                  " " 1 " =16× (No. of men+16);
               ... 24×No. of men=16×No. of men+256;
               ... 8×No. of men=256:
                   .'. No. of mon=32.
   7. When B is at the town, A is ‡ of the way there.
   Distance A goes in 70 min.=(18×3) mi.
   But B meets A ? of 12 mi, from the town;
              ... the distance= } of the distance+(3j+8) mi.;
         . d of the distance=111 mi.:
              .'. the distance=f of 11f mi.
                                           =151 \text{ mi.}
  8. Capital at end of 4th yr.=192 of $3660.25=$91506.25;
Hence, 11 of 11 of 11 of 11 of original capital=$91506.25;
       Circumference of dial=(2×9×4) ft.:
. . No. of min. -spaces in 11 ft.=
                           2×9×41 of 60 min.-spaces
                          =11f min.-spaces;
  Hence, the time is 11f min. past 12.
 10. (1) Interest on $120 for 1 time =$5;
      ... $120 " 2 times=$10:
      .'. discount on $130 " 2 " =$10:
               " $125 " 2 " ___125×10
     (2)
               Interest for 1 time=1 of principal;
            .'. amount for 1 . " =## " . "
               " 2 times =(14) of principal
                                 =## of principal:
             .. interest for 2 times=4% " "
 . discount for 2 times on ### of principal=175 of principal;
           .'. discount for 2 times on $125=$(125×41)=$04.
```

PART III.

Suggestions for Teaching Arithmetic.

I. NUMBER WORK.

I. Counting

Let the pupils use splints, pebbles, measure with rules, etc.

II. Numbers from 1-10.

(a) Teach each number as a whole by means of (1) objects, (2) definite measures, and (3) number-pictures, and have the pupils learn the symbol (figure) for each.

The following is and gested as blackboard summary:

Norn.—Only one form of number-picture should be presented so that the

(b) Teach the facts of addition and subtraction in connection with each number and introduce the symbols of operation + and -.

Thus, by objects as splints, definite measures as 1 in., 1 ft., etc., and by number-pictures teach that

| | AND SOURT STATE | |
|--------|--|-------|
| 5+1=6. | e je priše ekonomija 🧸 🐧 | -5=1. |
| 1+5=6. | | |
| T-0-0. | The first of the f | -1=5. |
| 4+2=6. | | |
| | A Charles and a second | -4=2. |
| 2+4=6. | | 0 4 |
| | La Spilla la Charles Contra Co | -2=4. |
| 3+3=6. | The state of the s | 0 |

If though, preferable begin with 3+3=6, etc.

No fact should be symbolized until the pupils have performed the operations by counting, measuring, etc.

These facts will be fixed by brief, repeated drills (a) with objects, (b) without objects, (c) having pupils form problems, (d) having pupils work problems.

Norm.—(1) In practice it is better to postpone the facts of multiplication and division until the pupil has a general knowledge of numbers to 30.

NOTE,-(2) The pupils may be exercised in making and solving such exercises as

| 4+2=1 4+ | 1=6. |
|----------|------------|
| | f=2. f-1=2 |
| | 1=6. |
| R 0. 0 | 1=2 |

III. The Numbers from 11-20.

(a) Analyze these numbers as in step II., the work being confined to the facts of addition and subtraction and one of the parts being always 10. Thus,

(b) The numbers from 1-20 should now be measured by such units as 2, 3, 4, etc., and such questions answered, as how many times 2 inches make 8 inches? How many twos make 8? etc.

IV. The Numbers from 21-106.

By using number-pictures, definite measures, etc., these numbers should be analyzed to discover the chief facts of addition, subtraction, multiplication and division, the tens being mainly dealt with, thus,

Nors.—No attempt should be made to break the number up into such parts as 87=19+18=16+21=13+24, etc.

II. ARABIC NOTATION AND NUMERATION.

I. The Units.

As the numbers from 1 to 9 are developed their symbols are given and pupils learn to associate each number with its symbol.

II. The Tens.

Have bundles of ten and single splints.

Have pupils represent 1 splint, thus, 1.

Have pupils represent 1 bundle of ten, thus, 1.

How is the 1 representing 1 splint to be distinguished from the 1 representing 1 bundle?

The teacher explains that this is done by the position of the 1's. The 1 representing 1 bundle of ten is always placed to the left of the 1 representing 1 splint.

Hold up 2 bundles of ten and 1 splint and have the number represented by 21; 3 bundles of ten and 1 splint and have it represented by 31, etc.

Now, put down the 1 splint and holding the bundle, give the question, How can the one bundle of ten be represented to show that is a bundle of ten and not a single splint?

The teacher will thus be able to show the use of 0 is to give position to the significant figures.

Continue to 100, as 30, 40, 50, 60, 70, 80, etc.

III. Combine the Tens and the Units.

Thus, 25, 27, 34, 39, 47, etc.

IV. Hundrods.

- (a) Using bundles of ten-tens, show, in a similar way, that 1, 2, 3, 4, etc., in the 3rd place represent hundreds.
- (b) Combins hundreds, tens and units together and give such drill as will enable pupils to write and read with readiness any number expressed by three figures.

V. Thousando.

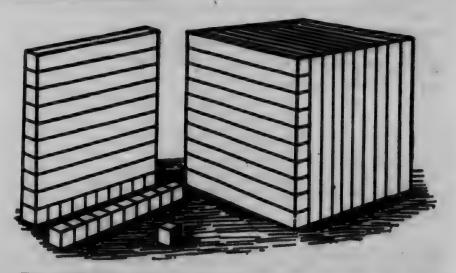
- (a) In a similar way teach the thousands' place and have much practice in reading and writing numbers expressed by four figures.
- (b) Introduce the fifth place, give its name, and, as before, give much practice in reading and writing numbers of five figures.
- (c) Introduce the complete period and give practice in reading and writing it as before.
- (d) Teach the meaning of period and how many places constitute a period. Show that in the two periods that have been taught that units, tens, and hundreds occupy the same relative positions.

NOTE.—The first period is the units' period; the second one, the thousands', &c.
The first period is never to be called the hundreds' period as some teachers do-

VI. Large Numbers.

- (a) Teach the millions' period by giving its name and drilling in reading and writing numbers of 7, 8 and 9 figures.
- (b) Continue thus giving the names and periods in order and having much drill.

The following device of Sonnenschein and Nosbitt is suggested as a better means of impressing the idea that each digit has two values, an obsolute one, and a relative one depending upon its position in a number:



The small cube represents 1 unit; the stave is 1 ten; the plate is 1 hundred; and the large cube, 1 thousand.

A handy teacher can make these for himself. There should be at least 19 each of the small cubes, staves, and plates. It is to be used in a similar manner to the splints, bundles of ten, etc.

NOTE.—In our system of notation 3 figures make a period. This is the French system of notation. In the English 6 figures make a period. One million is expressed in the same way in each case, viz., 1,00000. One billion in the English system is expressed thus, 1,000000,000000, and is honce 1000 times as great as our billion.

HI. ROMAN NOTATION.

I. Numbers from 1-10.

(a) By means of the reader, let the pupils observe how the lessons from 1 to 10 are numbered.

Tabulate the results as 1=1; 2=II; 8=III; 4=IV; 5=V; etc.

- (b) From observation of these symbols teach the following:-
- 1. The effect of repeating a symbol.
- 2. The effect of writing a symbol of lower value to the left of one of greater value.
- 3. The effect of writing a symbol of less value to the right of one of greater value.
 - 4. How often a symbol is repeated.

M. Numbers from 11-100.

- (a) Teach how to read and write the tens as 20, 30, 50, 40, 60, 70, 80, 100, 90.
- (5) Combine the tens and units as 17, 24, 43, etc.

III. Numbers from 100-2000.

- (a) Teach the hundreds alone as 100, 200, 300, 500, 400, sic.
- (b) Combine the hundreds and tens as 110, 120, 250, 340, etc.
- (e) Combine the hundreds, tems and units as 275, 456, 945, etc.

Norn.—Pupils will thus see that encolour. Anothe Mitation must always be represented by its Roman equivalent belong going to the next place. Thus,

IV. ADDITION.

I. Orei Addition, or the Addition Table.

Pupile should not be given written addition until they can combine numbers without counting by ones. Facility in oral addition can be secured by (1) constant drill and (2) correct practice.

Delli Extrelate.

(1) Count by twoe beginning with (a) 2, and (b) 1, up to and just beyond 100.

Count by threes beginning "th (a) 8, (b) 2, and (c) 1, up to and just beyond 100.

Treat each of the other numbers up to 10 in a similar way.

(2) Teach the sum of two numbers, as 7+8; 8+7.

Pay attention to the ending, as 17+8; 18+7; 27+8; 28+7, etc. When a second combination is known as 5+5, use these in giving drill in rapid addition as (add from the left)

When a third combination, as 4+8, 3+4 is known, other exercises are given st,

As each new combination is learned, as 9+8, the pupil should use it as shown above, thus,

Thus, the pupil is never called on to add combinations which he has not learned and thu compelled to resort to counting on his fingers, or making marks which he counts.

Pupils should be taught from the beginning to give the sum at once; thus, in the last line: 17, 25, 30, 30, 47, etc., and not 9 and 8 is 17; 17 and 8 is 25, etc.

(3) Piace a number in the centre of a circle with other numbers round the circumference. Have the pupils add the number in the centre to those on the circumference as they are rapidly pointed to.

Vary the tens in the numbers on the circumference.

(4) Write the digits on the blackboard, as

2, 7, 8, 8, 9, 6, 4, 7, 5, 2, 8, 3, 7, 9, etc.,

and as the digits are pointed to have the pupils add. At first take the answer as seen as the sum is sufficiently large; but after a time have a number of such exercises before there is any interruption in the concentrated effort necessary, the pupils placing the answer to each exercise as soon as the teacher stope pointing and being ready to begin adding as seen as he begins to point to the digits again.

Gradually increase the speed of pointing.

(5) Write a column of digits on the blackboard and as soon as the last figure is on erace the whole. The pupils must add as the digits are placed on the board.

The answers may be taken as in (4) above.

(6) Train pupils to look for easy combinations, especially those that make ten.

Morn.-1. In all the exercises used to secure accuracy and rapidity in addition, experience shows that rapidity and accuracy are closely associated together.

2. When a pupil fails, assertain where and why and give special exercises on the combinations causing the difficulty.

II. Written Addition.

- (a) Addition where there is no carrying.
- (1) Show how the addends must be placed.
- (2) Give examples for practice.
- (3) Give problems to be solved.

Norn.-In an example the pupil is told what he is to do; in a problem he is required to find the process for himself.

- (b) Addition where there is carrying.
- (1) Show the necessity of carrying.
- (2) Show the convenience of beginning at the right hand side.
- (3) Give examples for practice.
- (4) Give problems to be solved.

In introducing carrying, let the pupils do a few examples, thus,
4 3 7 Then their knowledge of notation should be used
6 5 9 to show that 24 units are the same as 3 tens and 4
8 7 8 units, etc. Make use of the plates, staves and cubes,
18 15 34 or bundles of splints.

The exercises on pages 15 and 16 of the Public School Arithmetic are so arranged that they may be added without transferring the figures to the slate or note book and any number of addends may be given up to 29 on page 16 or 43 on page 15.

M. Methods of Proof.

Pupils should be shown how to prove their work.

(1) Add upwards and downwards. If the sums agree the work is likely correct.

(2) Divide the addends into a number of groups. Find the sum of each group. Then find the sum of these sums. If the result agrees with the sum of all the addends the work is likely correct.

V. SUBTRACTION.

I. Oral Subtraction, or the Subtraction Table.

This is merely the converse of 'he addition table. It should be impressed by mue—skilful drill and practice.

Drill Exercises.

(1) Count backwards by twos from 100.

| threes (* 98. | |
|--|--|
| (c) (d) (d) (d) (d) 98. | |
| (c) (d) (d) (d) (d) 98. | |
| 11 11 11 11 11 11 11 11 11 11 11 11 11 | |
| | |
| | |
| four 100. | |
| 90, etc. | |

(2) Describe a circle; place the subtrahend at the centre and round the circumference write numbers. Let the pupil subtract as the teacher points to a number on the circumference.

(3) Place the minuend at the centre of a circle and the digits in any order round the circumference. Let the pupil subtract as the teacher points to a subtrahend.

(4) Place the digits in any order upon the blackboard, as

7, 4, 9, 5, 3, 8, 6, 2, 1,

and require the pupils to subtract each from a ρ ? en number, as 70, when the digit is pointed to.

(5) Pince the digits as in (4) and let the numbers indicated by the digits be successively subtracted from a given number, as 65. Thus, 65, 56, 56, 45, 49, 37, 29, 23, 21, 20.

II. Witten Subtraction.

- (a) bubiraction where every figure in the minuend is of a greater value than the corresponding figure in the subtrahend.
- (1) Give examples and show how the subtrahead is placed with reference to the missead.
 - (2) Give problems.
- (b) Subtraction where every figure of the minused to not greater than the corresponding figure of the subtrahend.

There are several modes of procedure here.

(I) The method of Decomposition eften improperly called the "borrowing" method,

Thus, from 22 splints take 14 splints.

$$32 = 8 + 2 = 8 + 13$$
 $14 = 1 + 4$
 $1 + 8 = 18$

Illustrate by using bundles of ten splints, or by taking staves and changing one into its equivalent number of cubes.

(II) The method of Equal Additions often improperly called the "borrowing and carrying" method.

Borrowing is incorrect because in borrowing several conditions are to be fulfilled. (a) There must be a leader. (b) The leader has less after than before the leading. (c) The leader must be repaid. (d) He will then possess the original amount. These conditions are not fulfilled in subtraction.

The method of Equal Additions depends upon the principle that adding the same number to both minuoud and subtrahead does not alter the remainder.

Illustrate this principle by many examples, as

| From | 5 | 7 | | 6 | 16 | 26 |
|------|---|---|-----|---|----|----|
| Take | | 5 | . 7 | 2 | 12 | 22 |
| | 2 | 2 | 8 | 4 | 4 | 7 |

Norm.—While it is important for the teacher to understand the rationals of processes, the important thing for the pupil is facility in performing operations; hence, at this stage the pupil may be shown there is a reason for what is done, but he should not be expected to reproduce the reason.

(III) Computers' Subtraction,

This method is based on the fact that the sum of the remainder and the subtrahend is equal to the misuend.

From 49721 take 15697.

7+4-11; 4+8-12; 9+8-17; 6+3-0; 1+3-4. 49721 15097 This is the most direct way of preceeding from the known 23504 addition table to the answer required in subtraction.

Norr to erithmetical complement of a number in the difference between it and the uses of the next higher order. Thus, 4, 5, 165, respectively, one the e next higher order. Then, 4, 8, 142, respectively, are the meents of 6, 55, 565, being the differences, respectively, of 6, 50, and 897 and 10, 100, and 1000.

The computers' method is cometimes called the method of complementary addition for the reason that the complement of the Agure in the subtrahend which is greater than its corresponding figure in the minnend is added to the latter figure.

Thus, in the examples given above, the complement of 7 is 3; 3+1=4; the complement of 4 is 6; 6+2=8; etc.

The advantages of this method are the following:

(1) The sum of a number of addends can be subtracted at once from a given number.

Thus, from 8073 take the sum of 247, 968, and 3714.

8073 247 4+8+7+(4)=23 964 2+1+6+4+(4)=17 3714 1+7+9+2+(1)=30 3144 2+3+(3)= 8

(#) Subtraction and addition can be taught together. Thus, addition, 2+3=5, or 2 and 3 is 5; subtraction, 2+(3)=5, or 2 from 5 leaves 3.

(3) It may be used to shorten long division. Thus, divide 183410 by 379;

379)188410(483

4×9+(8)=44; 4×7+4+(1)=88; 4×8+8+(8)=18. 3181 8×9+(9)=81; 8×7+8+(4)=68; 8×8+6+(1)=81.

(4) In business, it is the method followed in making change.

(5) No special device is needed to obviate the difficulty when a digit in the subtrahend is of greater value than the one above it; hence, the labor required to teach subtraction is greatly lessened.

M. Mithods of Proof.

- (1) By Addition. The sum of the remainder and the subtrahend is equal to the minuend, if the work is correct.
- (2) By Subtraction. When the remainder is taken from the minuend, the result is the same as the subtrahend, if the work is correct.

VI. MULTIPLICATION.

I. Oral Multiplication, or the Multiplication Table.

Using splints, definite units in measuring, the numeral frame, etc., build up the table.

Thus, 1 in.+1 in.=2×1 in.=2 in., or 2 times 1 in. is 2 in.

2 in.+2 in. $=2\times3$ in.=4 in., or 2 times 2 in. are 4 in.

3 in.+3 in.=2×3 in.=6 in., or 2 times 3 in. are 6 in.; etc.

Then, 2×1=2:

2×2=4; proceeding from the concrete to the abstract.

 $1 \text{ in.} + 1 \text{ in.} + 1 \text{ in.} + 1 \text{ in.} = 4 \times 1 \text{ in.} = 4 \text{ in.}$, or 4 times 1 in. is 4 in.

 $2 \text{ in.} + 2 \text{ in.} + 2 \text{ in.} + 2 \text{ in.} = 4 \times 2 \text{ in.} = 8 \text{ in.}$, or 4 times 2 in. are 8 in.

 $3 \text{ in.} + 3 \text{ in.} + 3 \text{ in.} + 3 \text{ in.} = 4 \times 3 \text{ in.} = 12 \text{ in.}$, or 4 times 3 in. are 12 in.

Then, 4×1=4;

4×2=8, etc.

Thus it will be seen that multiplication is a short method of doing addition when the addends are all the same.

It will also be understood why the multiplier is always an abstract number.

Fix the table by much drill and as soon as a few of the facts are learned begin written multiplication.

Drill Exercises.

- (1) Describe a circle; place the multiplier in the centre and round the circumference range the figures, including 0, in any order. Have the pupils tell the product as a figure is pointed to.
- (2) Write the figures in any order in a row upon the blackboard, and placing the multiplier above, have the product given as a figure is pointed to.
- (3) Write the figures as in (2) and have a pupil begin at one end to state the successive products to the other.

NOTE.—When a pupil fails, he should discover the correct product by using addition.

II. Written Multiplication.

- (a) Short Multiplication.
- (1) Where there is no carrying.

Show how to place the multiplicand and multiplier and how to proceed.

Thus, John and James have each 243 marbles. How many have they together?

| Marbles | Marbles |
|---------|---------|
| 243 | 243 |
| 243 | 2 |
| 486 | 496 |

(2) Where there is carrying.

Show by easy examples the connection between carrying in addition and in multiplication.

| CTR1 | 6, | * | | | | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | |
|-------|----|-------|------|------|--------|---------------------------------------|------|
| Thus, | 25 | 1.7 - | 1 20 | 756 | | H. Darie | 750 |
| | " | *** | | | 49. 7 | | 100 |
| | | | | 756 | 21.000 | | 0 |
| | | | | | | | |
| | | | | 1513 | | | 1519 |
| | | | | | | | 4074 |

Give (1) examples; (2) problems.

In problems the pupil should learn (1) why the multiplicand may be any kind of a quantity; (2) why the multiplier must always be an abstract number (so many times); and (3) why the product must be of the same denomination as the multiplicand.

This will save both teacher and pupil from blundering later on by talking of such impossible operations as multiplying length by width and producing something different from either multiplicand or multiplier.

(b) Multiplication by Factors.

This must now be introduced to lead to Long Multiplication.

(1) Teach the term, Factor.

Use the pupil's knowledge of the multiplication table and place on the blackboard such products as

| 3×7=21
4×9=36 | 3 | and | 7 | RPO | the | factors | of | 21; | |
|------------------|---|------|---|-----|-----|---------|----|-----|------|
| | | | v | | • | 46 | | 36; | |
| 7×5=35 | 7 | . 44 | 5 | 8.6 | 4.6 | | | | ete. |

(2) By using numbers not greater that 12 show

(i) That multiplying by a number and by the factors of the number produce the same results.

| | - | and bearing | Learnie | | | |
|-------|-----|-------------|---------|-----|---|-----|
| Thus, | 17 | | 17 | 17 | t | 17 |
| | 19 | | 3 | 4 | | 6 |
| | 204 | | 51 | 68 | | 102 |
| | | | 4 | 3 | | 2 |
| | | 2 | 104 | 204 | | 204 |

- (ii) That it does not matter in which order the factors are used.
- (iii) That when a number can be resolved into several sets of . factors it does not matter which set is used.

In connection with this give much practice in multiplying by 20, 30, 40, etc., 200, 300, 400, etc., 2000, 3000, 4000, etc.

Show that the convenient factors are 10 and 2; 10 and 3; 10 and 4; etc.; 100 and 2; 100 and 3; 100 and 4; etc.; 1000 and 2, etc.

(c) Long Multiplication.

Illustrate the principle of long multiplication, vis.: Multiplying the several parts of the multiplicand by the several parts of the multiplier, multiplier the aggregate multiplicand by the multiplier.

Thus the pupil will see there is a reason for what he is doing. He should not be expected to fully reproduce it.

$$8 = 8+3$$

 $9 = 2+7$
 $72 = 2\times5+2\times8+7\times5+7\times3$

The pupil can multiply by 3 and by 20 and, hence, by 23.

$$\begin{array}{c} 362 \\ \underline{23} \\ 1086 = 3 \text{ times } 362. \\ 7240 = \underline{20} \quad \text{`` } 362. \\ 8326 = \underline{23} \quad \text{`` } 362. \end{array}$$

Multiply 457 by 205.

The uselessness of putting down the 0's will soon be observed and it will be noticed that the correct result is found by placing the first figure of each partial product under that figure of the multiplier by which it is obtained.

NOTE.—As accuracy and rapidity are closely associated, much drill should be given in doing a certain amount of multiplication in a given time. A number, as 788304, may be taken and the pupil required to multiply successively by a given multiplier (as multiply by 2, the resulting product by 2, the new product by 2, etc.) as often as possible in the specified time, as one minute; or a given number may be multiplied successively by a given multiplier a fixed number of times and the time required to do this observed.

In connection with problems, care must be taken to see that the correct multiplier is used.

Taus, find the cost of 7 hats @ \$3 each.

The pupil must understand (1) that 7 is the multiplier and (2) why 7 hats should cost 7 times as much as I hat. This step is often neglected.

Sometimes the multiplier is large and the multiplicand small when the above solution is used, hence another is suggested.

Find the cost of 7890 articles at \$5 each.

Cost of 7896 articles at \$1 each=\$7896;

" #5 " =5 times \$7896=\$39480. 7896

III. Proof of Multiplication.

(1) Until division is reached the only proof pessible is to multiply the multiplier by the multiplicand. If the two products are the same the work is likely correct.

(2) After division is known two other methods of proof may be tiend':

(a) Divide the product by the multiplicand. If the quotient is the same as the multiplier the work is likely correct.

This method has the advantage of locating the error, should there be one.

(b) Casting out the nines.

Cast the nines out of the multiplicand and out of the multiplier, multiply the remainders together and east the nines out of the product. The remainder thus obtained should be the same as that from easting the nines out of the product of the multiplicand and multiplier. Observe this method fails:

(i) If the order of figures in the product is misplaced, as 375

for 735.

(ii) If errors are made which counterbalance each other as 259 for 619, the remainder in each case being 7.

(iii) If 9 is written for 0, or 0 for 9, or if either is omitted or inserted too often.

IV. Mechanical Work in Multiplication.

In giving mechanical work from the blackboard the teacher should make the finding of the answer easy for himself. Short "euts" are good for the teacher, not for the pupil.

A few of these are suggested here,

- 1. (a) $53 \times 53 = 50 \times 56 + 3^* = 2809$.
 - (b) 78×78=80×76+2*=6084.
 - (a) 798×793=800×786+7°=628849.

- 2. (a) $46 \times 44 = 50 \times 40 + 6 \times 4 = 2024$.
 - (b) $123 \times 127 = 180 \times 120 + 3 \times 7 = 15621$.
 - (a) $152 \times 158 = 160 \times 150 + 2 \times 8 = 24016$.

Notice the number of tens is the same in both multiplier and multiplierand and that the sum of the units of the multiplier and multiplierand is ten.

3. Use the Arithmetical complement.

The arithmetical complement of a number is the difference between the number and the unit of the next superior order.

Thus, the A.C. of 6 is 10-6, or 4; of 78 is 100-78, or 22; of 584 is 1000-584, or 416.

Multiply 9984 by 9996.

9984; A.C. is 16 The A.C. of the multiplicand and 9996; A.C. is 4 multiplier are multiplied together and 99800064 0064 as many figures are written in the product by placing naughts to the left as will make the number of places, equal to the number of figures in the multiplicand or multiplier. Set down this product. Then the A.C. of the multiplier is subtracted from the 1 ultiplicand or vice versa and the emainder is written to the left of the figures already placed.

Norm.—(1) The multiplier and multiplicand should have the same number of figures.

(2) For convenience numbers with small A.C.'s should be used.

V. Contractions in Multiplication.

It is recommended that practice in such contractions as the following be given advanced students.

Such exercises are valuable in that:

(1) They facilitate results.

(2) They give pupils a clearer conception of the nature of the multiplication process.

(3) They furnish excellent practice to the pupils in determining the relations between numbers.

I. To multiply by such numbers as 999, 798, 9998, etc.

Ex. 1. Multiply 784564 by 999.

734564000 = 1000 times the multiplicand.

1. x. 2. Multiply 587469 by 798.

469975200 = 800 times the multiplicand.

 $\frac{1174938}{468800262} = \frac{2}{798} + \frac{11}{11} + \frac{11$

II. To multiply in a given number of lines of partial products.

Ex. 8. Multiply 785649 by 369 in two lines of partial products.

(36)9

7070841 = 0 times the multiplicand.

28283364 = 40 " 9 times, or 360 times the multiplicand.
280904481 = 369 " the multiplicand.

Ex. 4. Multiply 81234567 by 64432 in three lines of products.

81234567

(64)(4)(32)

294988268 = 400 times the multiplicand.

2599506144 = 8 "4 times, or 32 times the multiplicand.

5199012288 =2000 " 32, or 64000 times the multiplicand.
5234105620944 =64482 " the multiplicand.

III. To multiply by 5, 25, 125.

(1) To multiply by 5, multiply by 10 and divide the product by 2. $5=10\div 2$.

(2) To multiply by 25, multiply by 100 and divide the product by 4. 25=100÷4.

(3) To multiply by 125, multiply by 1000 and divide the product by 8. 125=1000-8.

VIII. DIVISION.

L Oral Division, or the Division Table.

The Division Table is the converse of the Multiplication Table and can be learned from it.

The pupil should discover similar answers to the following questions in connection with each product in the multiplication table:

- (1) How often can 2 be taken from 6?
- (2) How many 2's are there in 6?
- (3) How many times 2 make 67
- (4) How often is 2 contained in 6?
- (5) One of the factors of 6 is 2, what is the other?
- (6) Divide 6 into 2 equal parts.
- (7) What is the half of 6?

Suggestions for Drift.

(a) Describe a circle. Place the divisor in the centre, and round the circumference place numbers up to 12 times the divisor. Point to these and let the pupil tell instantly the quotient and

remainder. If he cannot tell, he should discover the nequired answer by using objects, or number-pictures.

(b) Place the digits in any order upon the blackboard with the divisor above, as

Point to a digit and have a pupil divide. If there is a remainder place it to the left of the next digit pointed to and divide the resulting number, etc.

Norn.-During the learning of the division table the pupils should gradually discover (1) that division is the process by which having given a product and one factor the other may be found; and (2) that Division is a short precess of performing asveral specessive rabtractions of the same number.

Let the pupils discover the latter by working with objects such problems as, Among how many boys may 30 marbles be divided, giving each boy 5 marbles!

| 20 | mark | la c |
|----|---------|------|
| | 1 1 4 1 | |

- Taking 6 marbles and giving them to the first boy,
- there are 25 remaining.
- Taking 5 of these and giving them to the second boy,
- there are 30 marbles remaining.
- Talling 5 of these and giving them to the third boy,
- there are 15 marbles remaining.
- Taking 5 of these and giving them to the fourth boy,
- there are 30 marbles remaining.
- 8 8 25 5 10 6 B 5 Taking 5 of these and giving them to the 56th boy,
- there are 5 marbles remaining.
- Taking these and giving them to the sixth boy, there are none remaining.

Hence, 30 marbles may be divided among 6 boys, giving to each boy 5 marbles.

If 36 marbles are divided equally among 6 boys, how many does each boy

30 maybles

- Taking 6 marbles and giving each boy I.
- there are 24 remaining.
- Taking 6 of these and giving each boy 1,
- 18 there are 18 remaining and each boy has 2.
- Taking 6 of these and giving each hoy 1,
- there are 13 remaining and each boy has \$.
- Taking 6 of these and giving each boy 1,
- there are 6 remaining and each boy has 4.
- Taking these 6 and giving each boy 1,
- there are none remaining and each boy has 5.

II. Short Division by the Long Division Method.

Divide 68 splints equally between 2 boys.

Let the pupils discover how many each boy will get by dividing 6 hundles of ten and 8 eplints.

Then show the figuring on the blackboard, thus,

Divide 72 splints equally between 2 boys.

As before, the pupils have 7 bundles and 2 sp!ints. The half of 6 bundles is readily found and after a time they find they must untie the bundle and then they have 12 splints, which they can easily divide into 2 equal parts.

Show the figuring:

| 2) | Splints.
72
6 | Splints.
(36 |
|----|---------------------|-----------------|
| | 12
12 | |

Ill. Short Division by the Usual Method.

NOTE.—In working problems pupils should learn that there are two kinds of exercises, vis.: (1) those in which the divisor is an abstract number and (2) those in which the divisor is of the same name as the dividend.

In each of these cases they should be exrefully trained to know the nature of the quotient and the remainder.

Thus, when the divisor is an abstract number, the quotient and remainder are always like the dividend. When the divisor is of the same name as the dividend, the quotient is always so many times and as in.(1) the remainder is of the same name as the dividend.

IV. Long Distalon.

Pupils should be trained in the following steps until they are automatic:-

- (1) See how many times the divisor is contained in the part of the dividend to be considered.
 - (2) Place the figure in the quotient.
- (3) Multiply the divisor by this number and place the product under the part of the dividend under consideration.
 - (4) Subtract the product from this part of the dividend.
 - (5) Bring down the next figure in the dividend.

After a pupil knows these steps there still remain two difficulties to be overcome:—

- (a) To tell the quotient figure.
- (b) To supply a 0 in the quotient when the divisor is not contained in the part of the dividend to be divided.

To evercome (a) let the pupils form the multiplication table for the given divisor. Thus, suppose the divisor is 19, let them put down 19 times.

| 19×1=19
19×2=88
19×3=57 | It will be an easy matter to divide correctly by 19. |
|--|---|
| 19×4=76
19×5=95
19×6=114
19×7=133
19×8=152 | After a time this help should be withdrawn and examples with divisors like 51, 61, 461 given for working, gradually increasing in difficulty as in Exercise XLIX. |
| 19×9—171 | |

To oversome (b) let the pupils go through the steps of Long Division just enumerated. This difficulty arises from attempting to crowd too much upon the pupil before he is ready for it.

Thus, divide 856905 by 21.

| 1)856905(| 40800 |
|-----------|-------|
| 16 | |
| 100 | |
| 10 | , |
| 108 | |
| 105 | |

After a time the pupils will see the uselessness of setting down the product by 0 and will shorten the work in the usual way. V. Division by Factors.

- (a) Division when there are two factors and no remainder.
- (b) Division when there are two factors and a remainder with the first only.
 - (c) Division when there are two factors and remainders with each.
- (d) Division when there are three or more factors and remainders with any or all the divisors. Divide 132 by 19

| no row nh TS | | | |
|--------------|------|---------------|-------------------------------|
| 12)132 | 3)33 | 8)182
4)44 | 6)13 <u>2</u>
2)2 <u>2</u> |
| | | | |

Working an example in this way shows

(1) A number is divided by another when it is divided by one factor of the divisor and the resulting quotient divided by the othert

(2) Either factor may be used as the first divisor;

(3) When a divisor can be received into several sets of factors, it matters not which set is used.

Ex. 1. How many 3 sekages of 15 lb, each can be made of 578 lb. of sugar, and how many pounds will remain?

The working of such by factors depends on the principle that the remainder is always of the same kind as the dividued.

3 578

â

5)192 bags of 3 lb. each and 2 lb. remaining;

38 packages of 15 lb. each and 2 bags of 3 lb. each remaining;

Hence, the remainder is (2×3+2) lb., or 8 lb.

As a first step put the sugar into bags of 3 lb. each. Now show that 5 of these must be put together to make a package of 15 lb.

The work should be shown to be correct by means of Long Division.

VI. Methods of Proof.

(a) Multiply the Divisor and Quotient together and to the product add the Remainder; the sum should equal the Dividend if the work is correct.

(b) Subtract the Remainder from the Dividend and divide the result by the Quotient; the result should equal the Divisor if the

The following are suggested as TESTS of the THEORY of the Simple Rules

| cembre 125188; | | or one amount of the |
|--|---|---|
| Addition,
987
27684
384560
444444 | | Subtraction. *********************************** |
| 57694
1256031 | | Division.
379)*******(2487 or ***)82031(976 |
| Multiplication. | | 243 over. 47 over. |
| 75649
3×7
529543
************************************ | 5687

**** | 3708) 28157041 (**** |
| | | 32010 |
| 27006693* | | 34704 |
| | • / | 18321

2197 |
| | | 419/ |

VIII. PROBLEMS.

Experience shows that the chief difficulties in solving problems arise from the following causes:—

(i) Pupils do not understand the nature of the transaction involved in the problem.

(ii) They are unable to analyze the given conditions and so determine their relations to the quantity to be found.

(iii) They have an imperfect understanding of the nature of the four simple operations of Arithmetic.

Hence, the steps in teaching the solution of a problem are as follows:

(i) The pupil must acquire as clear an understanding of the nature of the transaction as possible. This should be illustrated by the teacher in the concrete. Failure to do this makes much of the commercial arithmetic incomprehensible, more especially to girls.

(ii) The problem must be analyzed to connect what is given with what is to be found.

When pupils understand the transaction involved, and by questions have been made to reason out the connection between the statement and the demand, they should be left to find a way of solution for themselves.

Many teachers fail at this point; for not satisfied with leading the pupil to the difficulty, they teach the solution as well. In fact much of the questioning is often on the solution rather than on the reasoning.

A pupil who understands the four fundamental operations and who is trained to be accurate in his mechanical work will have little difficulty in reaching a correct result.

Mechanical accuracy should be insisted upon. It should be felt to be a disgrace to make a mistake in addition, subtraction, etc. A pupil should be held responsible for every figure he sets down.

(i) It is a good plan to train pupils to state the supposition or datum by itself and underneath it to write the demand.

(ii) In the case of "Rule of Three" problems the supposition should be written so as to bring the number of the same name as the answer required, at the end of the statement.

Then the pupil should reason from the number given to unity and from unity to the number required.

When he is able, he should reason at once from the number given to the number required.

(iii) When teaching, the problems should be classified; when testing, missellaneous problems should be used.

(iv) In giving problems the teacher should have a definite end in view. This requires forothought on his part.

(v) All work should be done neatly and intelligibly.

(vi) Pupile should be taught to examine their answer to see if it is a resconable one.

(vill) Questions occurring in practical life are often of great interest to pupils.

(ix) Pupils should be exercised in making problems; i.e. Probiem-making should accompany problem-solving.

Ex. 1. Find the cost of 7 barrels of flour if \$30 pay for 5 barrele.

Solution: - Cost of 5 barrels = \$30; (a) 44 44 1 barrel ==\$30+5

(4) " " " 7 barrelam) times \$6-\$12.

(0) The reasoning from (a) to (b) is 1 bbl. is 1 of 5 bbl.; hence, the price of 1 bbl. will be 1 of the price of 5 bbl.

Similarly, the reasoning from (b) to (c) is 7 bbl. is 7 times 1 bbl.; hence, the price of 7 bbl. will be 7 times the price of 1 bbl.

Ex. 2. A building-lot 30 ft. in frontage by 120 ft. deep is sold at \$100 per foot frontage. How much is that per sere?

Before such a problem is given, pupils should understand square measure and the finding of the area of a surface. It should not be necessary to teach these when the problem is given.

The new feature in this problem is the method of measuring city property. The explanation of this should precede the solution, a diagram being placed on the board to aid the explanation.

After this explanation the class should have an opportunity to work the problem without further aid.

For these unable to work it, such questions as the following will be found helpful:-

Show a foot frontage on the diagram. How deep is the lot? What is the area of a foot frontage carried back to the depth of the lot? Ams. 120 sq. ft.

What is the value of this much land? Ans. \$100.

What is required to be found?

How many sq. ft. are there in an accef Ass. (4840×9) sq. ft.

The reasoning in this case is (4840×9) eq. ft. is $\frac{4840\times9}{120}$ times 120 eq. ft., hence the cost of (4840×9) eq. ft. is $\frac{4840\times9}{120}$ times the cost of 130 eq. ft.

وبشياطا

(i) It is a mistake to conduct the work as if getting a solution and finding the answer were the main purpose in the solution of problems.

This accounts for pupils being tought the solution of type problems and being required to remember these as so many facts.

- (ii) It is a mistake to divert attention to the merely mechanical operations involved.
- (iii) It is a mistake to allow the "unitary method" to be mechanically used. Pupils must be required to reason at each step.

For further exemplification of solutions see Part II.

IX. REDUCTION. AND THE COMPOUND RULES.

By using proper appliances, pupils should be led to discover most of the facts of the tables. Thus, they can discover that 2 pints make 1 quart; 4 quarts make 1 gallon; etc.; 12 inches make 1 foot; 3 feet make 1 yard; etc.; 144 square inches make 1 square foot; etc.; 1728 cubic inches make 1 cubic foot; etc.

During the learning of the tables many simple problems should be worked, nothing being said of Reduction, as

Ex. 1. How many pints are there in 5 qt.?

1 qt.=2 pt. :

But 5 qt.=5 times 1 qt.;

Honee, 5 qt.=5 times 2 pt., or 10 pt.

Similarly, How many pints in 2 qt. 7 in 7 qt. 7 in 12 qt. 7 etc.

Ex. 2. How many pints are there in 3 qt. 1 pt.?

1 qt.=2 pt.;

3 qt.=3 times 1 qt.;

.'. 3 qt. = 3 times 2 pt., er 6 pt.;

.'. 8 qt. 1 pt. -6 pt. +1 pt., or 7 pt.

Similarly, how many pints in 4 qt. 1 pt.7 in 7 qt. 1 pt.7 in 10 qt. 1 pt.7 etc.

Ex. 3. How many quarte are there in 12 pt. ?

2 pt.=1 qt.;

2 pt.) 12 pt.

6 times:

.'. 12 pt.=6 times 1 qt.=6 qt.

Similarly, how many quarts in 8 pt. 7 in 16 pt. 7 in 30 pt. 7

Ex. 4. How many quarts are there in 7 pt.?

2 pt.=1 qt.; 2 pt.)7 pt.

3 times and 1 pt. over:

... 7 pt.=8 times 1 qt.+1 pt.=3 qt. 1 pt.

Similarly, how many quarts are there in 18 pt.f. in 17 pt.f in 23 pt.f

SURPACE MEASURE.

1. Definition of Surface.

By having the pupils pass their hands over the outside of such objects as boxes, cylinders, spheres, sheets of paper, etc., their minds are prepared for the term surfaces. Have many surfaces now pointed out and touched.

2. Dimensions of Surface.

Show that each surface has length and breadth, or height and length, etc., but never length, breadth and thickness; also that the boundaries of a surface are lines.

3. Shapes of Surfaces, ----

Teach the terms rectangle, or oblong, and square. State that surfaces are measured in squares. Teach the terms, square inch, square foot, square yard.

4. The Table.

Have pupils draw a square foot and mark it off into square inches. When they have found the number of square inches in a square foot, give easy problems to utilize the information they have gained.

Treat the square yard similarly.

Have the pupils measure a square red under your directions. Then have each draw a plan of the square rod, using an inch to represent a yard. Mark off the plan into square inches each of which will thus represent a square yard. It will be readily seen that there are 25 such squares and 10 obiougs, each representing one-half a square yard and I square half as large as one of the oblongs, making 30% square inches in all and representing 30% square yards in 1 square red.

In a convenient place have the pupils measure 16 rd. by 10 rd.; tell them this is an acre; and have them draw a plan of this with 1 inch representing 1 rod. By marking the plan off into square inches, they will discover that 160 square rods make I acre.

CUBIC MEASURE.

1. Mooning of Solid.

Show solids and then withdraw them. Pupils will observe that objects take up room, or space. The term solid is given, and pupils give a definition. "A solid is anything that takes up, or occupies, space." Have pupils give examples."

2. Etmonology of Solids.

Show that solids are bounded by surfaces and that they have length, breadth, and thickness.

3, Volume and How It is Measured.

The amount of spaces an object occupies is called its volume. Teach the terms rectangular solid and cube. Tell pupils the volume of a solid is measured in cubes and teach the terms cubic inch and cubic foot. Let the pupils discover the number of inchslices the cubic foot will make, the number of rows of cubic inches, and the number of cubic inches in each row of the slice. They will thus be able to find the number of cubic inches in the 12 slices.

Give easy problems to utilize the information acquired. Teach the cubic yard in a similar manner,

DEHOMMATE QUANTITIES; DENOMINATIONS.

\$6, \$9, \$2.75 are quantities that express value.

4 oz., 7 lb., 7 lb. 3 oz. are quantities that express weight.

3 hr., 7 min., 4 hr. 8 min. are quantities that express time.

All these are called Denominate Quantities.

Apple,

In So, the unit is le-

In 4 os, the unit is 1 os.

In 5 mi, the unit is 1 mi.

These are Simple Denominate Quantities because the Denominate Quantity is expressed in one kind of unit.

The unit in which a Simple Denominate Quantity is expressed is called its DENOMINATION.

Again,

t

g

In \$9.25 the units are \$1 and 1c.

In 7 lb. 9 oz. the units are 1 lb. and 1 oz.

In 8 ft. 6 in. the units are 1 ft. and I in.

A denominate number expressed in more than one kind of unit is called a Compound Denominate Quantity.

The units in which a Compound Denominate Quantity is expressed are called its DENOMINATIONS.

Exercises should be given in determining whether a denominate quantity is simple or compound.

WEDUCTION.

- (a) By means of questions similar to the following, the terms, Reduction, Reduction Descending, Reduction Ascending, should be taught:
 - (1) In \$0, how many cents are there?
 In 4 lb., how many runess are there?
 In 3 lb. 7 oz., how many curess are there?
 - (2) In 700 cts., how many dollars are there?
 In 32 cs., how many pounds are there?
 In 45 cs., how many pounds are there?
- (b) When examples in written reduction are reached, the pupil should be required to write out the work in full for a time. When the process is understood he should be shown the abbreviated form in ordinary use and required to compare the new form, step by step, with the one used at first.

Ex. 1. Reduce 5 bu. 3 pk. 1 gal. 2 qt. to quarts.

5 ba. 3 pk. 1 gal. 2 qt.

! In giving an oral explanation of this, the pupil should be required to give a full statement, thus, 28 pk. 1 bu. is 4 pk.; 5 bu. are 5 times 4 pk., or 20 pk.; 3 gal.

20 pk. plus 3 pk. are 23 pk.; etc. 47 gal.

d qt. 190 qt.

It should be quite clear to the pupil that 4 pk., 2 gal., 4 qt. are the multiplicands and the respective multipliers are 5, 23, and 47, sistract numbers, not denominate once.

If thought desirable, the "Law of Commutation" may be used. Thus.

4 times 5 pk. are the same as 5 times 4 pk; " 23 gal. " "

" 47 qt. " 4 at.

(c) In Reduction Ascending similar steps should be followed. Ex. 2. Reduce 317 qt. to bushels.

(i) dilities 4 qt.=1 gal.; 4 qt.)817 qt.

79 times and 1 qt. over.

... 317 qt.=79 times 1 gal.+1 qt.=79 gal. 1 qt.

2 gal .= 1 pk.; 2 gal.) 79 gal.

39 times and 1 gal. over.

... 79 gal.=39 times 1 pk.+1 gal.=39 pk. 1 gal.

.'. 317 qt.=39 pk. 1 gal. 1 qt., etc.

317 qt.==12 gal.=79 gal. 1 qt.; (ii)

79 gal.=17 pk. =30 pk. 1 gal., etc.

6 qt.)317 qt.

2 gal.) 79 gal. 1 qt.

29 pk. 1 gal., etc.

In giving an oral explanation of this, the pupir smould give a full statement, thus, 4 qt. make 1 gal., hence 317 qt. will make as many gallons as the number of times 317 qt. contains 4 qt., etc.

COMPOUND ADDITION.

| R | 170 | 17 | | | | |
|---|-----|------|--|---|------|----|
| 7 | 6 | . U. | | | L T. | U. |
| | | 5 | | | 7 5 | 8 |
| | 8 | | | | 7 | 5 |
| | | 9 | | | | |
| | | 81 | | | | _ |
| | 9 | 9 | | - | 3 8 | |

By questions cause the pupil to discover why he sets down 1 in the units' place and easies 3 to the tens; etc.

II. Addition of Compound Quantities.

| | - Committee | , | |
|----------|--|-------|-----|
| 7 5 8 | | 4. 5 | D. |
| 9 7 5 | energaen two persons programs. | 9 7 | . 5 |
| 9 9 9 | The second secon | 6 8 | 9 |
| 31 29 21 | | 82 11 | 7 |

Make it clear that the only difference between Simple and Compound Addition is in the fact that the number of units making 1 of the next higher order is constant in Simple Addition, being always ten, while in Compound addition, this number varies. This can be well done by using the same numbers in Simple and Compound Addition.

COMPOUND SUBTRACTION.

The steps in Compound Subtraction are similar to those in Compound Addition.

Whatever method of subtraction is used in Simple Subtraction, the same method should be used in Compound Subtraction. In giving the first lesson, the same numbers should be sed in Simple and Compound Subtraction.

COMPOUND MULTIPLICATION.

1. Resiew Simple Stuttleliestics.

| | - Ł | |
|------------|---------------------|-----------|
| H. T. U | . 23 | |
| 7 5 9 | | a TE TEL |
| Total Mary | and the second that | 0 9 |
| 49 98 69 | THE REAL PROPERTY. | 1 1 1 1 1 |
| 43 90 OS | : 58 | 1 8 |

The pupil should be able to explain why he sets down 3 in the units' place and carries 6 to the tens; etc.

II. Multiplication of Compound Quantities.

| 7 | 8. | D. 9 | | A.
7 | 8. | D.
9 |
|----|----|---------|--|---------|----|---------|
| 40 | 85 | 7
63 | | 51 | | 7 |

In giving the first lesson, care should be taken to use the same numbers as multiplicand and multiplier in both Simple and Compound Multiplication.

COMPOUND DIVISION.

(A). WHEN THE DIVISOR IS AN ABSTRACT NUMBER.

I. Review Simple Division.

II. Division of a Compound Quantity.

(B). WHEN THE DIVISOR IS A DENOMINATE NUMBER.

Introduce this by problems such as the following:

- 1. How many yards of cloth at 2s. a yard can be bought for 20 s.f
- 2. How many yards of cloth at 2s. a yard can be bought for £1? What step had to be taken in the latter case which was not taken in the former?
 - 2. How often can you subtract 5s. from £2f

How often does £2 contain 5a.?

Explain the steps by which £2 is divided by 5a.

4. How often does £2 5s. contain 9s.?

Explain the steps in the solution.

Continue such examples until it becomes clear that to divide one denominate number by another, each must be reduced to the lowest denomination mentioned in either.

X. SIMPLE APPLICATIONS OF THE PREVIOUS RULES. BILLS AND ACCOUNTS.

In teaching this subject, a bill neatly written and perfect in all its details should be on the blackboard.

The pupils should be questioned to cause them to discover the following:

- (a) What is shown in the bill.
- (b) Why each item of detail is shown.
- (c) The arrangement of the various parts.
- (d) The effect of omitting any detail.

After such a bill has been carefully studied, and the details tabulated, the pupils should be given practice in ruling bills, filling in details, etc.

The common mistake in teaching a bill is in attempting to build up a bill, 6.c., in teaching synthetically instead of analytically.

SIMPLE MEASUREMENTS.

THE RECTANGLE.

Case I. Given the length and width of

Pupils should draw rectangles of various dimensions. These should be subdivided into squares according to the unit of area selected. The pupils will thus learn that the unit of area can be placed along one side of the rectangle as often as there are corresponding linear units of measure in that side and that there are as many rows of such square units of area as there are corresponding linear units in the adjacent side of the rectangle.

Ex. 1. Find the area of a restangle ? ft. 4 in. long by 1 ft. wide. Let 1 sq. in. be the unit of area.

Length of rectangle=16 in.; Width " Area of rectangle 1 in. long by 1 in. wide=1 sq. in.; 16 in. " " 1 in. " =16×1 sq. in.;

16 in. " "12 in. " =12×16×1 aq. in.

=192 sq. in.

A number of examples worked by the pupils by means of diagrams will show them that the area of a rectangle is found by multiplying the number of units of length by the number of like units of width to obtain the number of corresponding units of area.

Case II. Given the area of a rectangle and one of its dimensions to find the other.

As in Case I the pupil should be required to draw a rectangle and place along the side whose length is given as many square units of area as there are corresponding linear units of length. It will then be an easy matter to find how many such rows must be taken to form a rectangle as large as the given one. Thus the number of linear units of measurement in this dimension will be

Ex. 1. A rectangular floor contains 486 sq. ft. It is 27 ft. long, find its breadth.

Number of square units along the length=27;

" rows to make 486 sq. ft. =486÷27=18.

Hence, the breadth is 18 ft.

Week a number of similar examples and the rale will follow:

Divide the number of units of area by the number of extremonding units a, 11h or breadth and the questions will be the number of like linear units in the side to be found.

Metalea

(a) In Case I the most common mistake is in teaching that the length is multiplied by the width.

One who talks of multiplying length and width together does

not understand the nature of multiplication.

- (b) In Case II the usual mistake is to divide the eres by the given dimension. The foundation of this error lies in not understanding the nature of division. It is impossible to divide square units by linear units.
- (c) Another mistake consists in giving a mechanical solution as follows:—The area is the product of two numbers. Our of these is given. How is the other found? This is purely mechanical as it does not compel the pupil to analyze the problem and give an adequate reason for each step.

BOARD MEASURE.

To teach Board Measure, have several boards a root square and of various thickness, as 2 in., 4 in., 1 in., 2 in., 3 in., etc.

Explain that the boards & in. thick, & in. thick, and 1 in. thick are all called one board foot; that the 2 in. one is 2 beard feet; the 2 in. one is 2 beard feet; the

RECTANGULAR SOLIDS.

Case J. Given the length, width and Mickness of a rectangular solid to find the cubic content.

The pupils should be required to draw rectangular solids of various dimensions. These should be subdivided into cubes according to the unit of subic content selected.

Ex. 1. How many c. ft. of air are there in a rectangular room 18 ft. by 10 ft. and 10 ft. high?

No. of c. ft. which can be placed on length=18 c. ft.;

'' on floor = (16×18) c. ft.;

'' in room = (10×16×18) c. ft.

=2890 c. ft.

A number of examples in which the pupils are required to draw and subdivide the solid and set down a solution will show them that the subic content of a rectangular solid is found by multiplying the number of units of length by the number of like units of width and this result by the number of like units of thickness to obtain the number of corresponding units of solid content.

Case II. Given the cubic content of a rectangular solld and two of its dimensions to find the other.

As in Case I the pupils should be required to draw a rectangular solid and place a layer of cubic units corresponding to the measurements given along the side of the solid whose dimensions are given. It will then be an easy matter to find how many such layers are necessary to form the solid.

Ex. 1. There are 60 cords of wood in a pile 8 ft. wide and 12 ft. high. How long is the pile?

No. of e. ft. in the pile of wood= (60×128) e. ft.; No. of e. ft. which can be placed on one end= (8×12) e. ft.;

No. of layers to make (60×128) e. ft. $= \frac{60 \times 128}{8 \times 12} = 80$. Hence, length of the pile is 80 ft.

Mictalian.

The following mistakes are often made:-

- (a) Pupils are taught to multiply length, breadth and thickness together.
- (b) The cubic content is divided by the area of one side and the quotient is called the third dimension.
- (c) A solution is given which, although theoretically correct, becomes mechanical, e.g.,

The number of units of cubis content is the product of three factors. If this product is divided by the product of any two of them, the quotient is the third factor. A pupil reaches a correct result by this solution but soon loses sight of why it is necessarily correct.

SHARING.

In introducing Sharing, objects should be used to aid pupils in forming a conception of what is to be done and how it may be performed. These should not be continued too long. Pupils should be encouraged to "picture" to themselves what they are called on to do.

Case 1. Sharing where provision has to be made for some receiving more than others.

Ex. 1. Divide 86 marbles between James and Frank so that Frank may have 10 more than James.

Piret give Frank 10.

This will leave 26 to be divided equally between Frank and James.

26 marbles + 2=13 marbles;

James' share-13 marbles:

Frank's " =(10+13) marbles=23 marbles.

Show that the shares 18 and 33 fulfil all the conditions of the problem.

It samuet be repeated too often that pupils should be trained to examine their results and find whether they fulfil the conditions required.

Ex. 2. Divide \$112 among A, B and C, giving B \$7 less than A who is to receive \$16 more than C.

C receives the least.

Extra for C=#0;

" ." A=\$16; ;

" B=\$(16-7)=\$9;

Extra for A and B=\$25.

Setting this saide for A and B, the sum left to be divided equally among three is \$(112-25), or \$87.

867÷3=639.

A receives \$(29+16), or \$45.

U ** \$(29+0), or \$29.

The pupils should be required to show that these results are correct.

Case II. Sharing where the ratio of the shares is given.

.Ex. 3. Divide \$100 between James and Frank so that James may have 3 times as many as Frank.

When Frank has \$1,

James has \$3,

Both have \$4.

It is evident that Frank will have as many times \$1 and James as many times \$3 as the number of times \$4 is contained in \$100.

:". Frank's share=0(25×1)=\$25;

.'. James' = 4(25×3)=\$75.

Hx. 4. Divide \$60 among A, B and C, giving B twice as much as A, and C three times as much as B.

When A gots \$1,

B gets \$2,

and C gets \$6,

out of every \$0.

\$65 + 60 = 7 times;

B " # 7 " 92, or \$14;

C 44 4 7 4 05, or \$43.

Ex. 5. Divide \$45 between A and B so that B may receive \$3 as often as A receives \$2.

When A receives \$3
B '' \$6
out of every \$6
\$45:45=9 times;

Case III. Sharing where Cases I and II are combined.

Ex. 6. A, B, and C together have \$308. B has \$13 more than twice as much as A, and C has \$20 more than four times as much as A. How much has each?

Extra for B=#13;

Extra for B and C=\$33;

Remainder to be divided=\$(206-33)=\$175;

A has \$1, B ** \$2,

G " 84.

out of every \$7.

\$175-\$7=25 times.

A has 25 times \$1, or \$25.

B " 25 " \$2+\$13, or \$63.

C " 25 " \$4+\$20, or \$120.

Ex. 7. \$2.40 is made up of three times as many 5s. pieces and twice as many 10s. pieces as 25s. pieces. How many are there of each?

These are one 25c. piece, two 10c. pieces, and three 5c. pieces, out of every 60c.

Honce, there are 4 times 1 twenty-five cent piece, or 4 twenty-five cent pieces;

4 times 2 ten cent pieces, or 8 ten cent pieces; and 4 times 3 five cent pieces, or 12 five cent pieces.

Norn.-The "equational" method may with profit be introduced to more

Ex. 8. Divide \$607 among A, B, and C, so that B may have \$20 less than 3 times A's share and C \$17 more than twice B's.

Let A receive 1 share,
then B receives 3 shares—\$20,
and C '' 6 shares—\$40+\$17;
all receive 10 shares—\$60+\$17;
.'. 10 shares—\$60+\$17=\$497;
.'. 10 shares—\$407+\$43;
1 shares—\$407+\$45.
Sum B receives—\$245—\$30=\$115,
'' C '' =6x\$45—\$30=\$115.

XI. FACTORS, CANCELLATION, MEASURES AND MULTIPLES.

L FACTORS.

L Prime and Composite Numbers.

(a) Use the pupils' knowledge of factors (see Multiplication) to teach the distinction between Prime and Composite numbers.

Blackboard summary:—

| than on | Other factors t | | noopt one
number; | No factors o |
|---------|-----------------|---|--|--------------|
| 6 | 6 | | | 8 5 |
| | 10 | | | 7 |
| | 12 | 5 17 34 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | en e | 17 |
| | Composite 2 | STUSSEL LIT | mbers. | Prime Nu |

(b) In a similar manner teach the distinction between Odd and Even numbers.

II. To receive a number tale Prime Factors.

Br. 1. Besoive 120 into prime factors.

| 2) 120 | Dietie a |
|--------|--|
| 3)00 | Divide the given number by the smallest prime |
| | factor other than 1; treat the quotient in a similar |
| 2)30 | Manney, and so on middle desired to a similar |
| 3)15 | manner, and so on until a quotient which is a |
| -110 | prime number is obtained. |

The divisors and hast questions will be the prime factors of the number.

The question for the pupil is, What is the smallest prime number that is a factor of 120? Then of 60? Then of 30? Then of 15?

(s) Gradually teach the common tests of divisibility.

(1) A number is exactly divisible by 2, if the right hand figure is 0 or indicates an even number.

(2) A number is exactly divisible by 3, if the sum of its digits is exactly divisible by 3.

(3) A number is exactly divisible by 4, if its two right hand figures are zeros or express a number exactly divisible by 4.

(4) A number is exactly divisible by 5, if its right hand figure is 6 or 5.

(5) A number is exactly divisible by 6, if it is even and exactly divisible by 3.

(6) A number is exactly divisible by 8, if its three right hand figures are seves or express a number exactly divisible by 8,

(7) A number is exactly divisible by 9, if the sum of its digits is exactly divisible by 9.

(6) A number is exactly divisible by 11, if the difference between the sum of the digits in the edd places and the sum of the digits in the even places is either 0 or exactly divisible by 11. Thus, 75601 is exactly divisible by 11, 7+6+1=5+0.

(b) To find all the divisors of a number.

Ex. Find all the divisors of 360.

| 2)360 | 1, 2, 4, 8
1, 3, 9 | |
|-----------|---|----|
| 2)90 | 1, 2, 4, 8, 8, 6, 12, 24, 9, 18, 36, 1 | 79 |
| 8)15
6 | 1, 2, 4, 8, 3, 6, 12, 24, 9, 18, 36, 7
5, 10, 20, 40, 15, 30, 60, 120, 45, 0 | 2, |

Bessive the number into the prime factors.

Form as many series as there are different prime factors, making I the first term of each series, the first power of the factor the second term, the second power of that factor the third term, etc. Multiply these series tegether as shown. The resulting products will be the divisors of the number.

IL CANCELLATION,

Teach the principle on which Cancellation is based, vis. Dividing both divisor and dividend by the same number does not affect the quotient.

Thus, #1-4-4-4-4-4-6.

In cancelling care must be taken to place the uncancelled faster in place of the cancelled number. When this is not done pupils get the idea that 0 replaces the number.

Ex. 1. Divide the continued product of 16, 4 and 5 by the continued product of 8, 2 and 10.

HL MEASURES.

l. Deffaillean.

(a) Measure.

Review and teach measure by such problems as the following:-

- (1) Find all the units of length which will exactly measure 12 in.; 15 in.; 18 in.; 20 in.; etc.
- (2) Find all the units of area which will exactly measure 6 sq. ft.; 16 sq. ft.; 26 sq. ft.; 27 sq. ft.; etc.
- (3) Find all the units of value which will exactly measure 25e.; 50e.; 75e.; etc.

(b) Common Measure.

Find all the units of length that will exactly measure 18 ft. and 24 ft.

Blackboard work:

The measures of 18 ft. are 1 ft., 2 ft., 8 ft., 6 ft., 9 ft., 18 ft. The measures of 24 ft. are 1 ft., 2 ft., 8 ft., 4 ft., 6 ft., 8 ft.,

12 ft., 24 ft.

The measures common to 18 ft. and 24 ft. are 1 ft., 2 ft., 3 ft.,

(e) Greatest Common Messure.

By examples worked as in (b) the G.C.M. is seen to be the largest factor common to all the given numbers.

ft. To find the G.C.M.

Ex. 1. Find the G.C.M. of 560, 600, and 700.

| 3/500 | 600, | 700 |
|---------|------|-----|
| 3) 280, | 315, | 850 |
| 3)140, | 315, | 178 |
| 4)70, | 316, | 178 |
| 5)35, | 315, | 178 |
| 7)7, | 68, | 35 |
| | - | 100 |

Piret find the prime far ore of one of the numbers easily factored, as 560.

Then try each factor in turn as a trial factor of the other numbers and strike out such as are not found to be factors of each of the other numbers. The product of all the 5 common divisors will be the G.C.M. required.

NOTE.—The number selected must be resolved into prime factors, less a smaller factor found in one of the other numbers may be overlooked.

In practice the G.C.M. is most readily found by using the following principle:—"The G.C.M. of two numbers must be a factor of their difference or of the difference between a multiple of one of them and the other."

Ex. 2. Find the G.C.M. of 520 and 007.

667-820=136.

136-2×3×35.

By inspection it is seen that neither 2 ner 3 is a common factor. By trial 23 is found to be a factor of 520 and hence must be contained in 667, 6 times more than in 529.

When there are three or more numbers, the G.C.M. is a factor of the smallest difference between any two of the numbers.

Ex. 3. Find the G.C.M. of 406, 510, 544, and 506.

The smallest difference is 24.

34-3×17.

2 is seen not to be a common factor.

By trial 17 is found to be a common factor.

With large numbers the work may be set down as follows:

Ex. Find the G.C.M. of 680 and 1573.

| | The state of the s |
|------------|--|
| 689 2 1573 | The difference between a multiple of 680 and |
| 780 4 1878 | 1578 to 106 - 4b - 310 |
| | to is too; the dimerence between a multiple of |
| 91 2 196 | 196 and 680 is 91; the difference between a multiple of 91 and 195 is 132 this is contained a multiple |
| ET 8 400 | and does it of the dimerence between a multiple |
| P1 7 182 | of 91 and 195 is 13; this is contained exactly in 91 |
| | the state of the s |
| 91 1 13 | and is the G.C.M. of the murchess |

IV. MULTIPLES.

L Dellattions

· (a) Multiple.

Have pupils multiply such quantities as 3 in., \$5, 7 successively by 1, 2, 3, 4, 5, etc.

Blackboard work:

| Products. | Producte. | + £8 | Products. |
|--------------------------|------------|------|------------|
| 1×3 in.= 3 in. | 1×45=45 | · | 1×7= 7 |
| 2×3 in.= 6 in. | 2×45=#10 | • | 2×7=14 |
| 8×8 in. $= 9$ in. | 3×45=415 | | 8×7=21 |
| 4×8 in.=12 in. | 4×45=430 | | 4×7=28 |
| ' Multiples. | Multiples, | | Multiples. |

Have each multiple in the first column measured by 3 in; in the second, by \$5; in the third, by 7.

Thus it is evident that a multiple of a given number may be defined as (1) one or more integral times the given number or (2) as a number which contains the given number exactly.

(b) Common Multiples. . 1

Have pupils write multiples thus;-

The multiples of 2 are 2, 4, 6, 8, 10, 12, 14, 16, 18, etc.

Then have the common multiples selected, vis., 6, 12, 18, etc.

(c) Lenet Common Multiple.

From among the common multiples of numbers found in (b), select the smallest number which is a common multiple of each of the given numbers.

Thus, multiples of 6 are 6, 12, 18, 34, 30, etc.

The L.C.M. of 6 and 9 is 18.

II. To find the L.C.M.

(a) Use the mathod of resolving the numbers in prime factors.

Ex. 1. Find the L.C.M. of 24, 30 and 36.

24=2×2×2×2.

10=2×3×5.

25=5×7.

To contain 24 the L.C.M. must have the prime factors 2, 2, 2, 3; to contain 30, 2, 3, 5; and to contain 35, 5, 7. Hence, to contain

24, 36, and 35, the L.C.M. must have (2, 2, 2, 3), (3, 3, 5) and (4, 7) as factors, or 2, 2, 2, 3, 5, and 7.

L.C.M.=2×2×2×3×5×7=840.

The pupils should be questioned as to how many times each of the numbers is contained in the L.C.M. and made to see that the quotients are prime to one another.

From a series of examples worked in this way the rule will be derived, vis.: The L.C.M. of two or more numbers is the product of all the prime factors of the numbers each being taken the greatest number of times it is found as a factor in any of them.

(b) For young pupils the following is a convenient application of the rule :-

Ex. 2. Find the L.C.M. of 15, 18, 24, 40, 50 and 60.

2) 35, 18, 24, 40, 50, 50 2)15, 9, 12, 20, 25, 30 2)15, 9, 6, 10, 25, 15 5)5, 8, 1, 5, 26, 5

The numbers are arranged as shown and a prime number that is contained exactly in any two or 3)15, 9, 8, 5, 25, 15 more is selected and need m a divisor as shown. Then a second d, a, d, 1, 5, 1 prime number is enlisted and need

as a divisor like the first. Thus the week is carried an antil these is no prime number greater than one that is contained in any two of the quotients. The product of the divisors and undivided quotients will be the L.C.M. required.

Time, L.C.M. -- 8X3X2X2X5X8X6=1800.

(c) The following method is recommended for entrance pupils. Ex. 3. Find the L.C.M. of 15, 18, 24, 40, 30, and 60.

60)15, 18, 24, 40, 50, 60 30)1, 8, 2, 2, 5, 1 11, 1, 1, 1, 1, 1 L.C.M.==60×30==1800.

One of the numbers, as 60, having several factors is selected. The G.C.M. of 60 and each of the given numbers is cancelled out of the numbers in succession and all

the uncancelled factors and any uncancelled numbers are written in a line. These are then treated in a similar manner unless the L.C.M. can be found by inspection as above. The product of all the numbers colored will be the L.C.M. of the given numbers.

A very common mistake is to speak of one number containing another evenly when exactly is meant. Thus 35 contains 7 exactly 6 times.

XII. FRACTIONS.

L DEFINITION, NOTATION AND NUMERATION.

There are three steps in teaching the definition:

(1) Division of a unit into equal parts.

(2) Comparison of the parts with one another and with the unit.

(3) A collection of the equal parts.

A fraction is a number and should be treated just like integral numbers. The only difference is that in the integral number, the unit is a whole, as in 7 the unit is 1; in 7-eighths, it is 1-eighth. In a fraction the unit is a definite part of the primary unit, as in 3-fourths, the unit is one-fourth of 1; in 5-eighths of a dollar, it is one-eighth of one dollar.

A common mistake is made in speaking of dividing a unit into parts instead of equal parts.

Pupils should be required to solve by actual measuring many problems, as find 3-fourths of a foot; 5-sixths of 18 inches; etc.

. As soon as pupils have the notion of fraction, the notation and numeration should be given and explained. The terms, numerator and denominator, should be given and their significance abown. Thus, in \$, the 5 indicates the fractional unit and so gives a name to the number, 4, which is hence called the numberer, or numerator.

The connection between whole and fractional numbers should be impressed by many examples in Addition, Subtraction, Multiplication, and Division of fractions given now. Of course the fractions to be added or subtracted must have a common denominator. Thus,

IL REDUCTION.

The terms, proper fraction, mixed number, improper fraction, lowest terms, etc., should be introduced and taught as required. (a) Reduction of a whole number to a fraction with a given dea

Rx. 1. How many ninths are there in 7?

Since 1=0 minths and

7m7 times It

.'. 7=7 times 9 minths=63 minths=4.

Ex. 2. How many ninthis are there in 7\$?

The important point here is for the pupil to know that 7\$ is. 7+\$. This should be made clear in teaching the meaning of mixed number by such examples as, Mary bought 7 yards of cloth and then f of a yard more. How much did she buy altogether? Since 78-7-1-8

Ex. 3. Express AA as a mixed number.

4 fourths) 35 fourths

(4) Reduction to lower or higher terms.

Great care should be taken to teach the principle upon which this rests, viz., Dividing or multiplying both terms of a fraction by the same number does not after the value of the fraction.

. (1) In teaching this use the knowledge of reduction of compound numbers to show that where the value of the unit is changed, the number of such units is necessarily changed so that the value of the quantity may not be altered; thus, 5s.=60d.; 43-12 twenty-five-cent pieces; etc.

(2) Use such expedients as:

(i) Divide a foot into 2 equal parts and represent one-half of it as 1.

(ii) Divide a foot into 4 equal parts and represent one-half of it

(iii) Divide a foot into 6 equal parts and represent one-half of it aa 8.

(iv) Divide a foot into 9 equal parts and represent one-third of it as f.

(v) Divide a foot into 18 equal parts and represent one-third of # as A.

(vi) Divide a foot into 3 equal parts and represent one-third of it as t.

(3) Take paper such as is used in Kindergartens for folding and fold it as illustrated below.



(4) Have pupils rule two diagrams, each 1 in. squars and have them show that forth; forth; fort; forth; etc.

(5) Constantly call for the reasoning meed in working Energices CXIX, CXX, CXXI, CXXII.

(d) Reduction to equivalent fractions with the least common de-

(1) Exercises in which one denominator is a multiple of each of the others, as 4, 4, and 4.

(2) Energies in which the denominators are prime to one

another, as \$, \$, and \$.

(3) Exemines in which the denominators are not prime to one another, as t, fr, and fr.

(f) Reduction of Compound to Simple Fractions. Steen. 284

(1) The Definition.

The usual definition, "a fraction of a fraction," Is so concise that it is difficult for a beginner to comprehend it; hence, many exercises similar to the following should be worked:-

(i) Pind I of a foot. Find for half a foot.

(ii) Find \$ of a yard. Find \$ of a third of a yard.

(iii) Pint 4 of 4 of a yard; etc.

(iv) Draw an inch square. Mark off † of it; then find † of the part marked off.

These and similar exercises will make clear that a compound fraction is a number of the equal parts of a fraction.

Contrast a compound fraction with a simple one.

(2) Simplifying compound fractions.

The following are suggested as a series of exercises:

(1) 1 of 1; 1 of 1; 1 of 11.

(ii) \$ 0: A; \$ of \$\$; \$ of \$\$.

- (fill) det Ly tofft toft.
- (iv) \$ of \$; \$ of \$; \$ of \$.
- (v) \$ of 41; \$ of 34; \$ of 14.

In solving (iii) make use of the pupils' knowledge of reduction of denominate numbers to aid them in understanding why the second fraction must be changed.

Thus, to find one-failf a dellar, the dellar must be changed into such a quantity that it can be divided into two equal parts, as 100c., or 4 quarters, etc.

Bolution of (iii)
$$i=\frac{2\times 1}{2\times 3}=i$$
:
 $i=1$ of $i=1$ of $i=1$.

Solution of (iv)
$$\phi = \frac{5 \times 4}{5 \times 7} = \frac{44}{5}$$

Norm 1.-Draw diagrams and show that

2.—Show how cancellation shortens the work. Thus,

M. ADDITION OF FRACTIONS.

Street,

NS

90

- (1) Addition of fractions having a common denominator, as
- (2) Addition when one of the denominators is a multiple of each of the others, as 1+1-1-1
- (3) Addition w ... the denominators are prime to one another, as i+i+i=!
- (4) Addition when the denominators are not prime to one another, as \(\frac{1}{4} + \frac{1}{4} = \frac{1}{4}\)
 - (5) Addition of mixed numbers, as 41+21=1

Hence, add the sum of the whole numbers to the sum of the fractions to find the sum of the mixed numbers.

Norz.—It is easy for the teacher to add two fractions with a common numero-

$$t+t=\frac{2\times (7+9)}{7\times 9} = -6t.$$

$$t+t=\frac{5\times (12+18)}{12\times 18} = \frac{5\times 30}{12\times 18} = -6t.$$

IV. SUBTRACTION OF FRACTIONS.

Steps.

- (1) Subtraction of fractions having a common denominator, as
- (2) Subtraction when one of the denominators is a multiple of the other, as from \$\frac{1}{2}\$ take \$A_c\$.
- (3) Subtraction when the denominators are prime to each other, as from # take %.
- (4) Subtraction when the denominators are not prime to each other, as from in take it.
 - (5) Subtraction of mixed numbers.

'NOTE.—In taking one mixed number from another there are various ways of proceeding when the fraction of the subtrahead encode that of the minuted.

This is the method of decomposition.

This is the method of equal addition.

This is the method of complementary addition.

In general the last method is the simplest. It consists in adding such a fraction to that in the subtrahend as will make its value 1, and adding the same fraction to the minuend. The subtraction can then be readily performed.

More 1. - Frantisms having the teacher, Thus,

$$\begin{array}{ccc} + -1 - \frac{2 \times (9 - 7)}{7 \times 9} & = 4. \\ 15 - 15 - \frac{17 \times (23 - 19)}{19 \times 23} - 44. \end{array}$$

V. MULTIPLICATION AND DIVISION OF FRACTIONS.

Case I. The Multiplication of a fraction by a whole

Show by many examples that a fraction is multiplied by a whole number either by multiplying the numerator by the whole number or by dividing the denominator by it. . Thus,

Case II. The Division of a fraction by a whole i

By many examples worked as in the reduction of compound fractions, show that a fraction is divided by a whole number either by dividing the numerator or by multiplying the denominator by the whole number.

Case III. The multiplication of a whole number or a fraction by a fraction.

Nors 1.—Before this step is taken the pupil should be taught that a fraction indicates the division of its numerator by its denominator.

Do this as follows:--

M

of

h

r£

(a) Draw two lines, one a foot long and the other two feet long. Take # of the shorter and # of the longer.

Compare these parts.

It will be seen that \$ of 1=\$ of 2, or 2÷6. Similarly show that \$ of 1=2 of 3, or 3-4, etc.

(b) = 1 fourths of a unit; 3=3 times 4 fourths of a unit =12 fourths of a unit: . . i of 3=1 of 12 fourths of a unit =3 fourths of a unit

=1 of 1:

. d of 8=1 of 1.

Ex. 1. Multiply # by 4.

The multiplier is 1 of 3, or 3:4. AXE W. If BUREAU COME MAKE I WE

This result is evidently 4 times too great because the multiplies is 4 times too large.

4 must, homes, he divided by 4.

Hence,
$$\{\times\}=\}\}=\frac{5\times8}{7\times4}$$
 PRODUCT OF SUMERATORS.

Norz 5.—Cure ment be taken to enaced all the further comment to both aumeonters and denominates before performing the multiplication.

NOTE 8.—In giving examples for practice in multiplying one mixed number by another, the teacher can make the work easy for himself by having the whole remains the mass and the wort of the fractions 2.

Case IV. The Division of a whole number or a fraction by a fraction.

In dividing a whole number or a fraction by a fraction there are various ways of proceeding.

Ex. 1. Divide ? by ?.

$$=\frac{1}{5}$$
 $=\frac{3\times 0}{5\times 7}$ $=\frac{1}{5}\times\frac{1}{7}$ $=\frac$

To be referenced as to the more to

formed by inverting the divisor.

This is evidently 9 times too small as f is not to be divided by 7 but by f of 7. Hereo, the true quotient will be 9 times for eff.

Thus,
$$4 \div i = 1i = \frac{3 \times 9}{5 \times 7} = 1 \times 1$$

=dividend multiplied by the fraction formed by inverting the

(e)
$$1 \div 1 = (1 \times 1) + (1 \times 1) = 11 \div 1 = 11 = \frac{3 \times 9}{5 \times 7} = 1 \times 1$$

=dividend multiplied by the fraction formed by inverting the divisor.

This method depends on the following:-

(i) Any number divided by 1 gives that number for quotient,

(ii) Multiplying both divisor and dividend by the same number does not after the quetient.

(iii) The divisor when multiplied by the fraction formed by inverting its terms produces 1,

Nove.—The inverted divisor is called the resipress! of the divisor, resiprocal massless being those which multiplied together will produce unity.

VI. COMPLEX FRACTIONS.

Stope

H.

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(1) The Definition,

Use many enumpies in which one or both terms are fractions as

After giving the term complex fraction to such forms, the definition will readily follow.

- (1) To simplify a complex fraction.
- (a) Use the knowledge that the numerator of a fraction is the dividend and the denominator the divisor.

(b) Use the principle that multiplying both terms of a fraction by the same number does not alter its value.

Multiply both terms by 12 and
$$\frac{1+1}{1+1} = \frac{4+3}{6+4} = \frac{1}{15}$$
.

Multiply both terms by 18 and
$$\frac{2\frac{1}{4}-1\frac{1}{4}}{2\frac{1}{4}+1\frac{1}{4}} = \frac{42-28}{42+28} = \frac{1}{4} = \frac{1}{4}$$
.

In multiplying 2½ by 18, multiply the fractional and integral parts separately and add the results. In multiplying ‡ by 18, divide 18 by 9 and multiply the numerator, 5, by the quotient, 2.

VIL THE GREATEST COMMON MEASURE OF FRACTIONS. Use the pupils' knowledge of the G.C.M. of whole;

Thus, find the G.C.M. of 20s, and fin.

44 . .. £1 and fa. 34 £2 au 1 15a. 66 14, 13d. and 9d. " 1s. and 9d. 44 " 1s. 6d. and 1s.

When the pupils see that the numbers must be reduced to equivalent ones with the same unit, then the application to fraetions is easy.

Find the G.C.M. of #, # and #. Find the G.C.M. of f, A and H.

Beduced to a common denominator these become \$\$, \$\ \$\ and \$\ \$\ \$\.

The G.C.M. is readily seen to be A.

On examining the original fractions, 4 is seen to be the G.C.M. of the numerators and 75 is the L.C.M. of the denominators,

OF, $\sqrt{n} = \frac{0.0.M. \text{ OF HUMBRAFORS.}}{\text{L.C.M. OF DENOMINATORS.}}$

Show that each fraction contains the G.C.M. exactly and that the several quotients are prime to one another.

Thue, f+A=15; A+A=10; H+A=9.

15, 10 and 9 are whole numbers and are prime to one another.

VIII. THE LEAST COMMON MULTIPLE OF FRACTIONS. Use the pupils' knowledge of the L.C.M. of whole numbers.

Thus, find the L.C.M. of 12d. and 8d.

6 ls. and 8d. 11 2n. and 1s. 4d. " £1 5s. and 15s.

As soon as the pupils see that the numbers must be reduced to equivalent once with the same unit, then the application to fractions can be made.

Pind the L.C.M. of A and A. 16 .. 16 . . . 14 " A and H. " 1. 1 and 1.

Reduced to a common denominator, these become if, if and it. The L.C.M. is readily found to be 44, or 4.

Comparing this with the original fractions, the L.C.M. is seen

to be t.c.w. OF NUMERATORS.

Show that this contains each of the given fractions exactly and that the several quotients are prime to one another.

Thus, 4+1-10; 4+1-8; 4+1-15.

10, 8 and 15 are integral numbers and are prime to one another.

IL THE SIMPLIFYING OF COMPLEX EXPRESSIONS.

In simplifying such expressions as those in Exercise CL, the following is the usual usage regarding the signs "of," \times , \div , -. +1-

(1) The operations indicated by " of," × and + should be performed before adding or subtracting.

(2) The operation indicated by "of" should be performed before that indicated by +.

NOTE.—This is the only once in which usage makes a distinction between

(3) The operations indicated by X and + should be performed in the order in which they coour.

X. DENOMINATE FRACTIONS.

L The Deffulti

Distinguish between the primary and the fractional unit and point out that when the primary unit is a denominate number the fraction is said to be a denominate fraction, as \$2, 1 mi., 2 of a league, ato.

2. To find the value of a fraction of a denominate

Ex. 1. Find the value of # of a ton.

Since # t.= | of 4 t. (page 157), 4 t. is divided 5)4 t. 16 ewt. by 5 as in compound division.

Find the value of \$ of £1 to. 4d.

Ex. 1. Express 45 as the fraction of 98.

40 to 1 of 46;

65 to 5 times 61;

.'. 46 to 5 times † of 46, or † at ;

Morn.—This emaple may be worded in any of the follow

(a) Reduce \$6 to the fraction of \$8.

(a) What frustion of 60 in 667 (c) What function in 65 of 692 (d) What part of 60 in 161

(s) If 90 in the unit, what is the measure of \$60

Ex. 2. What part of £7 11s. 8d. is £3 8d. ?

£1 84. =7284.

£7 11s. 84.=1830d.

Man, 1d. to Tries of 1830d.;

But 7284. is 728 times 1d.;

.. 7284. to fife of 18904.: -M-1.

.. 43 84. to \$ of £7 11a 84.

Ex. 3. Reduce Trainer mi. to the fraction of a feet.

1 mi. = 5900 ft. 1

rrous mi. = rrous, of 5260 ft.;

Now, There of 5280 ft ... of ft.:

and Traine of \$200 ft .- A ft .- A ft.

Hx. 4. What fraction of \$ of 42 is \$ of \$?

f of 41-1-11:

Now, & to & of HY

.'. 18 to 18 of 18:

.. f of f in if of f of 4h.

XIII. DECIMALS.

& DEPRNITION

For an introduction to teaching the definition of a decimal see the Public School Arithmetic, page 316.

This will make clear why the first piace to the right of the point is tenths, the second hundredthe, etc.

In introducing the point make use of the notation of deliars and conta. The point fixes the position of units of deliars; new it is used to fix the position of units.

The distinction between common, or unique fractions and decimal fractions, or decimals about the made clear. It should be shown that when both numerator and denominator are expressed the fraction is vulgar; whereas when only the numerator is expressed, it is decimal.

Thus, \$, 16, 16 are common fractions, and .8, .19, .345 are decimals.

II. HOTATION AND NUMERATION OF DECIMALS.

- (1) The reading and writing of integral numbers should be thoroughly reviewed.
 - (2) Pupile should know the following:
 - (a) There are three places in each period.
- (b) Reading from right to left, the first place in each period is units; the second, tens; the third, bundreds.
- (c) The periods from right to left are Units, Thomsands, Millions, Billions, Trillions, etc.
- (d) The value of any digit in a number depends upon its position in that number. Thus, in 193,456,730, the value of 6 in unitthousands, or 6 thousands. The value of 2 is 2 ten-millions, or 20 millions.
- (c). Each digit has thus two values, an absolute value which it has when standing alone, and a relative value depending upon its position in a number. Thus, in the number in (d) the absolute value of 5 is five and its relative value is 5 ten-thousand, or afty thousand.
 - (3) Put a number such as 77777.7777 upon the binekboard.

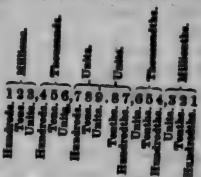
From the introduction (page 115) the pupil will learn that the names of the places to the right of the point are tenths, hundredths, etc.

(4) Show that the same law of increase from right to left or of decrease from left to right prevails to the right of the point as to the left of it.

Thus, 10 of any place makes one of the next higher place, and 1 of any place makes 10 of the next lower one.

The introduction shows that 10 tenths=1 unit; that 10 hundredths=1 tenth; that 1 hundredth=10 thousandths, etc.

- (8) Compare the names of the places immediately left and right of the units' place; the second places to the left and right of units; the third places, etc.
- (6) Mark off the number into periods to the left and right from the units. Thus:



If instead of writing the point between the 9 and 8, it is placed over the 9, the units' place, to mark this place much of the trouble in connection with reading decimals would disappear.

From this it will be seen that the thousands' and the thousands' periods compy corresponding positions to the left and right of the unite' period. The same is true of the millions' and the millionths' periods, etc.

(7) Much practice should be given in reading numbers in all possible ways. Thus, 7:256 ulay be read as 7 and 256 thousandths; as 72 tenths and 56 thousandths; as 725 hundredths and 6 thousandths; as 7256 thousandths.

Teach this as follows:

7.256=7 units+2 tenths+5 hundredths+7 thousandths

$$=7+\frac{200+30+}{1000}$$

=7 and 256 thousandths.

Examples similar to the following should be given:-

- (1) Read 73.84 as a simple number; as a mixed number; as tenths; as tens; as hundredths.
- (2) Read 21.456 as a mixed number and give the value of each digit.
 - (3) Write 756 as ten-millions.

đ.

- (4) Write 756 as ten millionths.
- (5) How many figures are required to express 2145 hundred thousands?
- (6) How many figures are required to express 2145 hundred thousandthat
 - (7) Read 9 as units; as tenths; as hundredths; etc.
 - (8) Read 9 as units; as tens; as hundreds; etc.
- (9) Show that MAUGHTS affixed to a decimal have no effect on its value.

NOTE.—A common and convenient way of reading a decimal such as 7.200 is to say 7 point 2, 5, 6, or 7 decimal 2, 5, 6.

III. REDUCTION OF DECIMALS TO VULGAR FRACTIONS.

Ex. 1. Reduce .375 to a vulgar fraction in its lowest terms. .375=Ala=Ala=ii.

There will be no trouble with this if the notation and numeration of decimals have been properly taught. Appeals to these must be constantly made.

Thus, in example 1:

.275=2 tenths+7 hundredths+5 thousandths.

IV. ADDITION OF DECIMALS.

Introduce addition of Decimals by reviewing briefly:-

(a) Decimal notation.

(b) The fundamental principle of addition, vis., only numbers of the same unit can be added.

(e) How the addends must be written so as to bring noits of the same order under one another.

From this the pupils will see why the points are made to magunder one mother.

The addition follows as in addition of whole numbers.

Ex. 1. Find the sum of 4.8, 47.076, 26, .0007, 3.0000.

Place the addende on that units one under units, 47.876 tenthe under tenthe, etc. This is the case when the 26. points are in the same vertical line.

7 ten-thousandthe +0 ten-thousandthe=10 ten-91.7716 thousandthe=1 thousandth+6 ten-thousandths.

1 thousandth + 6 thousandths + 6 thousandths + 5 th 21 thousandths-7 hundfedths+1 thousandth, o

V. SUBTRACTION OF DECIMALS.

Whatever method of subtraction has been seed in whole numbers should be used in Subtraction of Decimals.

Fx. 1. From 17.3 take 12.876.

17.300 17.3 12.876 12.876 4.494 4,494

As in subtraction of integers, write units under units, tenths under tenths, hundredths under hundredthe, etc. As there are more figures in the subtrakend than in the missend, annex ciphers so as to make the number of decimal places in each the same. This will not affect the result. (Page 105.)

This expedient for making the antiquitien conier for a baginner should be gradually discontinued.

VE MULTIPLICATION OF DECIMALS.

Make use of multiplication of valgar fractions to infer the rule for Multiplication of Decimals. Take the following steps:-

(a) Multiply a decimal by a whole number.

Ex. 1. Multiply .7 by 9.

.7= A:

....7×9=-6×9=-11=6.8.

Br. 4. Multiply .077 by 7.

.err-rile:

(8) Multiply a mixed desimal by a whole number.

Ex. 3. Multiply 17.047 by 3.

17.847-17-MA-48841

... 17.847×2-444-43.511.

(c) Multiply a docimal by a docimal.

Ex. 4. Multiply .10 by 7.

.10=1/6 and .7=1/6; .'. .18K.7=1/6×1/6=1/46=.120.

Ex. 5. Multiply .0017 by .013.

1 obig == 270. ben wilder =: 7200.

(d) Multiply a mixed decimal by a decimal.

Ex. 6. Multiply 4.79 by .83.

4.79=11 and .80=14;

... 4.79×.88=111×14=11111=3.9787.

(e) Multiply a mined decimal by a mined decimal,

Ex. 7. Multiply 7.23 by 5.9.

7.13={id and 5.9={1:

7.18×6.0=116×19-11W-11.007.

By examining the products obtained in each case it will be seen that the figures of the product are obtained by regarding both multiplier and smalliplicand as whole numbers and multiplying in the neual way.

By comparing the number of decimal places in the product with that in the multiplier and multiplicand together, it will be seen that these are as many decimal places in the product as in the multiplier and multiplicand together.

Carried.—Avoid cancelling even if the figures would permit of it.

Norm.—The supil abould now be given practice in multiplying by 10, 160,

Br. Multiply 87.800 by 10, by 1000, by 100000.

87.500 10 07.500 1000 87509.000

100066 8756990,000

Hence, to multiply by a number expressed by 1 followed by manghie, move the decimal point as many places to the right in the multiplicand as there are naughts in the multiplier.

. This is done to prepare the pupil for making the divisor a whole number in division of decimals.

VII. DIVISION OF DECIMALS.

The difficulty in division of decimals arises from inability to put the decimal point in its proper place in the quotient.

Overcome this as follows:-

(1) Make the divisor a whole number.

(2) Put the point in the quotient as seen as the tenth's place of the dividend is used as a partial dividend.

Illustrate with care the principle upon which (1) is based, i.e., multiplying both divisor and dividend by the same number does not affect the quotient.

Thue 3)6 8)24 1 10)30

Or, multiplying the numerator and demoninator of a fraction by the same number does not alter the value of the fraction (page 153).

.. 1×1=1-8. 1×1=H=1, etc.

The divisor can always be made a whole number by it by a number especiated by 1 followed by as me there are decimal pinces in the divisor.

Stops in division of decimals :-

(a) Division of a mixed decimal by a whole number:

Rx. 1. Divide 42.3 by 5.

Birtie the whole number by 5. These are 2 5)02.3 12.46 ever; 2+.8=28 tenthe; 28 tenthe-5=4 tonthe and 3 tenths over; 5 tenths=30 hundredths; 30 hundredths+6= hundrodthe.

(b) Division of a decimal by a whole number.

Hx. 2. Divide .0236 by 8.

(e) Division of a decimal by a decimal.

$$=\frac{12.5}{25} + \frac{1250}{25} + \frac{125}{25} + \frac{1250000}{25}$$

Ex. 6. Divide 1.73646 by 456.7.

Morg. -Much practice chould be given in multiplying and dividing a decimal by 10, 100, 2000, etc., by morely moving the decimal point.

VIN. GOATRACTIONS IN MULTIPLICATION AND DIVISION OF DECIMALS.

When the number of desimal places given is large, and securety is not required beyond 4 or 5 places, the labor of multiplication and division may be avoided by a contraction of the ordinary process.

No. 1. Multiply 39,100005 by 1,4142136 correct to five doctmal

| Ordinary Form. | |
|--|--|
| 83.166245 | Contracted Form. |
| 1.4142136 | 38.100045 |
| | 6912414.1 |
| 1 96997479 | Control of the last of the las |
| 9 9406735 | |
| 33 166245 | |
| 663 32490 | 20000 |
| 13266 4989 | 18266 = 8016×4+3 |
| 33166 245 | $663 = 331 \times 2 + 1$ |
| 1326649 80 | 38 = 33×1 |
| 3316624.5 | $10 = 3 \times 3 + 1$ |
| 46.90415 47898320 | |
| TOTAL EL 0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (| 46.90415 |

To explain the contracted method, observe that multiplying any order by units gives that order as product, honor the units' figure of the multiplier is written under the place to be retained. The other figures of the multiplier are written in reverse order.

Now 2, a decimal of the fourth order, multiplied by 4, a decimal of the first order, gives a decimal of the fifth order; also, 6, a decimal of the third order, multiplied by 1, a decimal of the second order, gives a decimal of the fifth order; etc. The partial products are written with the right-hand figures in the same vertical line. This brings the same orders under one decimal.

Rx. 2. : Divide 6.275040 by 46.20073 correct to five pinces of decimals.

| Common Method.
46.20673)6.278340(.19667
4638573
1646770 0 | Contracted Method,
46.36573) 6.275949 (.18687
4628573
1646776 |
|--|--|
| 200204 10
200204 10
201428 65
26775 460 | 1888573
258306
331430 |
| 23142 865
3682 5856
3240 0011 | |

In the contracted method, offer the first figure of the quotient line been found to the need measure, and the first remainder obtained, instead of affixing a 8-or bringing-down the next figure, out off from the divisor the right-hand figure, and divide by the number-formed of the remaining figures. At each surrountre step in the division out-off another figure from the right of the divisor, and continue the division with the numbers formed of the remaining figures. It is, however, necessary to early from the rejected figures as in tanishplication.

IX. THE G.C.II. AND L.C.II. OF DECIMALS.

Mn. 1. Find the O.C.M. and L.C.M. of .35, 1.25 and .0025.

G.C.M. of Will, 1898 and Tilly to Teller, or

G.C.M. of .2500, 1.2500 and .0025 is .0025.

L.C.M. of 1866, 18880 and Table in 18688, or

L.O.M. of .2500, 1.2500 and .6025 is 1.2500, or 1.25.

Hence, to find the G.C.M. or L.C.M. of two or more decisials, reduce the decimals to equivalent ones of the same order and, disregarding the decimal point, find the G.C.M. or L.C.M. of the resulting numbers, and mark off the order by placing the decimal point.

X. REDUCTION OF VULGAR FRACTIONS TO DECIMALS.

It was shown on page 157 that a fraction indicates the division of the anmerator by the denominator, so in reducing a vulgar fraction to a decimal merely divide the numerator by the denominator by means of division of desimals.

Rr. 1. Beduce it to a decimal.

The pupils should be asked to read it as 7 divided by 20. 30)7.0(.35

the de of 7. 7=70 tenthe; is of 70 tenths is 00 3 touths and 10 tenths over. 100 100

10 touthe-100 hundredths and ye of 160 hun dredthe is 5 hundredthe. Hence, 1/100.25.

When pupils can readily seduce valgar fractions to decimals he following precess may be used:-

se viv to a deal

6)7.00(.000

Ex. 4. Reduce I to a decimal.

1=.0006 ... indefinitely.

Ex. 5. Reduce # to a decimal.

}=.7777 . . . indednitely.

Hx. 6. Reduce A to a decimal.

A=.121213 . . . indefinitely.

Ex. 7. Reduce # to a decimal.

$$t=\frac{8}{9\times3}=\frac{8\times10}{3\times3\times10}=t=.8833...$$
 indefinitely.

Ry. 8. Reduce if to a decimal.

$$7 = \frac{7}{3 \times 3 \times 3} = \frac{7 \times 10 \times 10}{3 \times 3 \times 3 \times 10 \times 10} = \frac{115}{15} = .56233 \dots indefinitely.$$

Ex. 9. Reduce of to a decimal.

$$3 = \frac{7}{9 \times 9 \times 9 \times 11} = \frac{7 \times 10 \times 10 \times 10}{9 \times 9 \times 9 \times 11 \times 10 \times 10 \times 10}$$

=_1116=.0796454 . . . indefinitely.

By comparing these nine examples, it will be observed:-

- (1) That when the fraction is in its lowest terms and the denominator has no factors other than 2 or 5, the decimal is finite and that there are as many places in the decimal as the greatest number of times 2 or 5 occurs as a factor in the denominator.
- (2) That valgar fractions in their lowest terms whose denominators contain no 2's or 5's as factors produce decimals which never terminate and that the figures repeat from the decimal point.
- (3) That vulgar fractions in their lowest terms whose denominators have 3's er 5's and other prime numbers as factors produce decimals of which parts do not repeat and parts repeat and that there are as many figures in the parts which do not repeat as the greatest number of times 2 or 5 occurs as a factor of the denominator.

Nors.—When a fraction in its lowest terms with a prime number for its denominator is reduced to a recurring decimal, the number of places in the period is either equal to one less than the denominator, or is a factor of the number of units in the denominator less one.

The first of these results arises from the fast that each remainder must be less than the denominator and, house, the number of remainders cannot be greater than one less than the denominator and whenever a remainder, the same as a provious one, comes the period will begin to repeat.

will have 6, 3, 2, or 1 piaces in the period; " 10, 5, 2, or 1 " " " 12, 6, 4, 8, 2, or 1 places in the period; 16, 8, 4, 2, or 1 44 46 11 18, 9, 6, 3, 2, or 1 places in the period, etc.

Hence, decimals fall into two great classes, viz.;-

- (a) Those which terminate. These are TERMINATING DECIMALS.
- (b) These which do not terminate. These are CIRCULATING DECIMALS.

Circulating Decimals fall into two cineses, viz.:-

- (1) These which begin to repeat from the decimal point. These are PURE CIRCULATING DECIMALS.
- (2) Those which do not begin to repeat immediately after the point.

These are MIEED CINCULATING DECIMALS.

Table of Decimals

dte

est

m-

leb

nt.

OFF

als 88

eat

Ebe bee Decimals. (a) Terminating. ((1) Pare. (b) Circulating. (2) Mized.

Exercises similar to the following should be given :-

- (1) What kind of decimal will be preduced by each of the
- (2) How many digits are there in the decimal arising from each of the following: A, t, th, th, th, the
 - (3) Reduce to, 18, 18 to decimals.
- (4) What kind of circulating decimals will the following prodece: - f. t. t. t. 181
- (5) How many figures are there in the finite parts of the befinale arising from \$5, Ms. 25, 127

M. CIRCULATING DECHALS.

(a) The Hatelless of Circulat

Reduce the fellowing to decimals;-1, t, i, i, t, t, A, t, Ht.

Blackbeard shows :-

| i=.5
i=.78 | t=.000
t=.565 | 1005 |
|---------------|------------------|---------------|
| 1415 | n=.0003 | ##89626414614 |

The tension should now explain that the Agures which mour are the repetends and show the means adopted to indicate a repetend, vis.; to put a det over the Agure that is repeated and if more than one, to put a det over the first and instiffment which are repeated.

| | | | | | White |
|-------|---|-----|---|-----------|-------|
| Thus, | , | 1-4 | 1 | Am. | 41 à |
| | | - | | eth jedi. | |
| | | | | 100 | 545 |
| | | | | 14000 | |

Points to be noticed are ;--

- (1) .6, .5, .66, .416, .316, and .30414 are circulating decimals.
- (2) 6, 5, 60, 6, 18, and 414 are the repetands, i.e., the figure or figures that are repeated.
- (8) That is, some eases the reputend begins at the decimal point, and in others there are one or more figures between the reputend and the point,
- (4) That the fermer are Punz Circulating Decimals and the latter are MIXED Circulating Decimals.
- (5) That a Pure Circulating Decimal consists of one part, the infinite part.
- (6) That a Mixed Circulating Decimal consists of two parts, a part which is not repeated; the finite-part, and the part which is repeated, the infinite-part.
- (i) Reduction of Pure Circulating Desirate to Velger Proctions.

 Two medic of precedure are in use :

From those and other examples it may be informed that a pure circulating decimal may be expressed as a sulper fraction by writing the figures which are repeated for the numerister of the fraction and placing for denominator as many 9's as there are figures in the repetend.

Norm.—It is semetimes objected that \hat{A}_i , \hat{M}_i , etc., are not desimals as defined, vis., fractions that have 10 or a power of 10 few denominators

This objection variables when it is remembered that when written as .5, or .25, the circulating desired parameters a sexu

(2) Beduce .7886 to a valgar fraction.

Let the valgar fraction 7200

.'. the valgar fraction # \$100.

(c) Reduction of Mined Circulating Decimals to Ve

Ex. 1. Reduce .25, .125, .125 and .01579 to equivalent vulgar

$$.36 = .31 - \frac{39}{10} - 11 - \frac{35 - 3}{90}.$$

$$.136 = .141 - \frac{141}{100} - 144 - \frac{135 - 1}{100}.$$

$$.136 = .131 - \frac{139}{100} - 144 - \frac{135 - 13}{100}.$$

$$.01576 = .01411 - \frac{1511}{1000} - \frac{1670 - 15}{10000}.$$

From these examples it will be readily seen that a Mirel Circulating Decimal is expressed as a sulgar fraction by subtracting the finite part of the decimal from the whole decimal and placing the remainder as numerator, and for the denominator planing as many b's as there are Aguree in the repetend, followed by as many siphere as there are figures in the finite part.

Ez. 2. Bednee Bissi to a valgar fraction.

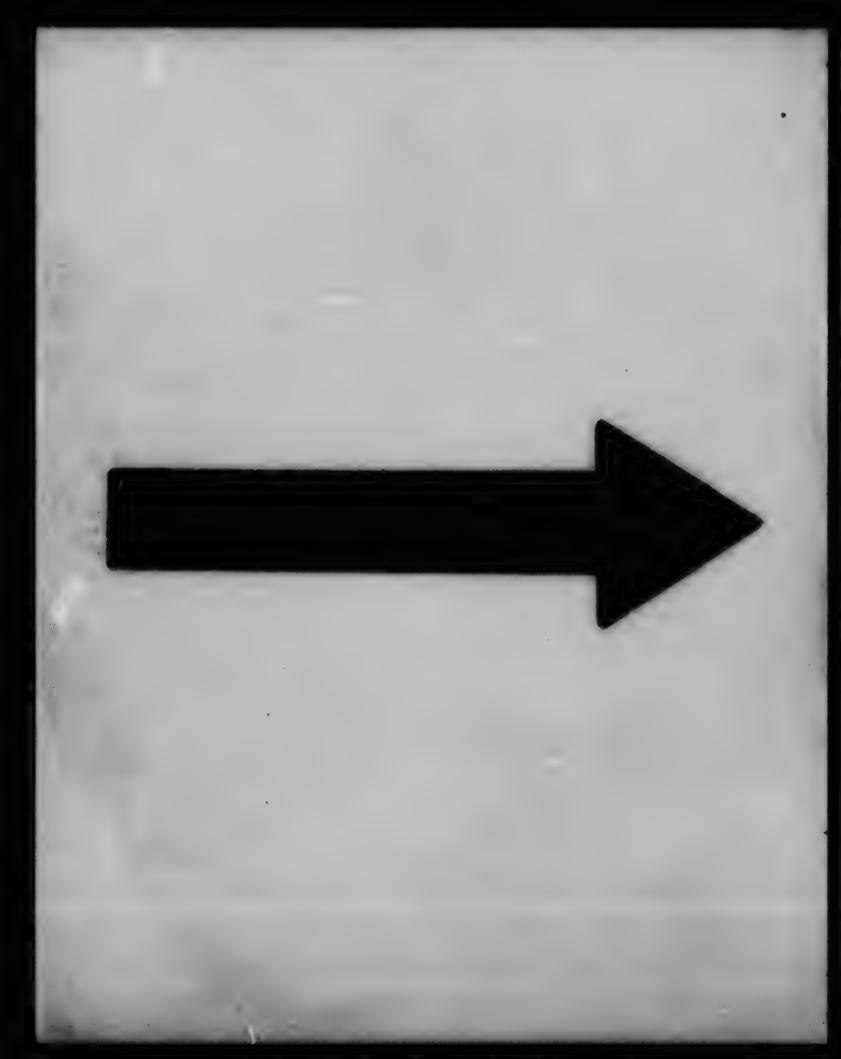
Let the velgar fraction ... 34257; 100000 times " 40 =34257.257 and 100 " 64 .". 99900 "

-1414 (4) Addition and Subtraction of Circulating D

Sufficient accuracy may, in general, be attained by extending the repetend a few places and adding or subtracting as in finite

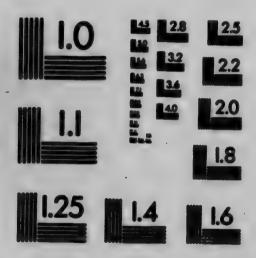
When perfect accuracy is required proceed as follows:-

(1) Make the decimals stattan, i.e., make them all begin to repeat at the same place to the right of the point.



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APPLIED IMAGE In

1853 East Main Street Rochester, New York 14809 USA (716) 482 - 0300 - Phone (716) 288 - 5000 - Fex This can be done as follows:-

(i) Regard a pure circulating decimal as a mixed one.

Thus. .3=.38=.333, etc.

(ii) Make a mixed circulating decimal begin to repeat at any place greater than the number in the finite part.

Thus, .23457=.234574=.2345745, etc.

Ex. 1. Add .3, .324, .2345 and .834567.

.3 = .3333

.324 = .32424

.2345 = .23454

.834567 = .834567

(2) Having made the decimals similar, next proceed to make them COTERMINOUS, i.e., make the repetends end at the same place to the right of the point.

This is done by finding the L.C.M. of the number of places in each repetend and repeating each repetend to that number of places.

Thus, the number of places in the repetends is 1, 2, 2, and 3.

L.C.M. of 1, 2, 2, and 3 is 6.

Thus. .3 = .333333333

324 = 324242424

.2345 = .234545454

.834567 = .834567567

1.726688779

The number to be carried to the right hand column is found by adding the first column of repeating figures, thus 5+5+2+3=15; earry 1.

Ex. 2. From 7.9845 take 5.7856387.

7.9845 = 7.984584 = 7.984584584584584

5.7856387=5.7856387=5.785638763876387

2.198945820708196

(e) Multiplication and Division of Circulating Decimals.

Sufficient accuracy can generally be secured by extending the repetends a few places and then multiplying or dividing as in ordinary decimals.

When perfect accuracy is required, the decimals must be reduced to their equivalent vulgar fractions and then these are multiplied or divided and the result is reduced to a circulating decimal.

XIL DECIMALS OF DENOMINATE NUMBERS.

1. To find the value of a decimal of a Denominate Number.

Ex. 1. Find the value of £.875.

Ex. 2. Express 2.375 bu. as a compound number.

2. To express a compound number as a decimal of a higher denomination.

Ex. 1. Reduce 4 cwt. 3 lb. 8 oz. to the decimal of a ton.

16)8 oz. 8 oz. =
$$\frac{1}{16}$$
 lb. = .5 lb.;
100)3.5 lb. ... 3 lb. 8 oz. = 3.5 lb.
20)4.035 ewt. 3 lb. 8 oz. = 4.035 ewt.;
4 cwt. 3 lb. 8 oz. = 4.035 ewt.;
4.035 ewt. = $\frac{4.035}{20}$ t. = .20175 t.

Ex. 2. Express £2 17s. 6d. as the decimal of £5.

Ex 3. Express # of 2 qr. 14 lb. as the decimal of 3 of 1 ton.

XIV. PERCENTAGE.

Present many problems as:-

- (1) A drover lost 7 out of every 100 sheep he had; how many sheep did he lose out of 900?
- (2) A merchant gained \$20 on every \$100 he had in business; how much did he gain on \$1200?
- (3) A company charges \$2 for every \$100 of insurance; how much would it charge for \$700?
- (4) A boy is absent from school 3 days out of every 100 school days; how many days is he absent in 200 school days?

Tell the class that the usual way of stating these problems is to say 7 per cent. instead of 7 out of every 100:

| 20 | 4.6. | :## : | 166 | ٠,٠,, | 920 44 | 7 | -44 | \$100 ; |
|----|------|-------|------|-------|--------|---|-----|------------------|
| 2 | 6.6 | 44 | - 46 | | 49 11 | | 56 | \$100;
\$100; |
| 3 | 66 | 46 . | ** | | 3 da. | | ** | 100 da. |

Thus it will be seen that per cent. (per centum) means FOR OR BY 100, and being a contraction is to be written with a period.

Explain that business men compute their gains and losses at so much per cent.

Also that the symbol % is used for the words per cent.

Ask many questions as 8 is what per cent. of 100?

8 ** ** ** ** ** 50 * 8 ** ** ** ** ** ** 200 ** 8 ** ** ** ** ** ** ** ** ** 25 **

What is 5% of 100? of 200? of 300? of 400?

11. THE RELATION OF PER CENT. TO DECIMALS.

(a) Much practice should be given in reading per cents. as decimals and expressing them as such.

Thus, 5% is read as 5 hundredths and is written .05.

25% ** ** ** ** 28 * ** ** ** ** ** .25.

Examples. Write as decimals the following:— 15%, 35%, 40%, 37½%, 5½%, 8½%, 150%, 112½%, 1½%.

(b) The converse of this should also be given, i.e., decimals should be expressed as per cents.

Thus, .25 is read 25 hundredths and is 25 %.

EXAMPLES. Read the following desimals as per cents.:

HL THE RELATION OF PER CENT. TO VULGAR FRACTIONS.

(a) Give practice in expressing per cont., first as decimals and then as common fractions, and finally change the per cents. to common fractions without having them read as decimals.

$$12\frac{1}{100} = \frac{12\frac{1}{100}}{100} = \frac{12\frac{$$

(b) Give practice in expressing vulgar fractions in their equivalent per cents.

The following shows the principle involved:-

Thus,
$$\frac{1}{4 \times 25} = \frac{1 \times 25}{4 \times 25} = \frac{100}{4 \times 25} = \frac{33}{4 \times 25} = \frac{33}{100} = \frac{33}{4 \times 25} = \frac{37}{100} = \frac{37}{4 \times 25} = \frac{37}{100} = \frac{37}{10$$

NOTE 1.—As the denominator of the fraction must be changed into 100, both terms of the fraction must be multiplied by the quotient arising from dividing 100 by the denominator of the vulgar fraction.

NOTE 2.—It will now be clear that per cent. can be expressed in four ways:—

874%=4.

01%= A.

- (1) By using the words per cent.
- " symbol %. (2) 5 " 188
- (9) ** a decimal fraction.

** a vulgar fraction.

IV. APPLICATION TO TYPE PROBLEMS.

There are three things involved in every example of per cent. Hence, there arise three cases as follows:—

Case i. To find any per cent. of a given quantity.

Case II. To find what per cent. one number is of another.

Case III. To find the quantity when some per cent. of it is given.

Case i. Ex. 1. A drover having 2500 sheep sold 43% of them. How many did he sell?

- (a) 43%=140
- 100 of 2500 sheep=1075 sheep.
- (b) Or, 43%=.43;

.48 of 2500 sheep=2500 sheep×.43=1075.00 sheep.

Case II. Ex. 2. A drover having 2500 sheep sold 1075 of them. What per cent. of his sheep did he sell?

- (a) No. sold from 2500 sheep=1075:
- .. " " 100 " =1011, or 43;
- .'. 43% of the sheep were sold.
- (b) Or, 1075 sheep is \(\frac{1275}{1275}\) of 2500 sheep; and \(\frac{1275}{1275}\) of 100 hundredths=43 hundredths=43 \%.

Case III. Ex. 3. A drover sold 1075 sheep; this was 43% of the number he had. How many had he at first?

43%= $\frac{48}{100}$; ... for of the number of sheep=1075; ... '' = $\frac{189}{17}$ of 1075 =100×25 =2500.

XV. APPLICATIONS OF PERCENTAGE.

NOTE.—The difficulty of applying percentage to commercial transactions lies in the pupil NOT COMPREHENDING THE NATURE OF THE BUSINESS INVOLVED. Hence, before problems are solved, MUCH CARE SHOULD BE GIVEN TO AN EXPLANATION OF THE TRANSACTION. This should be illustrated, as far as possible, by regular business forms, as catalogues, policies of insurance, application forms, interim receipts, etc. The more concrete the illustrations are, the better for the subject. Mere terms should not be taught. The topics involved should be discussed, explained, and illustrated.

These illustrations and explanations will remove the difficulties arising from the language of the problems. The pupils will be readily able to read them, i.e.,

picture the transactions and house will be easily able to make the relations that determine the calculations to be performed.

I. TRADE DISCOUNT.

L Explonation of Terms.

Manufacturers and wholesale dealers generally catalogue their goods at certain fixed prices. These are usually the retailers selling price.

The price is variously called the catalogue, list, gross, or invoice price.

A deduction is made from this price to enable the retailer of make his profit. If the catalogue fell into the hands of the purchaser, he would not think that the retailer was charging him too much for the goods. Whereas, if the net price were printed in the catalogue, the purchaser would naturally feel that he was being overcharged. Such a catalogue, also, enables the manufacturer or wholesale dealer to meet the fluctuations of the market by merely changing the rate of discount and thus the expense of printing a new catalogue is avoided.

Sometimes a second deduction is allowed off what remains after deducting the first one. This is to induce prompt payment by the purchaser.

At times a third deduction is made on certain kinds of goods, but this is a matter of special arrangement between buyer and seller.

These various deductions are known as TRADE OR COMMERCIAL DISCOUNT.

Trade Discount is always reckoned at a certain rate per cent. The first discount is deducted from the list price; the next one from what remains; etc.

The final result is not affected by the order in which the discounts are made. Thus, discounts of 40%, 10%, and 5% are the same as those of 10%, 5%, and 40%; or as those of 5%, 40%, and 10%; etc.

II. Application to Solution of Problems.

Case i. To find the discount having given the amount of the bill and the rates of discount.

Ex. 1. Find the discount off a bill of \$120, the rates of discount being 25%, 10%, and 5%.

Amount of bill=#120

Pirst discount at 26 % = 30

Second " "10 % = 9

####

Third " 5 % = 4.05

Not price #76.95

Total discount = \$(120 - 76.95) = \$43.05.

Case II. To find the bill having given the rates of discount and the net price.

Ex. 2. What was the bill for which \$114 was accepted as payment, the rates of discount being 60% and 5%?

Part of bill remaining after the first discount- Av of bill.

Second " =150 "
two discounts=Av "
Hence, for of the bill=\$114;

... " " = 100 of \$114

Or, part of bill remaining after the first discount for of bill;

" " second " = No of the of bill;

•• the bill= 100 of 100 of \$114 =\$200.

Case III. To find the rate of discount having given the bill and the net price.

Ex. 3. What is the rate of discount when a bill of \$375 is settled by a payment of \$250?

Amount of dissount=\$(375-250)=\$125. \$125 is iff of \$375:

... rate of discount=\ff=\frac{1}{2}.

Case IV. To find a single discount equivalent to two or

Ex. 4. What single discount is equivalent to discounts of 30% and 10%?

Part of bill remaining after first discount= $\frac{70}{100}$ of bill; Becount at $10\% = \frac{70}{100}$

... part of bill remaining after second discount = 100 to the second discount = (181 - 180) of bill= 100 to the second discount = (181 - 180) of b

=37%.

IL PROFIT AND LOSS.

In Profit and Lose there are four things to be considered;—

- (1) The cose prior, or the price at which the goods are bought.
- (2) The SELLING PRICE, or the price at which the goods are sold.
- (3) The difference between the cost price and the selling price which constitutes THE PROPER or THE LOSS according as the selling price exceeds or falls short of the cost price.

(4) The GAIN OR LOSS PER CENT.

The gain or loss per cent. is usually expressed as a certain per cent. of the cost price. When this is not the intention, care should be taken to express what is meant.

Before attempting to work problems, the pupil should acquire facility in expressing the selling price, and the gain or the loss, as a certain per cent. of the cost price. Inability to do this readily is a source of trouble in Profit and Loss.

Case i. Olven the cost price and the selling price to find the profit or the loss.

Ex. 1. A merchant bought goods for \$257 and sold them for \$310. Find his profit.

Case It. Given the cost price and the selling price to find the gain or less per cent.

Ex. 2. A merchant bought cloth at 5c. per yard and sold it at &. per yard. Find his gain per cent.

Case III. Given the cost price and the gain or less per cent, to find the selling price.

Ex. 3. A merchant bought sloth at 5c. a yard and sold it to gain 60%. Find the selling price.

Selling price=| | | of east price=| | | of 5e.= | | |

Case IV. Given the selling price and the gain or less per cent. to find the cost price.

Ex. 4. A morehant sold cloth at Sc. a yard and thereby gained 60%. Find the cost price.

Soiling price-iff of cost price; ... iff of cost price=80.;

" = | | of 8e. = 5e.

1. Explanations.

An Agent is a person employed to buy, or sell goods, collect accounts, and transact business for another.

M. COMMISSION.

The PRINCIPAL is then person for whom the business is transacted.

The Agent is variously spoken of as a Commission Menonant, Factor, Collector, Broker and Consigner.

When goods are sent to the agent to be sold, the goods are the Consignment; the person sending them is the Consignon; and the agent is the Consigner.

The Gross Processed of a sale or collection is the total amount received by the agent for the goods before deducting his commission and other charges.

The New Processes is what remains after all charges have been deducted.

At times the Agent is called a Broker, and the sum paid to him is known as Brokerage. The term, Commission, is used in some kinds of business, and Brokerage in others. When the Agent is placed in possession of the goods bought or sold, he is usually called a Commission Merchant; but, if the Agent contracts to buy or sell in the name of his Principal and is not put into possession of the goods, he is called a Broker.

The Commission or Brokerage depends upon the amount of the transaction and is stated at so much per cent. of the sum received for sales, expended for purchases, collected from debtors, etc.

NOTE.—It should be made clear that Commission is to be charged only on the money assually employed in the business transaction.

There are three things involved in Commission, viz., the sum involved in the business transaction, the RATE of commission and

These give rise to three cases similar to those of Percert go.

Care must, however, be taken with those problems in which the commission is to be deducted from a sum and the remainder invested.

Ex. 1. A sent his agent \$2255 with instructions to deduct his commission at 24% and invest the remainder in sugar. How much was invested in sugarf

Commission on \$100=#2#; .'. sum invested out of \$1021=\$100;

" " \$2255=\$2255×100

IV. INSURANCE.

Companies are organized to insure property of various kinds from loss by fire, water, wind, lightning, or other specified causes.

Insurance Companies are of two main classes, STOCK COMPANIES and MUTUAL COMPANIES.

A STOCK INSURANCE COMPANY is one in which the capital is owned by the members of the company, who are called STOCKholdens. These share the profits and are responsible for the losses, in proportion to the capital which each one owns.

IN A MUTUAL INSURANCE COMPANY the persons whose properties are insured become members of the company and give notes for the premium. Those notes are called PREMIUM NOTES and they render the makers liable for their proportionate shares of the salaries of the managers, expenses of the office, and possible losses. After these expenses are met, if there is any surplus it is returned to the members of the company pro rata.

There are various kinds of PROPERTY INSURANCE:-

(1) Fire Insurance, or indemnity for loss by fire.

(2) Marine Insurance, or indemnity for loss or damage of vessels or their cargoes by the accidents of navigation.

(3) Insurance of Live Stock, or indemnity for loss of horses, cattle, etc., by lightning, or other specified causes.

(4) Transit Insurance, or indemity for loss or damage to merchandise during transportation from one place to another.

(5) Accident Incurence, or indomnity for breakage of plate gless, etc.

Fire Insurance Companies usually insure property for only a nart of its value so that the person insured may be interested in

When a person wishes to effect an insurance, he makes application to a company, usually through an agent who supplies him with a blank form to be filled in and signed.

If the agent approves of the application, he gives the applicant an Isrance Ruchier for the promium paid. This binds the company until the policy is issued by the company or the application has been declined by it. In the latter case, the part of the premium proportionate to the unexpired time is returned.

When loss or damage occurs to the property, the insured fills in a CLAIM PAPER stating his loss. This is forwarded to the company. An inspector is sent to the place, who reports to the con any the extent of the loss.

If the property is completely destroyed, the sum insured is paid. If the loss is partial, the company agrees to pay the full value of the property destroyed, provided this does not exceed the sur1 mentioned in the policy.

A Com of Inc

There are three things involved in Insurance, viz., the sun for which the property is insured, the nars of insurance, and the

These give rise to three eases similar to those of Percentage and Commission.

To test the understanding of pupils, there is a fourth kind of problem given at times, viz., to determine for how much property of a certain value must be inserved so that the owner may receiver both the value of the property and the promises

Ex. 1. For what sum must a house worth #3950 be insured at 12% so that in case it is totally destroyed the owner may sustain

A policy of \$100 will pay for \$12 premium and \$982 of property. Honce, sum for which property worth \$98\$ is insured=\$100;

V. TAXES.

1. Explorellane.

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The affairs of Canada are carried on by means of the Dominion, Provincial, and Municipal Governments, or authorities. Money is needed to enable these parties to discharge their duties. The money raised for such purposes is a Tax.

When the tax is paid directly by the person who is to bear the burden, it is a DIRECT TAX and is called a TAX.

When the tax is paid by a person who expects to indemnify himself by charging it to another, the tax is an INDIRECT TAX and is called a DUTY.

Illustrate the use made of the money collected by reference to the cost of making roads, lighting streets, building bridges, creeting and maintaining municipal buildings, paying firemen, policemen, municipal officers as the township clerk, assessor, collector, etc.

For purposes of direct taxation property is regarded as REAL or PERSONAL.

REAL PROPERTY, OR REAL ESTATE, consists of fixed property, as lands and houses.

PERSONAL PROPERTY consists of movable property, as each, stocks of banks and companies, merchandise, cattle, income, etc.

Officers called Assessors or Assessment Commissioners are appointed by the township, town, and city council to estimate the value of all the taxable property in the municipality.

The report which the Assessor makes to the Council is known as the Assessment Roll. On it he has entered the name, address, estimated value of property (real and personal) of each resident of the municipality.

When the municipal authorities know how much taxable property there is in the municipality and also what the expenses for the year will be, the RATE OF TAXATION is found by dividing the sum to be raised by the measure of the value of all the property to be taxed. The quotient is the tax on the dollar and is usually expressed in mills, or thousandths of a dollar.

When the tax on the dollar is known, the sum to be paid by each rate-payer is then computed. This sum is collected by a person called the COLLECTOR, appointed by the municipal council.

2. Ceses of Direct Taxes.

In direct taxation three things are involved, (1) the ASSESSED VALUE of the property which is taxed, (2) the RATE, and (3) the AMOUNT of the tax.

Case i. Given the assessed value of the property and the rate, to find the tax.

Ex. 1. Find the tax on property assessed for \$5400 at 151 mills on the dollar.

Tax on \$1 =\$.0155; ... " \$5400=\$(5400×.0155)=\$83.70.

Case II. Given the assessed value of the property and the amount of the tax, to find the rate.

Ex. 2. What is the rate of taxation when \$56 is the tax upon property assessed for \$3500?

Tax on \$3500=\$56:

·. " " 1 =0.160=\$.016.

... the rate is 16 mills on the dollar.

Case III. Given the amount of the tax and the rate, to find the assessed value of the property.

Ex. 3. What is the assessed value of property on which the tax is \$31.25 at 121 mills on the dollar.

Value of property when \$.0125 is the tax=\$1;

3. INDIRECT TAXES are of two kinds, CUSTOMS DUTIES and EXCISE DUTIES.

All goods entering Canada from foreign countries are required by law to be landed at certain places called Ports of Extry.

At each port of entry the Dominion Government has an establishment, called a Custon House, with one or more officers attached to it, called Custon House Officers. These officers inspect the goods, examine the invoices, collect the duties, etc.

AM INVOICE is a statement detailing the kind and quality of the articles shipped or sent to a purchaser or agent with their weight or amount, and the cost of each article. Invoices are made out in the currency, and weights and measures of the country from which the importation is made.

Customs Taxes or Duties produce a revenue for the support of the Government and also serve to pretect home industries.

Certain articles such as spirituous or mait liquors, eigars, snuff, etc., manufactured in Canada are required by law to pay duty. This is an Excess DUTY.

At each place where these are manufactured, there are one or more Government officials, called Excise Officers, who check the quantities manufactured, see that none are disposed of without

Duties, whether Customs or Excise, may be of two kinds, AD VALOREM and SPECIFIC.

The rate of duty and its kind is stated in the TARIFF which is a schedule of goods and the rate of duty imposed by law upon

4. Cases of Indirect Taxes.

In Indirect Taxation three things are involved:—(1) The VALUE of the goods, (2) the RATE of duty, (3) the AMOUNT of the duty.

The three cases arising from finding one of these when the other two are given are similar to those of Percentage.

The following is suggested as headings for teaching this subject:-

TAXATION.

(a) Direct.

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- (b) Indirect.
 - (a) Direct Taxes, called Taxes.
 - (1) By whom levied.
 - (2) On what levied.
 - (3) For what purposes levied.
 - (4) Basis of reckoning—the rate on the dollar and the method of obtaining this rate.
 - (5) Assessor, Assessment and Collector.
 - (6) Problems.
 - (b) Indirect Taxes, called Duties.
 - (1) Customs Duties.
 - (2) Excise Duties.
 - (3) By whom levied.
 - (4) How, when, where collected.
- (5) By whom paid.
- (6) The Tariff, Ad Valorem, and Specific Duties.
- (7) Problems.

VL. INTEREST.

MOTE 1.—Some arithmetics introduce Stocks before Interest, but as transactions in Stocks are difficult for one unacquainted with the subject, it is believed advisable to postpone their consideration until Interest has been studied.

NOTE 2.—Since a new element, time, enters into the calculations in Interest, it is necessary to give more attention to this application of Percentage than to some of the others.

1. Explanations.

Illustrate Interest by ealling attention to what is paid when a house is hired at a livery, when a house or farm is rented, when a man's labor is employed.

Make clear that the money paid is for the USE of the horse, or the house, or the farm, or the labor.

Point out that the rent varies with the value of the house and the time it is rented.

Apply this to money:-

Instead of getting the use of a house, one who gets the use of money pays for this use in proportion to the sum borrowed and the time he has its use.

Introduce the terms, Principal and Interest.

Money loaned to another is called PRINCIPAL.

The sum paid for its use is the INTEREST.

Money employed by a person in his own business is called CAPITAL.

Interest is computed at a certain RATE PER CENT. per annum.

At this stage give many mental examples in finding the interest.

Introduce the term, Amount, by means of an example, as:—A borrowed \$200 from B for a year at 8% per annum. How much must A pay B at the end of the year?

Make clear how the \$216 is made up, and give the term, Amount.

The AMOUNT consists of the Principal (which is constant) and the Interest (which varies with the Principal, Rate, and Time).

When Interest is paid on the Principal only, it is called SIMPLE INTEREST.

When the Interest remains unpaid after it falls due, it is sometimes added to the Principal and the Interest for the second period is computed on this increased Principal. This is known as Compound INTEREST.

In computing interest for ‡ yr., ‡ yr., ‡ yr., etc., it is usual to reckon a certain rate per cent. per annum, as equivalent to ‡, ‡, etc., this rate for the period specified.

Thus, 8% per annum is regarded as equivalent to 4% each † yr., 21% each † yr., or 2% each † yr.

This is, however, not strictly accurate.

Thus, the interest on \$100 at 8% for 1 yr. is \$8; at 4% per i yr. it is \$8.16.

2. Cases of Interest.

Case I. Given the Principal, the Rate per cent. and the Time, to find the Interest or Amount.

Ex. 1. What is the interest on \$350 for 21 yr. at 6% per annum?

Interest on \$1 for 1 yr. =\$\frac{1}{100};

'' \$1 '' 2\frac{1}{2} yr.=\(2\frac{1}{2}\times\tau_{100}\);

'' \$350 '' 2\frac{1}{2} yr.=\(350\times2\frac{1}{2}\times_{100}\)

=\(52.50.\)

Or, Interest for 1 yr. =\(\frac{1}{100}\) of \$350;

'' 2\frac{1}{2}\times_{100}\) of \$350
=\(52.50.\)

Case II. Given the Principal, Interest or Amount and Time, to find the Rate per cent.

Ex. 2. At what rate per cent. must \$350 be put out at interest for 2½ yr. to yield \$52.50?

Interest on \$350 for 2½ yr.=\$52.50;

'' \$350 '' 1 yr. = 0 \$52.50;

'' \$100 '' 1 yr. = 0 \$52.50;

=\$6;

... rate=6%.

Or, Interest for 2½ yr.=\$52.50;

'' 1 yr. = 6 of \$52.50=\$21;

the interest is \$10 of the Principal.

\$10 of Principal=\$10 of Principal;

the rate is 6%.

Case III. Given the Principal, Interest or Amount and the Rate per cent., to find the Time.

Ex. 3. In what time will the interest on \$350 at 6% per annum be \$52.50?

The interest on \$350 for 1 yr. at 6% is \$21.

Time for which \$21 is the interest on \$350=1 yr.;

... " " \$52.50 " " \$350=
$$\frac{52.50}{21}$$
 of 1 yr. =2\frac{1}{21} yr.

Case IV. (a) Given the interest, Rate per cent. and Time, to find the Principal.

Ex. 4. What Principal will give \$52.50 interest at 6% per annum in 21 yr.?

(b) Given the Amount, Rate per cent. and Time, to find the Principal.

Ex. 5. What Principal will amount to \$402.50 at 6 per cent. per annum in 21 yr. f

The interest on \$100 at 6% for $2\frac{1}{2}$ yr.=\$15; ... principal which amounts to \$115 for $2\frac{1}{2}$ yr.=\$100; ... " \$402.50 " $2\frac{1}{2}$ yr.=\$ $\left(\frac{402.50\times100}{115}\right)$

VII. COMPOUND INTEREST.

In Compound Interest the interest as it falls due at the end of a stated period is added to the principal and this sum becomes the principal for the next period; at the end of this second period the interest on the new principal is added on and the amount forms a new principal for the next period; etc.

When the interest is added at the end of each year, it is said to be compounded annually; when added at the end of each half year, it is compounded half-yearly; when added at the end of each three months, it is compounded quarterly, etc.

Case I. Given the Principal, Rate per cent. and the Time, to find the Compound Interest or Amount.

Ex. 1. A man deposited \$2500 in a savings bank, the interest being compounded half-yearly at 4%. (a) How much was at his

eredit at the end of 18 months? and (b) how much of this is

```
Original principal=$2500;
Interest for 1st period=2% of $2500
Principal " 2nd "
                                        = 850:
                     =$2550:
Interest " 2nd
                     =2% of $2550
Principal " 3rd
                 6.6
                    =$2601:
Interest " 3rd
                 4.6
                    =2% of $2601
                                         852.02;
Amount at his credit =$2653.02;
             Internst=$(2653.02-2500)=$153.02.
```

Pupils should see clearly why the interest for the second period is larger than that for the first and by how much; why the interest for the third period is larger than that for the second and by how

Examples in compound interest should be regarded as a series of examples in simple interest until the pupil becomes familiar with the subject. Then a shorter method should be introduced.

Thus, at 2% for a period, the amount of any sum at the end of a period is 188 of the sum.

Hence,

Amount of \$1 at end of 1st period=188 of \$1

```
=Principal for next period.
44
                    44 2nd
                                 = 100 of (100 of $1)=(100) of $1
                                 =Principal for next period.
                    " 3rd
                                =188 of [(188)* of $1)]
                                =(188)2 of $1;
     " $2500" " " 3rd
44
                                =$[2500×(\frac{188}{88})*] =$2653.02;
             Compound Interest=$(2658.02-2500)=$153.02.
```

By similar reasoning it may be shown that the amount of \$1 at compound interest for any number of periods is found by finding the amount of \$1 at the given rate per cent. for one period and then raising the measure of this amount to the power indicated by the number of periods. Thus, the amount of \$1 at interest, compounded quarterly at 6% per annum in 15 mos. is \$(1.015)*.

Case II. Given the Amount, Rate per cent. and Time, to find the Principal.

Ex. 2. What sum will amount to \$1378.42 in 11 yr. at 5%, interest being compounded half-yearlyf

Amount of \$1 for 3 periods=\$(1.025)2; Principal which amounts to \$(1.025) == \$1;

" \$1378.42 =
$$\frac{1378.42 \times 1}{(1.025)^8}$$
 = \$1280.

MOTE.—The other cases of Compound Interest are too difficult for this stage of progress of the pupil.

VHI. TRUE AND BANK DISCOUNTS.

If A owes \$212 to B, the money to be paid in 1 yr., it would be fair for A to pay \$200 to B at the beginning of the year, money being worth 6% per annum, for B would have the use of the \$200 for the year. B by accepting the smaller sum would lose nothing.

\$200 is called the PRESENT WORTH of the debt.

\$12 is called the TRUE DISCOUNT; being mathematically exact, it is sometimes called MATHEMATICAL DISCOUNT.

The PRESENT WORTH, of a debt at TRUE DISCOUNT is the Principal which will amount to the debt at the time it falls due at the given rate per cent.

TRUE, OR MATHEMATICAL DISCOUNT is the interest on the Present Worth for the given rate and time.

This kind of discount, the finding of which is often treated as a separate rule, is really the case of Interest in which the Amount, Rate per cent. and Time are given, to find the Principal or Interest.

Ex. 1. What is the debt on which the Mathematical Discount for 6 mo. at 8% is \$3?

This is the same as finding what principal will give 48 interest in 6 mo. at 8%. This is readily found to be \$75. Hence the debt

Ex. 2. If \$25 is the interest on \$325 for a given time and rate, what should be the mathematical discount off \$325 for the same time and rate!

The interest on \$325 for the given time and rate=\$25; " discount off \$350 " 66 66 66 66 " =\$25; 11 : 11 gggg 11 325×25 350 =\$2314.

Ex. 3. If \$5 is allowed off a bill of \$105 due 6 mo. hence, what should be the bill from which the same sum is allowed as 12 mo. discount?

\$5 is the discount off \$105 for 6 mo.;

- .'. \$5 " " interest on \$100 " 6 mo.;
- .'. 45 " " " 650 " 12 mo.;
- .'. \$5 " " discount off \$55 " 12 mo.

If a borrower binds himself by a note or bill to pay \$100 in 6 mo. and a banker or other money lender advances money on the security of the note or bill at 8% per annum, he will give to the borrower \$96. The difference, \$4, is known as Bank Discount.

In making such a transaction clear, the business practice must be specially emphasized. In doing this, the regular forms used in business should be introduced for illustrative purposes. Business transactions should be clearly outlined and carefully earried through.

In addition to what is said under the head of Bank Discount in the Public School Arithmetic, notice the following:—

The value of a note at maturity is the face of the note, i.e., the sum for which it is given, if it does not bear interest; and it is the face plus the accrued interest at maturity, if it draws interest.

COMMERCIAL PAPER embraces noise, checks, drafts, bills of exchange, letters of credit, etc.

The Maker of a note is the one primarily liable but each endorser is liable to succeeding holders if the maker fails in payment.

When the PAYEE writes only his name across the back of the note it is a BLANK ENDORSEMENT.

If he writes above his signature, Pay to A. B., or order, it is a FULL ENDORSEMENT, and A. B. would have to endorse it before receiving payment.

If it is made payable to A. B. only, then it is a RESTRICTIVE ENDORSEMENT.

A QUALIFIED ENDORSEMENT is one in which the endorser does not wish to render himself liable for payment and then he writes "Without recourse to me" above his name.

A Protest is a declaration made in writing by a Notary Public, giving legal notice to both the maker and the endorser of a note of its non-payment.

A BANK CHEQUE is a written order on a banker or broker to pay money in his keeping belonging to the signer.

A BILL OF EXCHANGE is a written order, addressed to a person in a distant place called the drawes to pay a specified sum of

money to a third person called the payee or to the order of the payee.

Bills of Exchange are of two kinds, vis., (1) Inland Bills of Exchange, or Drafts, and (2) Foreign Bills of Exchange.

An INLAND BILL OF EXCHANGE is one in which the drawer and drawer reside in the same country.

This is usually called a DRAFT.

There are various kinds of Drafts, as Demand drafts, payable on presentation; dight drafts, payable after three days of grace; Time drafts, payable at a certain time after the date of the draft, or after presentation for acceptance.

After the Drawes agrees to pay it and writes "secepted" with his signature and the date, across the face of it, he becomes the Asseptor.

A FORHIGE BILL OF EXCHANGE is one in which the Drawer and Drawer reside in different countries.

A LETTER OF CREDIT is a letter or notification issued to persona travelling and addressed by a banker to his agent, informing him that the person named therein is entitled to draw a certain sum of money; when addressed to several agents on whom the money can be drawn in sums to suit the convenience of the traveller, it is called a CIRCULAR LETTER OF CREDIT.

2. Comparison of True and Bank Discounts.

Bank Dissount is equal to the interest on the value of the note at maturity.

True Discount is the interest on the sum which will amount to the value of the note at maturity.

Bank Discount is, hence, greater than True Discount by the interest on the True Discount.

3. Cases of Bank Discount.

Case I. Given the note, date of discount and rate of discount, to find the Bank Discount.

Three months after date, I promise to pay to the order of James Jones, six hur red and forty-four 100 dollars with interest at 8% per annum, value received.

JOHN BROWN.

This note was discounted at the Imperial Bank at 7% on May 1st.

Find (1) the bank discount and (2) the net proceeds on May 1st. On July 20, the day of maturity, the note is worth \$657. Number of days between May 1st and July 20 is 80. Bank Disseunt on \$667 for 80 days at 7% per annum

-M of riv of \$667, or \$10.08. Net proceeds=#(607-10.08)=#646.93.

Case II. Given the value of the note at meturity, the net proceeds of the note or the discount and the terms of lacount, to find the rate per cent.

Ex. 2. At maturity, a note is worth \$5621; the disegunt is \$41.58 and the term of discount 45 da. Find the rate per cent.

Interest on \$5621 for 46 da. =\$41.58;

" #5621 " 365 da.=
$$\frac{365 \times 41.58}{45}$$
;

" rate= $\frac{100 \times 365 \times 41.58}{5621 \times 45}$ =6%.

Case III. Given the note, the net proceeds or the Bank Discount and the rate of discount, to find the term of discount.

Ex. 3. At maturity, a note is worth \$116.80. It is discounted at the Imperial Bank at 74% and produces \$115.48. Find the term of discount.

Interest on \$116.80 for term required=\$(116.80-115.48)=\$1.32; " \$116.80 " 1 yr. at 71% =\$8.76; \$8.76 is the interest for 365 da.;

.'. term of discount is 55 da.

From this example it is evident that this is merely a modification of Case III of Simple Interest.

Case IV. Given the net proceeds, the rate of discount and the term of discount, to find the value of the note at maturity.

Ex. 4. Find the value of a note at maturity which will realize \$637 when discounted 4 mo. before maturity at 6%.

Interest on maturity-value of note for 4 mo. at 6%=150 of value; Net proceeds of note=14 " .. 1st of maturity-value=\$687; .'. maturity-value=100 of \$637 =6650.

EL STOCKS AND DIVIDENDS.

I. Esphysition

In addition to the explanations given in the Public School Arithmetic on pages 140 and 150 notice the following:—

The chief causes affecting the prices of stocks are:

(i) The risk of loss owing to the company or government becoming bankrupt.

(ii) The rate of dividend which is paid and the certainty that

it will continue.

(iii) The time at which the dividends are due. Prices are higher when the dividends are seen due and usually drop after they have been paid.

(iv) The prospect of a future increase or decrease in the dividends.

(v) The amount of the Rest, or Reserve.

Companies usually receive a part of their earnings, instead of paying them all in dividends, to enable them to meet unforcemen losses, etc. This is called the REST, OR RESERVE. When the accumulated Rest is large it adds to the value of the Stock.

Bonds bearing a fixed rate of interest, such as Consols, also fluctuate in price but not to the same extent. This fluctuation is due to the variation in the price of money. When money is plentiful and hence cheap, such bonds will increase in price; when money is scarce and hence dear, they will decrease in price.

DESERVORES are bonds or securities given as asknowledgment of debts, bearing fixed rates of interest, and providing for the repayment of the principal at a specified time.

PREFERENCE, OR PREFEREND STOCK is stock bearing a fixed rate of interest which must be paid before a dividend can be paid on ORDINARY, OR DEFERRED STOCK.

WATERED STOCK is stock which has been issued to stockholders in addition to what they own and for which no payment has been made or is required.

When the Charter of the company forbids the declaring of a dividend exceeding a certain rate per cent. of the par value of the stock or when the company wishes to keep the public in ignorance of its prosperity, its capital stock is increased by issuing additional shares to its present stockholders so that a low rate of dividend on the increased stock will produce as much income as a high rate upon the original capital stock. Stock so increased is said to be watered.

Groce BROKERS are persons who deal in stocks, debentures, etc. When a stock broker buys or sells stocks for a principal he charges a commission on the per value of the stock. This is termed Brokerage. The rate varies according to circumstances.

Problems involving Brokerage often cause difficulty to a beginner because of his inability to know when the brokerage is added to, or subtracted from, the market price. When the nature of the transaction is understood this difficulty disappears. Thus, when stock is purchased for a person, the brokerage must increase its cost to him; on the contrary, when stock is sold for him, the brokerage must diminish what he receives for it.

To buy one share (\$100) of Commercial Cable at 172 75, brokerage \$\frac{1}{2}\$, the purchaser must pay \$173.25 to the person for whom the stock is bought and \$.25 to the broker; hence, \$\frac{1}{2}\$ of C. C. stock will cost him \$172.50.

To sell one share of C. C. stock at the price quoted, the broker would receive \$172.25 for it. He would keep \$.25 for his brokerage and the seller would receive \$172 for the \$100 C. C. stock.

"Bears" are stock brokers who contract to sell stock at a certain price at a certain time. They therefore operate to deprese the market, buy, and then deliver the stock, thus realizing a profit.

⁴⁴Bulls' are stock brokers who endeavor to raise the price of stock in order to sell to advantage.

To "sell short" is to contrast to deliver stock at a fixed price within a fixed time, when the seller has not the stock on hand. Hence, the "Shorts" are the "Bears."

To "buy long" is to contract to purchase stock, deliverable at a stipulated time. The "Longs" are the "Bulls."

2. Cases of Stocks.

The following things are involved in problems in Stocks:—
(1) the PRICE of stock, (2) the QUANTITY of stock, (3) the AMOUNT of money invested, (4) the RATE of dividend, (5) the INCOME, (6) RATE PER CENT. of income.

Case i. Given the amount of stock and its price, to find its money value.

Ex. 1. What is \$650 stock of the Dominion Bank worth at 245? Value of \$100 stock=\$245:

.. " " \$650 " = | | of \$245=\$1592.50.

Case II. Given the sum invested in stock and its price, to find the amount of stock.

Ex. 2. How much stock of the Bank of Ottawn at 207 can be

Stock bought for \$207 of money=\$100;

Case III. Given the quantity of stock and the sum invested, to find the price of the stock.

Ex. 3. How is Bank of Mantroal stock queted when \$600 stock seems \$20567

Value of \$800 stock=\$2050;
... " ** \$100 " =\$****=\$257;
... B. of M. stock is quoted at 257.

Norn.—When a pupil understands these cases, they should be sewerhed with brokerage included.

Case IV. Given the sum invested and the price of the stock, or the amount of the stock, and the rate of dividend, to find the income.

Ex. 4. What annual income is derived from investing \$2040 in a 7‡ per cent. stock at 127‡?

Income from \$100 stock =\$7\$;
'' '' \$127\$ mency=\$7\$;
'' '' \$2040 '' = 2040 of \$7\$=\$120.

Ex. 5. A owns \$5200 in a stock which pays a dividend of 5%. What is A's income?

A's income=18, of \$5200=\$260.

Case V. Given the amount of stock and the income, to find the rate of dividend paid.

Ex. 6. A who owns \$5600 stock receives \$238 as the halfyearly dividend. What is the half-yearly rate of dividend?

\$5000 stock gives \$258 income;

... \$100 " page ", or \$42; ... the half-yearly rate of dividend is 42%.

Case VI. Given the Income and the rule of dividend, to find the amount of stock,

Ex. 7. A receives \$14 each quarter from a stock paying 11% quarterly dividends. How much of this stock does he own?

The of stock owned-#14:

.'. " " mage of \$14-\$800.

Case VII. Given the price of stock and the rate of dividend, to find the rate of interest made.

HE. S. A invests in Bank of Commerce stock at 150. This stock pays a yearly dividend of 7%. What rate of interest does he make on his investment?

Income from \$150-\$7;

æ

" \$100-111 of \$7-\$41;

.'. rate of interest-44 % .

Case VIII. Given the rate of interest made and the rate of dividend paid, to find the price of the stock.

Ex. 9. By investing in a stock paying 8 per cent., A makes 7 per cent, on his money. What was the price of this stock?

\$7 is the income from investing \$100;

86 f of \$100, or \$114#;

.'. the stock was bought at 114f.

Case IX. Given the price of the stock and the rate of fividend, to find what sum must be invested to produce a fixed

Ex. 10. What sum must be invested in the Dominion 34 per cents, at 97# so as to produce an income of \$1400?

Since \$3.50 is the income from investing \$97‡;

.". \$1400 ** ** of 407%, or 430000.

X. EQUATION OF PAYMENTS, OR AVERAGE OF ACCOUNTS.

Sometimes one person owes another several sums, due at different dates, and he desires to pay all in one sum at such a time that neither person may lose or gain by the transaction.

Thus, suppose A owes B \$200, of which \$100 is due in 6 mo. and \$100 in 12 mo. When might the whole be paid in one sum so that neither A nor B would gain?

Examining this, it becomes evident that if A deferred payment until the last sum is due that he would then owe B \$200 and the interest on \$100 for 6 mo.

Again, if he paid the whole sum when the first payment is due, it is clear that he would lose the interest on \$100 for 6 mo.

It thus becomes clear that he must pay the whole at such a time that the interest gained by deferring the first payment may balance the interest lost by pre-paying the second payment. Thus the payment would be made in 9 mo.

Again, suppose on Jan. 1st, 1901, A owes B \$1800, of which \$300 is payable in 4 mo.; \$700 in 6 mo.; and \$800 in 18 mo. When might A pay the whole to B without loss or gain to either person?

Examining this as in the last example it will soon become clear that the equitable time of payment is such a time that the interest on the sum whose payment is deferred will be equal to the interest on the sum whose payment is pre-paid.

To enable pupils to find this time, they should be given practice with such mental examples as the following:—

- (1) In what time will the use of \$1 balance the use of \$8 for 1 mo.? of \$3 for 2 mo.? of \$8 for 4 mo.? etc.
- (2) In what time will the use of \$1 balance the use of \$2 for 3 mo., and of \$5 for 4 mo.? etc.
- (3) How long should \$4 be kept in use to balance the use of \$1 for 4 mo. 7 of \$6 for 2 mo. 7 of \$8 for 6 mo. 7 etc.
- (4) How long will it require \$8 to balance the use of \$5 for 3 mo, and of \$3 for 7 mo.7 etc

The example can now be worked as follows:---

The use of \$300 for 4 mo. = the use of \$1 for 1200 mo.

" " " \$700 " 6 " = " " \$1 " 4200 " " " " \$1 " 14400 "

" " " 1800 " ; " = " " " 19800 "

Number of mo. = 19806 = 11.

It should be shown that 11 mo. is correct.

A has the use of \$300 for 7 mo. and of \$700 for 5 mo., but he loses the use of \$800 for 7 mo.

The use of \$300 for 7 mo. = the use of \$1 for 2100 mo.

These two deferred payments= " " \$1 " 5600 "

=A's gain or B's loss.

The use of \$800 for 7 mo.=the use of \$1 for 5600 mo. =A's loss or B's gain.

This method of solution is based on the assumption that what is gained by the debtor by deferring certain payments after they are due is lost by him by paying other sums before they become due. This is not strictly correct, for what he gains is the interest on the deferred payments and what he losse is the interest on the present worth of the anticipated payments. The error is, however, so small that it is the method used in ordinary business

The following is a convenient way of indicating the work:-

 $300 \times 4 = 1200$ $700 \times 6 = 4200$ 800×18=14400 19800

XVI. PARTNERSHIP.

1. Explor

When a number of persons unite to carry on some particular branch of business, the connection so formed is called a PARTMER-

The persons forming a partnership are called unitedly, a COMPANY, FIRM, or HOUSE. Thus there are Railroad Companies, Manufacturing Firms, Wholesale Houses, etc. Usually merchants and manufacturers are known as Firms or Houses.

The persons forming the Partnership are called separately, the PARTHERS.

The money or property invested by each is called his Grook or

It is usual to make an agreement among the partners to share the gains or losses is proportion to the capital contributed by each.

Property of all kinds belonging to the firm and all debts due to it are the RESOURCES, EFFECTS, or ASSETS of the firm.

The debts owed by the firm are the LIABILITIES.

The NET CAPITAL is the excess of resources over liabilities.

The NET INSOLVENCY is the excess of liabilities over resources.

The NET GAIN is the excess of the total gains over the total losses within the period under consideration.

The NET Loss is the excess of the total losses over the total gains within the period under consideration.

The term, "Limited," placed after the name of a firm means that the responsibility of the partners for the liabilities of the

company does not extend beyond the amount of capital each has in the firm. The law requires the word, "Limited," to be placed after the name of the firm whenever its name is used.

In the case of shareholders in banks, to secure bill holders and depositors, the law makes the liability of stockholders double the amount of the capital held by them. Thus, the owner of five paid-up shares of one hundred dollars each would be liable, in case of the bank's failure, to be called upon to pay \$500 as well as lose the money already invested. This is known as Double Liability.

When the several shares of capital have been in the business for the same length of time, the division of the gains or losses is called Simple Partnership, or PARTMERSHIP WITHOUT TIME.

When the several shares of capital have been invested for different lengths of time and the gains or losses are to be divided according to the average investments, i.e., in proportion to the several capitals and the times for which they have been employed, the division of the gains or losses is called Compound Parthership or Parthership with Time.

2. Simple Partnership.

Simple Partnership is merely an application of Case II of Sharing. See page 144.

There are three things to be considered, (1) the CAPITAL of the firm, (2) the CAPITAL of each partner, and (3) the GAIN OR LOSS to be shared.

Case I. Given the capital of each partner and the gain or loss, to find each partner's share of the gain or loss.

Ex. 1. A and B formed a partnership. A invested \$9000; B, \$7000. They gained \$4200. What share of the gain should each get?

\$9000 7000

2000 41-

\$16000, the whole capital.

Sum gained by \$16000=\$4200;

Case II. Given the total capital and the share of each partner of the gain or loss, to find the capital each invested.

Ex. 2. A, B, and C formed a partnership. Their total capital was \$29000. A received \$246 of the gain; B, \$314; and C, \$440. Find the capital of each.

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$(246+314+440)=$1000;
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A's capital=1846 of \$29000=\$ 7134.

= Ald of \$29000=\$ 9106.

C'a =14% of \$29000=\$12700.

nd Partnership or Partnership with Time.

Three things are to be considered, (1) the CAPITAL of each partner, (2) the TIME the capital of each partner is employed in the business, and (3) the GAIN OR LOSS to be shared.

It is plain that each partner's share will depend upon two things:-

First, the amount of his capital.

Second, the length of time it is continued in the business

It is evident that when the times are equal, the gain or loss must be shared in proportion to their capitals; when the capitals are equal the gain or loss must be shared in proportion to the times; and when neither the times nor the capitals are equal it must be shared as their product.

Ex. 3. A commenced business with a capital of \$6000; 3 mo. after he took in B with a capital of \$4000; and 4 mo. after this he took in C with a capital of \$1200. At the end of the year the firm had gained \$5175. Find the share of each partner.

```
Gain on $8000 for 12 mm = gain on $96000 for 1 mo.
```

11 90000 11 9 11 = 11 11 906000 11 1 11

es 60000 es 2 es = es . es \$6000 es 1 es Capital = " 138000 " 1 "

Gain on \$130000 for 1 mo. =\$5175;

.. " " \$96000 " 1 " = 1% of \$6175=\$3600=A's share.

and " " \$36000 " 1 " = 1 of \$5175=\$1350=B's " \$6000 " 1 " =rfs of \$5175=\$225 =C's "

The following is a convenient way of indicating the work:—

 $8000 \times 12 = 96000$

4000× 9 = 36000

 $1200 \times 5 = 6000$ 138000

A's share=15 of \$5176=\$3600.

B's " = 1 of \$5175=\$1350.

" = The of \$5175=\$225.

XVII. INVOLUTION AND EVOLUTION.

Steen.

1. Teach Power.

In doing this emphasize the number of factors in the power.

The definition of power is often inaccurately expressed as the number of times the number is multiplied by itself. The third power is not obtained by multiplying a number by itself twice but by multiplying the square of the number by the number; the fourth power is not obtained by multiplying a number by itself three times but by multiplying the square by the number to obtain its sube and this cube by the number to obtain its fourth power.

2. Teach Exponent or Index.

- (a) Have a number of factors indicated as powers.
- (b) Have powers expanded into factors.
- 2. Halse numbers to the powers indicated by the expensal.
- (a) Begin by squaring (1) whole numbers, (2) decimals, (3) vulgar fractions.

NOTE 1.—Call attention to a convenient way of squaring a mixed number with 2 as the fractional part. Thus,

2.—Show how to square a number of two figures. Thus,

- (b) Proceed to higher powers with (1) whole numbers, (2) decimals, (3) vulgar fractions.
- 4. Have pupils learn the following:-
 - (a) The squares of all the numbers from 1 to 12 inclusive.
- (5) The squares of any number of tens up to 10 tens. Thus, 90° , 30° , 40° , 50° , etc.
 - (c) Squares of frequent occurrence as 15°, 16°, 25°, etc.

Norn.—The second power of a number is called its square, because the product of the number of units in the length of a square by itself is equal to the number of units of area of the square.

2.—The third power of a number is called its cube, because the continued product of the number of units in the three equal sides of a cube gives the number of units in its cubic content,

3.—The square of a whole number is called a perfect square.

4. The cube of a whole number is called a perject cube.

IL SQUARE ROOT.

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ts

Review Involution in so far as it applies to the squares of whole numbers.

sing of Square Root and how it is indicated.

Take the squares up to \$1 and resolve each into two equal

Explain that 2 is the square root of 4; 3 is the square root of 9; etc.

Explain also that there are two ways of indicating the square root of a number, (1, \circ y using the radical sign \checkmark , and (2) by

Thus,
$$\sqrt{4}=2$$
; $\sqrt{9}=3$; $\sqrt{16}=4$; Or, $4^{\frac{1}{2}}=2$; $9^{\frac{1}{2}}=3$; $16^{\frac{1}{2}}=4$.

Fix the meaning by drilling on such mental examples as, find the square root of 36, 64, 81, 18, 82, 28, 18, 180, etc.

3. To accertain how many figures there will be in the square reet of a

Examine the following:-Since, 1'=1 and 9'=81;

... the square of a number of 1 digit is a number of 1 or 2 digita.

Conversely, the square root of a number of 1 or 2 figures is a number of 1 digit.

Again, since 10°=100 and 90°=9601;

.'. the square of a number of 2 figures is a number of 8 or 4

Conversely, the square root of a number of 3 or 4 figures is a number of 2 figures.

Again, since 100°=10000 and 999°=998001;

... the square of a number of 3 figures is a number of 5 or 6 ngures.

Conversely, the square root of a number of 5 or 6 figures is a number of 3 figures; etc.

Honce, to ascertain how many figures there will be in the square root of a-given number, divide the number into periods of

two figures each and there will be as many figures in the square root as there are periods or part of a period.

4. To analyze Perfort Squares.

From these examples, it is evident that the square of a number is equal to the square of the tens+twice the product of the tens by the units+the square of the units, or is equal to the square of the tens+the product of twice the tens plus the units by the units.

5. To find a number from its square.

Ex. 1. Find the square root of 1849.

| | Formal Method | | | |
|-----------------|-----------------|--|--|--|
| 1849(40+3 | 1849(48 | | | |
| 40*=1600 | 16 | | | |
| (2×40+3)3= 249 | 83 240 | | | |
| | 249 | | | |
| Square root=43. | Square root=43. | | | |

Since the square of tens is hundreds, the part of 1849 expressed by 49 contains no part of the square of tens. These figures are, therefore, disregarded for the present. The greatest square in 18 hundred is 16 hundred, the square root of which is 4 tens.

The remainder 249 equals twice the tens plus the units, multiplied by the units. Twice the tens is 8 tens; 8 tens is contained in 24 tens, 8 times.

Twice the tens plus the units is 83, and 83 multiplied by 3 is 249.

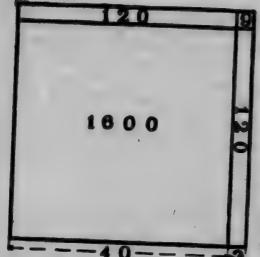
Another method of explaining square root is often given:-

Ex. 2. A has 1849 square disks and wishes to arrange them into a large square. How many disks will there be in each side of the square?

First, he ascertains that there will be between 40 and 50 disks in the side of the square.

Next he arranges a square with 40 disks in the side and places 1600 of them in position. He has still 249 to arrange.

To preserve the square already formed he must add disks equally to two sides as shown in the diagram.



One row along the two sides would take twice forty (2×40) disks.

To assertain how many rows he can place he divides so into 249 and finds he can place 2 rows along each of the two sides. He still has 9 disks which are needed to fill in the small square.

The formal solution is the same as that given above under Example 1.

Ex. 3. Extract the square root of 481686.

| The source of a signate root of 4 | 81686. | |
|---|----------|-----------------------|
| $600^{2} = \frac{481636(600 + 90 + 4)}{360000}$ | | 481636(694 |
| $(2\times600+90)90 = \frac{121696}{116100}$ | 129 | 1216
1161 |
| $(2 \times 690 + 4)4 = 5636$ | 1384 | 5536 |
| The square root=694. | The squa | 5536
Pro root=604. |

Since the square of hundreds is ten-thousands, the part of 481636 expressed by 1636 contains no part of the square of the hundreds. These figures are, therefore, disregarded for the present.

For the reason given under Ex. 1, the figures 36 are disregarded in finding the tens' figure.

Hence, when the number of figures in the square root of a number is known, it is at once evident what part of it must be considered in finding the left-hand digit of the root; what part must be considered in finding the next figure; etc.

Hence, the steps in the extraction of Square Root are:-

- (1) Divide the number into periods of two figures each beginning at the decimal point.
- (2) Find the largest square contained in the left-hand period. Place the square root of this number as the left-hand figure of the root. Subtract its square from the left-hand period and annex the next period to the remainder.

(3) Double the part of the rest found, place it to the left of the remainder, and using it as a trial divisor divide the remainder, omitting the last figure, by it. The quotient is the next figure of the rest and must be annexed to the trial divisor as well as to the root. Multiply the divisor, completed as it now stands, by the quotient. Place the product under the remainder and subtract. To the new remainder annex the next period.

(4) Proceed as in (8) to find the next figure of the root.

6. To extract the square root of a decimal.

Since the square of a number of tenths is a number of hundredths; and the square of a number of hundredths is a number of ten-thousandths; and the square of a number of thousandths is a number of millionths; etc., i.e., are decimals of 2nd, 4th, 6th, etc., orders, respectively, hence to find the square root of a decimal it must be of the 2nd, 4th, 6th... order, i.e., there must be 2 figures in each period counting from the point.

Ex.-4. Extract the square root of .4225.

.4225(.65 even, point off the decimal places is even, point off the decimal into periods of two figures each, counting from the point and extract the square root as in whole numbers, placing the point in the root as soon as the left-hand period is dealt with.

Ex. 4. Extract the square root of .4.

7. To entract the square root of a valger fraction.

(a) If both terms are exact squares, extract the square root of each. The result will be the terms of the root. Thus, $\sqrt{\frac{2}{16}} = \frac{2}{16}$;

(b) If both terms are not exact squares, reduce the fraction to a decimal and extract the square root of the decimal. Thus, $\sqrt{1-1}$. $\sqrt{1-1}$. $\sqrt{1-1}$. $\sqrt{1-1}$.

8. Applications of Theory.

(1) To find the square root of a number by resolving it into prime factors.

. (2) To find by what factor a number must be multiplied to make it a perfect square.

(3) To find what number must be subtracted from a number which is not a perfect square, so that the remainder may be a

(4) To find what number must be added to a number which is not a perfect square, so that the sum may be a perfect square.

(5) To find the fourth root of a number.

9. Procifed Apollegis

(1) To find the side of a square, when the area is given.

(2) To find the sides of a rectangle, when the relation between the sides, and the area are given.

(3) To find the radius of a circle, when the area is given.

(4) To find one side of a right-angled triangle when the other two are given.

(5) To find the corresponding dimensions of similar surfaces, when their areas and the dimensions of one are given.

IIII. CUBE ROOT.

Here.

L Introducti

Review Involution in so far as it applies to the cubes of whole numbers.

2. Teach the meening of Cube Root and how it is indicated.

Take the perfect cubes up to 729 and resolve each into three equal factors, as,

Explain that 2 is the cube root of 8; 3 is the cube root of 27; etc. Explain also that there are two ways of indicating the cube root of a number, (1) by placing of before the number, and (2) by

3. To ascertain how many figures there will be in the cube root of a

.'. the cube of a number of 1 digit is a number of 1, 2, or 3 digits.

Conversely, the cube root of a number of 1, 2, or 3 digits in a number of 1 digit.

Again, since 100-1000 and 900-970200;

.'. the cube of a number of 2 figures is one of 4, 5, or 6 figures. Conversely, the cube root of a number of 4, 5 or 6 figures is a number of 2 figures.

Again, since 100°=1000000 and 900°=907002000, therefore, the cube of a number of 3 figures is a number of 7, 8 or 9 figures; conversely, the cube root of a number of 7, 8 or 9 figures is a number of 3 figures, etc.

Hence, to assertain how many places there will be in the cube root of a given number, divide the number into periods of three figures each and there will be as many places in the cube root as there are periods and part of a period.

4. To analyze perfect cubes.

85°-614125:

$$\begin{array}{c} 15 \\ -25 \\$$

By treating other numbers in a similar way it will be evident that a perfect cube having 4, 5, or 6 places consists of tene³+3×tene³×units+3×tene×units³+units³.

5. To find a number from its cube.

Ex. 1. Find the cube root of 614125.

Trial divisor
$$3 \times 80^{2} = 19200$$
 $3 \times 80 \times 5 = 1200$
 $5^{2} = 25$

$$20425 \times 5 = 102125$$

The greatest cube in 614 thousand in 512 thousand, the sube rect of which is 5 tens.

The remainder 102125 is the product of two factors. One of those is largely made up of the term $3\times80^{\circ}$. The other factor is found by using $3\times80^{\circ}$ as a trial divisor.

Many devices of arrangement have been adopted in indicating the operation of obtaining the cube root of a number of more than one period; but all involve the principle as developed above.

The formal method.

| | | 614125 | | | |
|----|---|---------------|---------------|--|--|
| 24 | 5 | 19300
1225 | 512
102125 | | |
| | | 20435 | 102135 | | |

Ex. 2. Find the cube root of 14706125.

.

60 51

.

| | 14/700/125 | | | | |
|---------------|---------------------------|--|--|--|--|
| 1200 | 0706 | | | | |
| 1456 | 5894 | | | | |
| 1728 | 863125 | | | | |
| 361
176425 | 862125 | | | | |
| | 1200
256
1456
16 | | | | |

The number is separated into 8 periods.

The greatest cube in the left hand period is 8. Set down 2 its cube root and subtract 8 from 16 and to the remainder 6 annex. 706, the next period.

Then set down three times 3, which is 6, and three times the square of 2, which is 12 and annex two eyphers to it.

Then 6706 is divided by 1200. On trial 5 is found to be too large so 4 is set down under 2 and midway between 6 and 1200.

Then 6 and 4 are regarded as 64 and multiplied by 4. The product, 256, is added to 1200; the result, 1456, is multiplied by 4 and the product subtracted from 6706; and to the remainder the last period, 125, is annexed.

Next set down three times 24 and three times the square of 24 which is 1728.

MOTE.—This last result can be obtained by placing 16 the square of 4, the second figure of the root under the divisor and adding together the three numbers coupled by the brace.

Two syphons are then annexed to 1738 and the last figure of the root 5 is found by dividing 802135 by 173000. Then the divisor is completed by adding 5 times 735 to 172000.

6. To entract the cube root of a Business.

Since the cube of a number of tenths is a number of themsendths; and the cube of a number of hundredths is a number of millionths; and the cube of a number of thousandths is a number of billionths; etc., i.e., are decimals of the 3rd, 6th, 9th, etc., orders, respectively, hence to find the cube root of a docimal it must be of the 3rd, 6th, 9th . . . order, i.e., there must be three figures in each period counting from the point.

Ex. 3. Find the cabe rect of .008.

Ex. 4. Find the cube root of .079607.

Ex. S. Find the cube rect of .S.

| | 100 00 .5. | .800 000 017 000 |
|--------|-------------------------------------|-------------------|
| 27 1 | 94200
544 3 | 720
71000 |
| 276 a | 21844 } | 49008
21312000 |
| | 2561844 | 20100752 |
| 2784 3 | 256355200 | 831340000 |
| • | 200430729 | 775816187 |
| 2786 3 | 2561844
64
356356200
83629 | 8313400 |

Bonce #.8-.9283 ...

7. To extract the cabe root of a Valuar Fraction.

- (a) If both terms are exact subset, extract the subs root of, each. The results will be the serresponding terms of the substruction.
- (b) If both terms are not exact cubes, reduce the fraction to a decimal and extract the cube root of the resulting decimal.
- 4. To find the cube root of a perfect cube consisting of 4, 5, or 6 floures by inspection.

The tens' digit is readily found.

| | unito' | digit | lo | found | from | the | follo | wing: | - | |
|------|--------|-------|-----|--------|------|-----|-------|-------|----|------------|
| 86 B | | | | 3 10 0 | | - | - | - | | |
| | | | | | | | ** | ** | ** | |
| | | ••• | ** | 2 44 | ** | ** | ** | 0.0 | 40 | |
| 68 | ** | ** | 66 | 4 44 . | 18 3 | 66. | * ** | " . I | 44 | 7 |
| | ** | 0# | 66 | 8 44 | 11 | | 46 | | 44 | |
| 06 | ** | # | | | 46 | 86 | ** | | 66 | |
| 66 . | ** | 44- | 66 | 7 " | 66 2 | 44 | 60 | | | 8; |
| • | 4 | 66 | ** | A 46 | 4.6 | .44 | 44 | | ** | =; |
| ** | 44 | ** | 6.6 | 0 " | ** | 86 | 44 | ** | 66 | <u>a</u> ; |

Honce, when the last digit of the cube is 1 the units figure is 1;

44 44 A 44 44 88 -3; etc.

Thus, \$ 12836-24; \$ 661472-86; \$ 100023-47.

& Applications of Theory,

(1) To find the cube root of a number by receiving it into prime factors.

(2) To find what number must be subtracted from a number which is not a perfect cube so that the remainder may be a perfoot cabe.

(3) To find what number must be added to a number which is not a porfect cube, so that the sum may be a perfect cube.

(4) To find the sixth root of a number.

10. Proctical Apails

(1) To find the side of a cube, when its cubic content is given.

(2) To find the radius of a sphere, when the cubic content is given.

(3) To find the dimensions of a body, when the cubic content and dimensions of a similar one are given.

XVIII. MENSURATION.

I, THE RECTANGLE AND SQUARE.

See pages 135 and 141.

IL THE PARALLELOGRAM.

Draw parallelograms. Have pupils draw others of various sizes and shapes.

Show that the area depends upon (1) the length or width, and (2) the perpendicular distance between the parallel sides.

th of a side and the perpendi en this side and the opposite one, to find the area.



Show by figures similar to A B C D that every parallelogram may be changed into a rectangle whose length is that of the parallelogram and whose breadth is the perpendicular width, or altitude of the parallelogram. These two measurements are the

dimensions of the parallelogram.

A good test of the pupil's comprehension, is for the teacher to draw a parallelogram and give the length of a certain side, and then to require the pupil to point out the other dimension which must be given to enable the area to be found.

Case II. Given the area and one dimension, to find the other dimension of the parallelogram.

III. THE TRIANGLE.

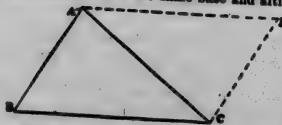
This is treated under the Restangle, page 141.

1. The Definition.

Steps.

(a) Draw and have drawn various kinds of triangles.

(b) Show that the area of a triangle is always half the area of a parallelogram of the same base and altitude.



(c) Draw triangles and give the length of one of the sides, have pupils draw the figure showing the other dimension to enable the area to be determined.

Case I. Given the length of a side and the perpendicular from the opposite angle on that side or that side produced, to find the area of the triongle.

In teaching this Case, the following order is suggested:-

(a) Right angled triangles.

(b) Acute "

(c) Obtuse "

. If it is made clear that the triangle is half the area of a parallelogram of the same base and altitude, there will be no difficulty with this Case.

Case II. Given the area and one dimension of the triangle to find the other.

All that is necessary is to convert the triangle into r parallelogram and this becomes Case II of the parallelogram.

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IV. TRAPEZOID.

1. Teach the meaning by drawing trapezoids and comparing and comtreating them with parallelograms, rectangles and squ

Have pupils take rulers and draw trapezoids of certain dimensions, as draw a trapezoid the parallel sides being 2 in. and 3 in. long respectively, and the distance between them, 2; in.

Case i. Given the length of the two parallel sides of a trapezoid, and the distance between them, to find the area.

The simplest way to teach this is to draw a diagonal dividing the trapesoid into two triangles of which the length of the bases and the perpendicular heights are given.

The area can be readily found.

Another way is to take half the sum of the areas of two rectangles one being on the longer side and the other on the shorter side of the trapezoid; each being of the same altitude as the trapezoid.

Ex. 1. Find the area of a trapezoid the parallel sides of which are 25 in. and 15 in. in length and the perpendicular distance between them 1 ft.

Area of one triangle
$$=\frac{25\times12}{2}$$
 eq. in. =150 eq. in.;

Area of the other triangle=
$$\frac{15\times12}{2}$$
 sq. in. =90 sq. in.;

Or area of both triangles
$$=\frac{40\times12}{2}$$
 sq. in. $=240$ sq. in.

Case II. Given the area and the sum of the two parallel aides, to find the perpendicular distance between them.

Ex. 2. The area of a garden with two parallel sides which measure 25 ft. and 17 ft., respectively, is 567 sq. ft. What is the perpendicular distance between the parallel sides?

Since
$$\frac{35\times p}{2}$$
, $\frac{17\times p}{2}$ —567;
 $p = \frac{2\times 567}{42} = 27$;

. . perpendicular height=27 ft.

Steps.

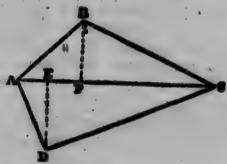
V. THE TRAPEZIUM.

1. Teach the modeling by drawing trapeziums and compare and contract them with trapezzido, parallelograms, rectangles, and equires. Notice that the trapezium is the simplest four-cided figure to define.

Cose i. Given the length of a diagonal and the length of the perpendiculars let fall upon this diagonal from the opposite angles, to find the area of the trapezium.

Show that the diagonal divides the trapezium into two triangles. Have pupils point out the measurements necessary to enable their areas to be found.

Ex. 1. A B C D is a trapezium. A C is 46 yd. long; B F and D E are respectively 17 yd. and 19 yd. long. Find the area of the trapezium.



Area of triangle A B $C=\frac{48\times17}{2}$ sq. yd.=408 sq. yd.

..
$$\triangle$$
 D C= $\frac{48\times19}{2}$ sq. yd.=456 sq. yd.

. area of A B C D=(408+456) sq. yd.=864 sq. yd.

Or, area of A B C D=
$$\left(\frac{48\times17}{2} + \frac{48\times19}{2}\right)$$
 sq. yd. =\frac{48\times36}{2} \text{ sq. yd.}=\frac{48\times36}{2} \text{ sq. yd.}=\frac{864}{2} \text{ sq. yd.}

Case II. Given the area and either the length of the diagonal, to find the sum of the lengths of the perpendiculars, or the sum of the lengths of the perpendiculars, to find the length of the diagonal.

Ex. 2. The diagonal of a trapezium measuring 1 aere is 88 yd. long. Find the sum of the lengths of the perpendiculars upon this diagonal from the opposite angles.

Area of trapezium=
$$\frac{88 \times \text{sum of p's}}{2} = 4840 \text{ sq. yd.};$$
... sum of p's=
$$\frac{2 \times 4840}{88} \text{ yd.} = 110 \text{ yd.}$$

VI. THE CIRCLE.

1. Teach Circle, Centre, Circumference, Diameter, Red

In teaching circle make clear that it is a surface, not a ring, mor a ball.

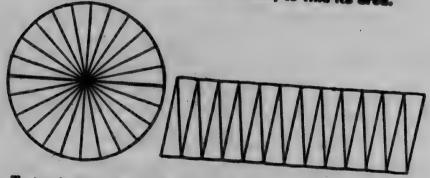
Have pupils describe circles, using a string for radius rather than a pair of compasses.

2. Teach the relation between the diameter of a circle and its circum-

This can be done approximately by comparing the lengths of the diameter and circumference of two or three cylinders.

- 3. Fix this relation by having many applications of it as fellows:-
 - (a) Given the diameter of the circle, to find its circumference.
 - (b) Given the circumference of a circle, to find its diameter.
 - (c) Given the radius of a circle, to find its circumference.
 - (d) Given the circumference of a circle, to find the radius.

Case I. Given the radius of a circle, to find its area.



To teach this, out a circle about 10 in. in diameter out of a piece of leather and mark it into an even number of triangles-24 is a convenient number—as shown in the figure. Then with a sharp knife cut the triangles almost to the circumference leaving a slight margin to connect the triangles. Now separate the circle into semi-circles and fit the triangles together as shown in the

diagram. The more numerous the triangles are, the more nearly the figure will approximate a rectangle.

The length of the rectangle is evidently half the circumference of the circle and its breadth is half the diameter, or radius.

Hence, the number of units of area is found by multiplying the number of corresponding units in naif the circumference by the number in the radius.

Hence, area=
$$\frac{1}{2} e \times r = \frac{2\pi r}{2} \times r = \pi r^3$$
.

Norn.—When other dimensions are given, as the diameter, or the circumference, it is better to express these in terms of the radius, rather than to teach a new way of finding the area of the circle.

Case II. Given the area, to find the radius.

Ex. 1. The area of a circle is 3850 sq. in.; find its radius. Since, $4 \times r^2 = 3850$:

Hence, radius=35 in.

Case III. To find the Area of an Angelos.

Ex. 2. A road runs round a circular shrubbery; the diameter of the shrubbery is 478 ft. and the width of the road is 19 ft.; find the area of the road.

```
Radius of shrubbery=41s ft. =239 ft.;

Radius of road and shrubbery=(239+19) ft.=258 ft.;

Area of large circle=(42×258s) sq. ft.;

"" small " =(42×239s) sq. ft.;

"" area of road=[42×(258s-239s)] sq. ft.

=[42×(258+239, (258-239)] sq. ft.

=(42×497×19) sq. ft.=29678 sq. ft.
```

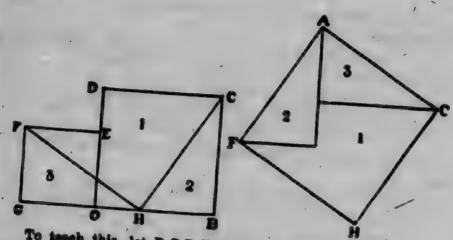
WIL THE MIGHT-ANGLED TRIANGLE.

Steps.

1. Teach the definition and the names of the sides.

Do this by drawing right-angled triangles of various sizes and shapes and give names to the sides. Then have pupils draw others and name the sides.

 Teach that the square on the hypothenuse is equal to the sum of the squares on the base and perpendicular of a right-angled triangle.



To teach this, let BCDEFG be a figure composed of two squares placed side by side. Take B H equal to G O and join F H and C.H. Cut the whole figure out of cardboard and then divide it into three pieces. Fit the pieces together as in the figure A F H C. A single square is thus obtained equal to the sum of the two squares. BCH is a right-angled triangle. BCDO is the square on the side B C; G O E F is equal to the square described on B H; and H C A P is the square on the hypothenuce. Hence, the truth of the proposition becomes evident.

Pupils should be asked to ent similar figures for themselves.

The following is suggested, have pupils draw right-angled triangles of the following dimensions:-

Sides containing the right-angle 3 in. and 4 in., or 5 in. and 13 in., or 7 in. and 24 in., or 8 in. and 15 in.

Then, by actually measuring, they should discover that the hypothenuse is 5 in., 13 in., 25 in., and 17 in., respectively.

They should then compare the sum of the squares on the two shorter sides with that on the hypothenuse.

Morn.—It is destruble that pupils should not be confronted with mechanical pulties of calculation at this stage. The following formule will enable the teacher to use such examples as will give perfect squares.

- (1) $(a^2+b^2)^2=(a^2-b^2)^2+(2ab)^2$.
- (2) $(2n^2+2n+1)^2=(2n^2+2n)^2+(2n+1)^2$.

In the first let a=7 and b=5, then

 $(7^2+5^2)^2=(7^2-5^2)^2+(2\times7\times5)^2$, or

74, 34, and 70 are the sides of the right-angled triangle.

Case I. Given the base and perpendicular, to find the hypothenuse.

Ex. 1. Find the hypothenuse of a right-angled triangle whose base and perpendicular are 40 in. and 42 in. respectively.

(The measure of the hypothenuse) ==40°+42°;

... the measure of the hypothenuse= $\sqrt{(40^{\circ}+42^{\circ})}=58$; ... length of hypothenuse=56 in.

Case II. Given the hypothenuse and one side, to find the other side.

Ex. 2. The hypothenuse of a right-angled triangle is 73 in. long and the base is 55 in. long; find the length of the perpendicular.

(The measure of the perpendicular) =73°-55°:

- .*. the measure of the perpendicular= $\sqrt{(73^{\circ}-55^{\circ})}=48$;
 - .'. the length of the perpendicular=48 in.

Case III. Given any two sides of a right-angled triangle to find the length of the perpendicular from the right angle upon the hypothemuse.

Ex. 2. The base and perpendicular of a right-angled triangle are respectively, 55 in. and 48 in.; find the length of the perpendicular from the right-angle upon the hypothenuse.

Length of hypothenuse= $\sqrt{(55^{\circ}+48^{\circ})}$ in.=73 in.

Twise the area of the triangle= (55×48) eq. in.; Also, "" " = $(n\times78)$ eq. in.

 $'' = (p \times 78) \text{ eq. in.};$ $p \times 78 = 55 \times 48:$

 $p = \frac{55 \times 48}{73} = 3611$;

Length of perpendicular=36+1 in.

VIII. SIMILAR BURFACES.

Steps.

1. Teach the Definition.

By drawings show that similar surfaces must be of the same shape. Thus, circles, squares, and equilateral triangles are similar. Show that when they are rectilineal they are (1) equiangular and (2) have the sides about the equal angles proportional.

Illustrate this by drawing many parallelograms and rectangles, of the same shape but of different sizes.

2. Show that the areas of similar surfaces are to one another as the squeres of the measures of corresponding lines of the purface.

Do this by drawing similar figures and comparing their areas. Thus, compare the areas of two circles 1 in. and 2 in. in radius respectively.

The first=3+ sq. in.; the second=12+ sq. in.

The areas are as 1 to 4, or as 1° to 2°.

Compare the areas of two circles 3 in. and 4 in. in radius.

Area of first=(9×3) sq. in.; area of second=(16×3) sq. in. Areas are as 9 to 16, or as 3° to 4°.

Compare the area of a rectangle 6 in. by 5 in. with another twice as long and wide.

Show by a diagram that the latter can be divided into 4 rectangles, each of which is equal to the fermer.

Hence, the areas are as 1 to 4 or as 12 to 22.

Ex. 1. A map is constructed on the scale of is in. to a mile. What area on this map will represent a lake 4000 acres in area? 1 mile is represented by 1 inches;

.', 1 sq. mi. is represented by res sq. in.;

4000 sq. mi. is represented by (4000 × 180) sq. in., or by 18

Ex. 2. A water pipe i in. in diameter will fill a eistern in 20 min. How long a time will be required to fill it when there is a discharge pipe in. in diameter opened at the same time.

The diameters are as i to i, or as 8 to 2;

.'. the areas of the openings in the pipes are as 9 to 4.

The area of a pipe that would fill the eistern as fast as the two would be represented by 9-4, or 5.

A pipe whose area is represented by 9 fills eistern in 20 min.; in the same the second of the

or 36 min.

IX. THE CUBE AND RECTANGULAR SOLID. Pages 133 and 142.

X THE CYLINDER.

1. Teach the Definition

Do this by showing cylinders of various dimensions.

Have the three bounding surfaces described. Two are circles of the same area. The third is a curved surface every part of which is equally distant from a straight line joining the centres of

2. Given the dimensions, to find the surface area.

First show how to find the area of the surved surface.

This is most readily done by cutting a sheet of paper to fit the curved surface. On removal the paper is seen to be a rectangle, one dimension of which it equal to the circumference of the cylinder and the other is equal to its height.

Hence, the area of the curved surface is found by multiplying the number of units in the circumference by the number of like units in the length to find the number of corresponding units of area.

The total surface can now be easily found by the pupil who can find the area of the bounding circles.

3. Given the dimensions, to find the Cubic Centent.

Ex. 1. Find the cubic content of a cylinder 3; in. in radius and 1 ft. in length.

Area of one end= $[44\times(3\frac{1}{2})^{4}]$ sq. in.=38\frac{1}{2} sq. in.

It is evident that a block from this sylinder 1 inch deep will contain 28% c. in. The cylinder is 12 in. deep, hence, the cubic content is (12×38%) c. in., or 462 c. in.

Ex. 2. Find the number of subic feet of iron in a water pipe 3 ft. in diameter, 12 ft. long, the iron being 1 in. thick.

This is to be found by computing the cubic content of two cylinders, one the whole cylinder as though it were solid, and the other the cylindrical opening, and then taking one from the other.

Thus, onbic content of a solid cylinder=
$$[12\times(\frac{14}{14})^2\pi]$$
 c. ft.

'' '' the opening = $[12\times(\frac{14}{14})^2\pi]$ c. ft.

Quantity of iron in cylinder= $(12\times\frac{14}{14}\times\frac{1}{14}\times\pi)$ c. ft.

=9\frac{1}{2} \cdot \text{ft}.

The popular way of doing this example is to conceive the pipe to be cut open and flattened out. This is inaccurate for the resulting shape is not a rectangular solid, the upper and lower surfaces not being of the same area.

4. Given the cubic content and one dimension, to find the other.

Ex. 3. Find the radius of a cylinder 28 in. long which contains 1782 c. in.

NL THE PYRAME.

Stone.

1. The Dellattice.

Teach the definition by showing pyramide of various kinds as those having bases which are triangular, quadrilateral, pentagonal, etc.

Call attention to the base—a plane surface bounded by straight lines.

Then examine the other faces. There are as many triangular faces as the base has sides and all most in a point.

Hence, a pyramid is a solid bounded by a plane face enclosed by three or more straight lines, which is called the base, and as many triangular faces as the base has sides.

2. Given the stant height and the length of each side of the base, to find the surface of the suremid.

Ex. 1. Find the total surface of a square-based pyramid whose edge measures 2 ft. 8 in. and slant height is 3 ft. 6 in.

Area of base=
$$(\frac{2}{3} \times \frac{2}{3})$$
 aq. ft. =7 $\frac{1}{3}$ aq. ft.;

Area of 4 faces=
$$\left(4 \times \frac{2\frac{3}{2} \times 3\frac{1}{2}}{2}\right)$$
 sq. ft.=18\frac{1}{2} sq. ft.;

Total surface=25f sq. ft.

3. Given the base and altitude, to find the cubic content of a syramid

To illustrate this procure a hollow vessel with a rectilinear base and sides at right angles to it and also a hollow pyramid with a base equal to the base of the other vessel and of the same altitude. Fill the pyramid with dry sand and empty it when exactly full into the vessel. Continue to do this until the vessel is full. It will be found that the vessel holds just THERE times as much as the pyramid.

Hence, to find the cubic content of a pyramid multiply the number of units of area in the base by the number of corresponding units of altitude and one-third of the product will be the number of corresponding units of cubic content.

Ex. 2. Find the cubic content of a pyramidal tent which covers a rectangular piece of ground 15 ft. by 18 ft. and is 23 ft. high.

Area of base=
$$(15\times18)$$
 sq. ft.:
Cubic content= $(1\times15\times18\times23)$ c. ft.=2070 c. ft.

All THE COME.

Bless

In The Definition

Teach this by showing cones of various since.

Call attention to the base, a circle, and to the curved surface tapering to a point.

Hence, a come is a solid bounded by a circular plane face, the base, and a curved face tapering from the circumference of the base to a point.

Show that a cone may be projected by revolving a right-angled triangle about one of the sides enclosing the right-angle.

2. Given the dimensions of the base and the stant height to find the error of the surface.

If a piece of paper be cut to fit the curved surface and then spread out, it will form a sector of a circle.

Ex. 1. Find the total surface of a cone 7 in. in radius and 18 in. in slant height.

The curved surface, the sector of a circle, may be supposed to be made up of triangles the sum of the bases of which is the circumference of the base of the cone and the altitude of which is the slant height.

Circumference of base= $(4^{\circ}\times14)$ in. =44 in.; Area of surved surface= $\frac{44\times18}{2}$ sq. in. =396 sq. in. Area of base= $(4^{\circ}\times7^{\circ})$ sq. in.=154 sq. in. Total area=550 sq. in.

3. Given the base and altitude, to find the cubic content of a cone.

To illustrate this procure a hollow cylinder and a hollow cone of the same area of base as the end of the cylinder, and of equal altitude. Then proceed as in the case of the pyramid. It will be found that the cubic content of the cylinder is just THREE times that of the cone.

Ex. 1. What is the volume of the largest possible sone turned from a cubic block of wood whose edge is 10\frac{1}{2} in.\frac{7}{2}

Diameter of cons=10\(\frac{1}{2}\) in.;

Area of base of cone=[\frac{1}{2}\times (5\(\frac{1}{2}\))^2] sq. in. =86\(\frac{1}{2}\) sq. in.;

Altitude of cone=10\(\frac{1}{2}\) in.;

Volume of cone=(\(\frac{1}{2}\times 10\(\frac{1}{2}\times 86\(\frac{1}{2}\)) e. in.=303\(\frac{1}{2}\) eu. in.

MIL THE SPHESE.

Money.

1. The Definition.

Present spheres of various sizes. Call attention to the position of the bounding surface. It is equally distant from a point within called the centre.

Hence, a sphere is a solid, bounded by a curved surface every point of which is equally distant from a point within, called the centre.

2. Given the radius, to find the area of the sphere.

How to find the area of a sphere cannot be shown to a class of beginners. The rule should be told. However, it may be approximately determined as follows:—

Bore a hole through the centre of a circular piece of board. Tie over one of the circular faces a rubber membrane and mark on the rubber any small area. Insert a cork and tube into the hole and introduce water until the rubber is bulged into the form of a hemisphere. Measure the area which was marked on the rubber. It is now just twice as large as before the water was introduced. Thus the curved surface of a hemisphere is just twice the area of the plane face.

Or, take a croquet ball and with a saw divide it into hemispheres. Place one with the flat part down and drive a tack into the centre of the curved part. Attach a ball of twine to the tack and wind it round the surface of the hemisphere as a cord is wound round a spinning top so that it will exactly cover the surface. Then drive a tack into the centre of the flat part of the other hemisphere and attach the twine to the tack and wind it around pressing it down on the flat surface until it is entirely covered. It will be found that the string covering the flat surface is just half as long as that covering the round surface.

3. Given the redice, to find the cubic content of a sphere.

A sphere may be regarded as composed of a large number of pyramids, whose apexes units at the centre of the sphere and whose bases form the curved surface.

Honor, number of units of area of base =4 T r s

or " " height = r;

or " " online content=\$xrx4 T r

=\$ T r s.

Ex. 1. How much iron is there in a hollow sphere 12 in. is diameter, the iron being 1 in. thick?

Cable content of sphere— $(4 \times 4^{\circ} \times 6^{\circ})$ c. in.;

" oavity— $(4 \times 4^{\circ} \times 5^{\circ})$ c. in.;
.". number of c. in. of iron— $4 \times 4^{\circ}$ (6°—5°)—2014.

XIV. SIMPLAR BOLIDS.

Steen.

1. The Definition.

Present similar solids as spheres, cubes, restangular solids, etc. Show that when similar they are of the same shape and have the same number of similar surfaces but they are not necessarily of the same size.

2. The volumes of similar solids are proportional to the cubes of the measures of the corresponding these of measurement.

·Illustrate this by comparing the volumes of a number of similar solids.

Thus, compare the volumes of two cubes with edges 1 in. and 3 in. long, respectively; of two spheres with radii 3 in. and 4 in., respectively; etc.

Compare the volume of a restangular block 2 in, by 3 in, by 4 in, with another three limes as long, three times as wide and three times as deep.

Show by drawing that the latter can be divided into 27 blocks each equal to former.

Ex. 1. A sphere 2 in. in diameter weight 16 oz.; find the weight of a sphere made of the same material 2; in. in diameter.

Weight of 2nd sphere= $\left(\frac{2\frac{1}{2}}{2}\right)^{3} \times 16$ os.=31\frac{1}{2} es.

Ex. 2. The breadth of a rectangular solid is 12 ft.; what must be the breadth of a similar solid whose volume is three times as great?

Here, (measure of breadth) =3;
... (measure of breadth) =12°×3;
... measure of breadth=12×1.44225=17.307;
... breadth=17.307 ft.

XIX. THE METRIC SYSTEM.

In 1786 France adopted the Metrie System of Weights and Measures. It is based on the decimal system of notation, all the units used being multiples or submultiples by 10 or by powers of 10, of the primary unit.

The standard unit is the metre which is legally defined to be the length of a platinum red at the temperature of multing ice, and which was supposed to represent one ten-millionth part of the distance from the equator to the pole of the earth at the level of the sea. It has since been assertained that this is not quite correct. Hence, the metric standard unit of length is Borda's pintinum red and not an exact fraction of a meridian of the earth. As will be seen from the diagram in the Public School Arithmetic the decimetre or touth part of a motre is nearly 4 inches long. The metre itself is 20.27 inches long, nearly lyk yards.

2. Primary Units.

(1) The unit of length is the METER.

(2) The unit of volume is the Little. This is the capacity of a subleal box 1 decimetre long, wide, and deep. It is equal to 1.761 Imperial Plats.

(3) The unit of weight is the GRAM. This is the weight of as much distilled water as at the temperature of 4°C. (its greatest density) will fill a subleal measure 1 continetre long, wide, and deep. It equals 15,4323 grains.

(4) The unit of surface is the Ann. This is equal to a square surface 10 metres long, and wide and contains 119.601 eq. yards.

Certain apparatus is necessary to teach the tables properly:-

(a) FOR LINEAR MEASURE !-

A divided metre stick, a metrical tape line, a metrical chain.

(b) FOR SQUARE MEASURE:-

A square decimetre sub-divided into square centimetres.

(e) FOR MEASURE OF CAPACITY:-

A litre; a cubical box I decimetre long, wide and deep; a contilitre.

(d) FOR MEASURE OF WEIGHT:-

A pair of scales and the following weights:-A gram wt., 2 two gram wis., a five gram wi., 2 ten gram wis., a twenty gram wi., a Afty gram wt., a hectogram, two hectogram.wtq., a half kilogram, and a kilogram.

4. Stone.

(a) Teach Linear Measure first.

(5) Begin with the metre. Show that 10 decimetres make 1 metre, and that 10 centimetres make 1 decimetre, and infer that 100 centimetres make a metre.

(e) Have pupils measure 2, 3, 4, 5, etc., decimetres and express each of these in centimetres. If they understand decimals have

these expressed also as metres."

(d) Show by measuring that 10 millimetres make a centimetre and once more use reduction to fix the relative lengths of the measures already taught.

(e) From the metre proceed by measuring to the dekametre; then to the hectometre and kilometre and use in each case many mental problems in reduction to fix the relative lengths of these measures.

A kilometre should be measured and marked off for future reference. This can be done after school with the class assisting.

Select a straight road or street for this purpose.

(f) At this time make no attempt to infer the meanings of the prefixes, milli, centi, deci, deka, hecto, and kilo. This may be done after Long Measure is well understood.

XX. MISCELLANEOUS EXERCISES.

L CIRCULATING DECIMALS.

See Page 173.

M. PROBLEMS ON WORK

(1) Show the relation between the time of doing a work and the part done in one unit of time.

Thus, a work can be done in 2 da., hence i of it is done in 1 da.; etc.

(2) Show the relation between the part done in one unit of time and the time necessary to complete the work.

Thus, if † of a work is done in 1 da., in what time can the whole work be done?

Time to do † of work=1 da.;

"" " | " | da.;

" | da.=1† da.

- (3) Show how to find the amount of work done by a number of men in a unit of time.
 - (4) Apply these principles to solving problems. See page 74.
- (1) By means of a clock or watch show that the minute-hand moves 12 times as fast as the hour-hand. It moves over 60

minute-spaces while the hour-hand moves over 5 minute-spaces and thus 55 minute-spaces are gained by it in 60 minutes of time, hence 1 minute-space is gained by the minute-hand in 11 minutes of time.

(2) Next train the pupils to find the relative position of the

hands at the time given.

(3) Then ascertain the number of minute-spaces to be gained by the minute-hand to bring them into the position required.

(4) Now calculate the time required.

Ex. 1. See page 78.

Ex. 2. What is the second time after four that the hands of a watch are 2 minute-spaces apart?

(1) At four they are 20 min.-spaces apart.

(2) These 20 min.-spaces must be gained and 2 more; hence, 22 min.-spaces must be gained.

(3) 22 min.-spaces are gained in 22 times 11 min. of time, or in 24 min.

Hence, the time is 24 min. past 4.

Ex. 3. What is the first time after 7 that the hands of a watch are at right angles?

(1) At 7 the hands are 35 min.-spaces apart.

(2) When at right angles they are 15 min.-spaces apart; hence, 20 min.-spaces must be gained.

(3) 20 min.-spaces are gained in 20 times 11 min. of time, or 21 n min.

Hence, the time is 21 min. past 7.

Ex. 4. What is the first time after 5 that the hands of a watch form an angle of 72°7

72'= of the circumference;

. . 72°= dof 60 min.-spaces=12 min.-spaces;

(1) At 5 the hands are 25 min.-spaces apart.

(2) 18 min.-spaces must be gained.

(3) 18 min.-spaces are gained in 18 times $1\frac{1}{11}$ of time, or $14\frac{1}{11}$ min. Hence, the time is 14 7 min. past 5.

Ex. 5. What is the first time after 5 that the hands of a watch are equally distant from the figure 5?

(1) The hands are 25 min.-spaces apart.

(2) The hour-hand is a certain distance from 5.

(3) The min.-hand is the same distance from 5 and 12 times that distance from 12.

(4) Hence, 13 times that distance=25 min.-spaces; .'. once that distance=1} min.-spaces: ... the min.-hand is (25-118) min.-spaces past 12, or 2218 min.-spaces past 12.

Time is 23r's min. past. 5.

IV. PROBLEMS INVOLVING VELOCITY.

These are quite simple. The main point is to state clearly what is given. There are just two cases as follows:---

Case I. Given the distance a body moves in a given time, to find the distance covered by it in enother given time.

Ex. 1. How many feet per second is equal to a rate of 45 miles per hourf

In (60×60) see, the distance gene—(45×5280) ft.;
... 41 1 44 45 44
$$=\frac{45\times5280}{60\times60}$$
 ft.=66 ft.

Case II. Given the distance a body moves in a given time, to find how long it will require to move a certain distance.

Ex. 2. How long will a train 80 yards in length, moving 20 miles per hour, take to cross a bridge 184 yards long?

Time to move
$$(20 \times 1900)$$
 yd.= (60×60) sec.;
 $(80+184)$ yd.= $\frac{264 \times 60 \times 60}{20 \times 1760}$ sec.=27 sec.

V. PROBLEMS INVOLVING THE SUM AND DIFFERENCE OF TWO QUANTITIES,

1. Given the sum of two numbers and the difference of the same two

By means of many examples show

(1) that the sum of two numbers added to their difference gives a sum which is equal to twice the greater number, and

(2) that the difference of two numbers taken from their sum gives a remainder equal to twice the smaller number.

2. Stream Problems.

Problems should not be given until the forces affecting a boat on a stream are understood. Show the following by such questions as, "What forces are causing a boat to move down a stream?" "How do these forces affect the boat in going up the stream?" etc.:

(1) The rate down the stream is the sum of two rates, vis., the rower's rate in still water and the rate of the stream.

(2) The rate up stream is the difference of the same two rates.
(3) The sum of the rower's rate down and up stream is equal to twice his rate of rowing in still water.

(4) The differe we between the rates down and up stream is equal to twice the cate of the stream.

Ex. 1. A can row 12 miles down stream in 3 hours and the same distance back in 4 hours. Find the rate of the stream in miles per hour.

Rate down per hour=4 ml.

Hence, rate in still water + rate of str. =4 ml. ... 2×rate of str.=1 ml.;

rate of str. : = | ml. Ex. 2. A can row 41 ml. down stream in an hour. Without the aid of the stream, it would have taken him 14 hr. How long will it take him to return f

Rate in still water per hour-40 ml.=3 ml.; of stream " =(4j-3) ml.=1j ml.; .'. rate of boat up stream=(8-1i) ml.=1i ml.; Time to row 4 \dagger ml. up stream= $\frac{\epsilon t}{14}$ =8 hr.

Ex. 3. A can row 6 ml. down stream and back again in 2 hr. 40 min., and his rate of rowing in still water is twice the rate of the stream. Find his rate of rowing in still water.

Rate down stream=3 times rate of str.

Hence, in going the round trip he spends i of the time in going down and f in rowing back.

i of 160 min .=40 min.

Rate per hour down stream=# of 6 ml.=9 ml. up " = ml. Hence, rate in still water-2 ml. =6 ml.

Ex. 4. A boat's crew can row over a course of 12 ml. against a stream which flows at the rate of 2 ml. per hr. in 10 min. The usual rate of the stream is 1 ml. per hr. How long would the crew take in the usual state of the river?

Rate up stream per hr.=(6×11) ml.=71 ml. Rate of stream=2 34 1 .'. rate in still water=94 "

.'. rate in usual state of river=9 Hence, time to row 9 ml.=60 min.;

" " " 11" = 11×60 min.=81 min.

PART IV.

Review Problems.

SIMPLE RULES

- 1. A boy rides round a field 80 rods long and 48 rods wide. How many rods will be travel in going round it three times f Ams. 768 rods.
- 2. A room is 64 ft. long and 27 ft. wide. How long will a biring be that will go around it twice ? Ams. 364 ft.
- 3. Find the sum of all the numbers ending in 73 between 9272 and 10087. Ans. 87057.
- 4. A has \$3120 which is \$634 more than B has. If C has \$1306 less than A and B together, how much have all? Ams. \$9306.
- 5. A man bought a house and lot for \$1500; he expanded \$1290 on it. The house was burned; he got \$3780 insurance, and sold the lot for \$1960. Find his loss. Axs. \$50.
- 6. Find a number that exceeds 14967 as much as 47058 exceeds 31407. Ams. 30618.
- 7. In a school there are 318 scholars; 177 are boys. The girls occupy two rooms, in one there are 65. How many are there in the other? Ams. 76 girls.
- 8. A boy caught 178 fish and another caught 262. How many must the first get from the second that both may have an equal number? Ans. 42 fish.
- 9. A drover bought 10431 sheep; he sold 5736 and then bought 763 less than he had left. How many had he then? Ans. 8627 sheep.
- 10. A is worth \$15687; B \$578 less than A; C \$947 more than B, and D \$1568 more than C. How much have they all ? Ans. \$64491.
- 11. John has \$1650 and James has \$764 less than John. If Chas. has \$2347 more than John and James together, how much have they all ? Axs. \$7419.

12. A man lost \$2750 on the race track; his father gave him \$3470 and he borrowed \$1550, he then spent \$3695 and had \$12000 left. What had he at first? Ams. \$13025.

13. Three brothers A, B and C had given to them the following amounts: A, \$12500; B, \$18000; C, \$11500. B gave C \$5375, who gave \$2875 to A, who gave \$1875 to B. How much had each then? Ams. \$14000 each.

14. A sold a horse to B and gained \$118. B sold it to C for \$550 and gained \$72. What did the horse cost A? Ams. \$360.

15. A wholesale merchant's sales for the first six months were as follows: Jan., \$21972; Feb., \$36489; March, \$17437; April, \$21008; May, \$14567; June, \$21497. Out of which his gain was \$35217. Find the cost of his goods. Ams. \$97753.

15. A man gave away \$37.50, and then borrowed \$26.75, spent \$75.50 and had \$13.35 left. What had he at first? Ams. \$100.

17. What number increased by the difference between 1875 and 2368 will make the sum of 416, 2487 and 2097? Are. 4507.

18. A lady paid \$26 for a dress, \$3.50 for a parasol, \$4.50 for boots, and \$7 for a hat. How much had she left of \$50? Ams. \$9.

19. Find the difference between the sum of the six numbers of 3 figures each that can be expressed by the figures 5, 8, 7; and the sum of six numbers of two figures each that can be expressed by the same figures. Ans. 4000.

20. A man has \$272.50 in the bank, he takes out \$26.95, he then puts in \$109.41, and five days after he draws out \$57.64. How much has he still in the bank? Ans. \$897.32.

21. A, B, C, D bought a farm for \$14000; A paid \$3750, B \$525 less than A, C \$800 more than B. How much less than A did D pay! Ams. \$550.

22. A man spends on Monday \$1.80, on Tuesday \$1.15, Wednesday \$1.05, and as much more for the rest of the week. He carned \$21.80. How much did he save? Ans. \$13.80.

23. Find the product of all the numbers ending in 4 between 21 and 61. Ans. 1938816.

24. Two trains start from Hamilton at 5 p.m. and travel in the same direction, one at 27 miles and the other at 36 miles per hour. How far apart will they be at 5 a.m. next day? Ans. 108 miles.

25. A farmer bought a horse for \$175, which he traded for some cattle and \$21 in each. Some of the cattle died and he sold the rest for \$137. How much did he lose altogether? Ans. \$17.

- 2f 4 man carns \$2.40 a day. What will be earn in the month of July at the month begins on Tuesday? Ann. \$64.80,
- 27. A man earning \$2.25 per day of 9 hrs., lost 17 hours in a week. What did his earnings amount to fer that week of 6 days?
- 28. A man bought 375 acres of land at \$18 per acre and sold it for \$7000. What did he gain? Ams. \$250.
- 29. A man earns \$18 a week and pays \$27 per month for board. How much can he save in a yearf 1 yr.=12 months=52 weeks. Axs. \$612.
- 30. What number is that to which if 17 be added the result will be 15 times 128? Axs. 1903.
- 31. Find the difference in the cost of 275 horses at #33.20 each and 483 eattle at \$56.10 each. Ams. \$1466.30.
- 32. A farmer exchanged 1840 bu. of wheat at \$1.10 per bu. for 164 bbl. flour at \$9.20 per bbl. and the balance in each. How much each should be receive? Ans. \$515.20.
- 33. Find the difference in the value of two farms one of 250 acres at \$74 an acre and the other 188 acres at \$125 per acre. Ams. \$5000.
- 34. What is the difference between the values of \$4 horses at \$129 each and 168 cattle at \$64 each? Ann. \$84.
- 25. Find a number such that when the sum of the edd numbers between 66 and 78 is taken from it the remainder will be 25 times 296. Ams. 7765.
- 36. What number is that from which if 47 times 19 be taken, the remainder will be 35 times 137? Ams. 5688,
- 37. If I buy coffee for 65c., ten for 98c. and butter for 127c., and give a \$5 bill in payment. What change should I receive? Ams. \$2.15.
- 38. 398 acres of wheat in Manitoba yielded 52 bu. per acre, which sold at 40c. a bu. What was the value of the crop? Ams. \$8278.40.
- 39. A farmer soli 234 sattle at \$64 each and then bought 960 acres of land at \$25 an acre, borrowing the balance to pay for it. How much did he borrow? Ans. \$9024.
- 40. A southern trader sold 673 bales of cotton of 417 lb. each at 23c. a lb. What did he get for it? Ann. \$64547.48.

- 41. A farmer has 166 sheep in one field, 3 times as many less 247 in another, and in a third 149 more than in both of the others. How many has he altogether? Axe, 999 sheep.
- 42. A, B, C and D bought property for \$100000. A's share was \$25625; B's \$7250 more than A, and C \$6219 less than B. How much had Df Ams. \$12825.
- 43. A farmer bought 48 cows for \$1056; he fed them at an expense of \$2.45 each, and sold them all for \$1496. Find his total gain. Ams. \$222.40.
- 44. A boy lives 96 rods from school, he goes regularly for 37 weeks, 5 days each week, and goes home to dinner every day. How many rods will be travel altogether? Ams. 71040 rods.
- 45. Four men bought mining property for \$26200. A put in \$6525; B \$845 more than A, and C \$100 less than B. What did D give? Ams. \$4095.
- 46. A drover bought 468 sheep at \$4 each; he paid freight \$117. Fifteen sheep died and he sold the remainder at \$6.19 each. Find his net gain. Ann. \$815.07.
- 47. In a factory there are 25 men at \$2.40 per day and 38 women at \$1.60 per day. How much more will be paid out to the women than to the men in 18 days? Am. \$14.40.
- 48. A man earns \$62.75 a month and spends \$7.25 a week, how much will he save in 5 years. 1 year=12 months=52 weeks. Ams. \$1880.
- 49. Divide the product of 784 and 348 by the difference between 784 and 436. Ams. 784.
- 50. 231 mon earn \$1732.50 in a week. What does each earn in a day? Ams. \$1.25.
- 51. Divide the product of 22, 23, 24, 25 by the product of their right hand digits. Axs. 2530.
- 52. Find the remainder when the product of the first 10 numbers is divided by the difference between the product of the even numbers and the product of the odd numbers. Ams. 1365 remainder.
- 53. The exports of obtton from the U. S. during 1885 was 1889514368 lbs. How many bales of 476 lb. each were exported? Ams. 3969568 bales.
- 54. In a paper mill 475 sq. ft. are manufactured per minute. How many sq. ft. will be made in 8 weeks, working 5 days each week and 600 minutes each day? Ams. 11406000 sq. ft.

- 55. I sold 56 horses for \$0000, gaining \$25 on each. Find the cost of each. Ann. \$130.
- 56. A Manitoba farmer bought 640 acres of land for \$14000, he sold part of it for \$0000 at \$22 per sere and the rest at \$65 am sere. What did he gain? Am. \$17700.
- 57. A merchant bought flour for \$1061.50 at \$5.50 per bbl. and sold it to gain 46c. on each bbl., find the number of bbl. and the total gain. Am, 190 bbl.; \$77.20.
- 56. If 36 horses cost \$4650, at what rate must each be sold to gain \$12.50 per head? Ams. \$150.
- 50. Multiply 41768 by 630 and divide the product by $2\times5\times7\times9$. Ams. 41768.
- 60. A fruit dealer bought 6 bbl. of apples at \$2.25 per bbl. Each bbl. contained 560 apples, which he sold at 8 for 5c. How much did he gain? Ams. \$42.50.
- 61. A man bought 30 oxen at \$45 each; 4 died and he sold the rest so as to gain \$80 on the transaction. Find the selling price of each. Ams. \$65.
- 63. A man sold 213 bbl. of flour for \$5112 and gained \$1278. Find the cost per bbl. Ams. \$18.
- 68. What is the smallest number divisible by 9 which added to 4362 makes the sum divisible by 127 Ams. 36,
- 64. A certain number increased by 4376 and the sum multiplied by 427 gives 3846416 for product. What is the number? Are, 4632,
- 65. What is the least number which taken from 292468 leaves a remainder of which 84 is an exact divisor? Avs. 59.
- 66. The dividend is $24 \times 9 \times 15 \times 84$ and the divisor $5 \times 7 \times 26 \times 108$. Find the quotient. Axs. 2.
- 67. I sell my home for \$4500; village lots for \$500; Loan Co. stock for \$1150; furniture for \$1050; and receive in payment \$6000 in each and the balance in N. W. lands at \$2.50 per acre. How many acres do I get? AMS. 480 acres.
 - 68. Find the amount of the following bill:—

 147 cerds hard wood @ \$5.75 per cord;
 206 '' soft @ \$4.25 '' ''

 4 car loads of slabs 16 cords each @ \$2.75 per cord;
 816 tons hard coal @ \$5.15 per ton;

536 " soft " @ \$8.95 " " Axs. \$8162.75.

- 60. A merchant bought 63 bbl. of apples and 47 bbl. of flour for \$722. He paid \$10 a bbl. for the flour; what did he pay per bbl. for the apples? Am. \$4.
- 70. A bought 100 acres of land for \$3750; he allowed 15 acres for streets, and divided the rest into village lots and sold them for \$17920 at \$230 each. How many lots did he sell? Ams. 56 lots.
- 71. In a certain city there are 5500 children in the P. S. and the cost of maintaining them is \$20050. What is the cost for each child? Axs. \$7.10.
- 72. In a block of stone there are 454664 c. in. How many c. ft. are there if 1 c. ft.=1728 c. in. f Axs. 268 c. ft.
- 73. The steel rails on a railway weigh 384 lb. each. How many will there be in 2211840 lb. Axs. 5760.
- 74. A history has 466 pages in a volume and 84 lines on a page. If the total number of lines is 249984, how many volumes are there? Axe. 6 volumes.
- 75. A coal dealer sold 552 tons coal for \$2456.40 and lost \$110.40. At what rate per ton should be have sold to gain \$138.00; Ams. \$4.90.
- 76. In South Africa a soldier's rations were 36 oz. per day. How many lb. of 16 oz. each would it take to supply Lord Robert's army for 64 days if he had 156000 men? Ams. 22464000 lb.
- 77. A fruit grower in California packed 340000 lemons in boxes and sold them for \$6528 at \$4.80 a box. How many lemons are there in a box? Ams. 250 lemons.
- 78. A drover exchanged 245 horses at \$75 each for 466 cattle and \$3463 cash. What was the price of the cattle per head? Ams. \$84.
- 79. How many doz. eggs at 14e. a doz. must be given for 15 yd. of cloth at \$14 for 5 yd.? Ams. 300 doz.
- 80. I sold 2048 yd. of cloth for \$1249.28 and by so doing lost 4c. a yd. At what price per yd. must I have sold it to gain \$102.40? Ams. 70c.
- 81. If I gain \$1428 by selling 119 seres for \$9168, what would 221 seres cost me to buy at the same rate? Ans. \$14265.
- 82. A man sold his farm in village lots for \$750 each and bought 200 horses at \$125 each with the money. How many lots did he sell? Are, 50 lots.

- 68. From the sum of 49065×7×9 and 50914×7×9 take the difference between 76906642+9 and 22730766+7. Ann. 1000000.
- 84. How many buthels of wheat at 72c. a bu, should be given for 800 bu, of oats at 40c. a bu. f Ams. 500 bu.
- 85. A train goes from Sarnia to London, 62 miles, in 2 hours. At the same rate in how many hours after leaving London will it reach Montreal, a distance of 436 miles? Axe. 14 hr.
- 96. If 45 lb. of ten cost \$26.50, what amount of butter at 16c. per lb. will pay for 8 lb. of tenf Ams. 32 lb.
- 87. Find the value of 6360 lb. of wheat at 71c. a bu. Axs. 875.33.
- 88. How many boxes of ten of 48 lb. each at 60c. a lb. must be given for 16 tube of butter of 50 lb. each at 18c. a lb.? Axs. 5 boxes.
- 59. A man bought 60 scree at 866 per sere; he paid out for repairs \$754 and sold it for \$6374. How much did he gain per sere? Am. \$21.
- 80. A boy buys 340 papers a week at 3c. each and sells them at 4 for 18c. How much did he gain in 7 weeks? Ans. 942.
 - 91. Find the amount of the following bill:—
 216 bu. potatoes @ 45c. a bu.;

150 bu. turnipe @ 25c. a bu.;

170 bu. peas @ 80c. a bu. Ams. \$270.70.

- 92. A man sold 1476 bbl. of flour for \$11588. 296 bbl. were sold @ \$7 per bbl. and 450 bbl. at \$6.50 per bbl. At what rate per bbl. did he sell the remainder? Arm. \$9.
- 98. A wold to B 350 seres at \$120 per sere; and gained \$5775. B sold it at a loss of \$47.25 per sere. How much less per sere did B receive than A paid? Ams. \$30.75.
- 94. A store keeper sold hats at \$3 each and an equal number at \$3 each. How many did he sell altogether for \$9635? Ams. 3984 hats.
- 96. What number is that to which if 247 and 4 times 247 be added, and 127 and 4 times 127 be taken from the result, the remainder will be \$1647 Ams. 8564.
- 96. A farmer raised 512 bu, wheat in 1898 and twice as much in 1899, and in 1900 as much as in the other two years. What was the value of all at \$1.25 per bu.f Ans. \$3840,

97. If I take 23778 from the sum of 8861 and 24867, divide the remainder by 25 and multiply the quotient by 9, what will the product be? Ams. 3862.

96. If 17 gal, of wine at \$8.75 per gal, are mixed with 51 gal, at \$8.86 per gal, at what price per gal, must the mixture be sold to gain \$94.177 Axi. \$8.60.

50. A recervoir holds 300000 gal. How many hours will it take to fill it if 1890 gal, are pumped in every minute and 1340 taken out in the same time. Ans. 12 hr.

100. A certain number is multiplied by 65 and 748 subtracted from the product, and when the remainder is divided by 264 the quetient is 32 and the remainder 36. Find the number. Apr. 142.

101. A dealer sold perk for \$33832 and gained \$5184 by selling it at \$19 a bbl. What was the cost per bbl. Are. \$16.

102. I paid \$30422 for horses at \$96 each; 17 died and the rest were said for \$31500. What did I gain on each one sold? Axs. \$9.

168. A farmer planted 864 rows of corn, with 297 hills in each row; had he put 243 hills in each row how many more rows would be necessary to have the same number of hills? Ams. 192 rows.

104. If 27 men can plant 11004 hills of corn in 13 hours, how many hills can 63 men plant in the same time? Axs. 27216 hills.

105. A man sells 250 bags of flour at 7c. a lb. and receives in payment 34 cheets of tea of 75 lb. each at 70c. a lb. Find the weight of one bag of flour. Ams. 102 lb.

106. A entitle drever paid \$22464 for cattle at \$26 each; 25 head were stolen and 56 died; he sold the rest at a gain of \$5724 above the cost of all. Find the selling price per head. Ams. \$36.

107. 5700 persons each paying 2c. toll and 728 cabs each paying 6c. toll pass over a bridge in 12 hours. Find the average amount of money paid per hour in toll. Ams. \$13.14.

198. A certain number increased by 12068 and the sum divided by 247 will give a quotient of 138 and a remainder; if the remainder is multiplied by 225 the product will be 55350. What is the original number? Ams. 21364.

160. If flour is \$4.75 a bbl. and apples \$2.40 a bbl., how many bbl. can be bought for \$343.20 to have the same number of each? Ams. 48 bbl. of each.

110. A farmer spent \$7.25 for groceries; \$13.50 for a store; \$3.75 for a pair of boots; \$17.75 for clothes, and \$6.25 for

harnous. Hew many bu. of wheat at 97c. will pay the bill. And.

- 111. A farmer sold an equal number of bu. of wheat, eats and barley for \$670; the wheat sold at \$60., the cats at \$20. and the barley at \$60. How many bu. of each were sold? Ams. 180 bu.
- 119. A greeer bought 48 bbl. of oil and sold it at a gain of 6s. a gal, and thus gained \$144. How many gal, were there in a bbl. f Ams. 80 gal,
- 113. A drover with \$6500 bought 36 horses at \$70 each; 55 cows at \$66 each; 100 pigs at \$5.25 each, and sheep at \$6 each. How many sheep did he buy? Aug. 297 sheep.
- 114. 36 bbl. of vinegar cost \$504. If it was sold at 40c. a gal. and there were 54 gal. in a bbl., how much was gained? Axe. \$163.60.
- 115. A speculator bought town lots for \$7300, and sold them to gain \$610 at \$600 each. How many did he soll? Axe. 80 lots.
- 116. If 40 sq. rods of land will produce 15 bu. of pointees, what will be the value of the crop grown on 17 acres at 50c. a bu.?

 AMS. 9510.
- 117. I sold 1600 bu. of wheat for \$2048 and thus lest \$60. It I had sold it to gain \$66, what should I get per bu.? 'Axe. \$1.20.
- 118. How many bhl. of apples containing 8 bu. each at 40c. a bu. will be equal in value to 16 boxes of cranges each containing 286 cranges at 12 for 15c.? Ams. 48 bhl.
- 119. How many bbl. of sugar of 300 lb. each worth 4s. a lb. must be given for 30 bbl. of flour at \$4.40 per bbl. and \$53.40 each? Axx. 15 bbl.
- 190. A farmer sold 1440 bu. of oats at 28c. a bu. and received in payment 8640 ft. of lumber at 3c. a foot and pigs at \$6.00 each. How many pigs did he get? Ans. 18 pigs.
- 121. A field containing 48 acres yielded 26 bu. per acre. The grain was sold at 65c. a bu. and the money invested in sheep at \$5.20 each. How many sheep were bought? Am. 156 sheep.
- 128. A dealer bought 840 bu. of wheat at 18 bu. for \$22.50 and sold it at 11 bu. for \$16.50. How much did he gain? Ams. \$210.
- 123. The smaller of two numbers is contained 48 times in 864 and the larger number is 28 times the smaller. Find the product of the two numbers. Ann. 7452.

- 124. A man buys 364 ib. of sugar for \$14.56. He uses 48 ib. At what price must be sell the remainder to gain \$4.407 Axe. 60. per lb.
- 125. A and B have equal shares in a load of potatoes of 86 bu. A takes 25 bu. and B the rest, giving A \$10.80. What are potatoes worth per bu.f Ams. 60e.
- 196. What is the cost of 296 head of entitle if by selling 247 head for \$18219 the gain is \$1435? Am. \$21812.

127. Extend the following and find the sum of the results:-

| | and were such suit of the |
|---------------|---------------------------|
| (a) 1×9+2= | 443 |
| 13×9+3- | (b) 1×8+1= |
| | 12×8+2= |
| 123×9+4= | 123×8+8= |
| 1234×9+5== | 1234×8+4= |
| 12345×9+6= | 12345×8+5= |
| 123456×9+7= | 123456×8+6= |
| 1284567×9+8= | 1234567×8+7= |
| 12345678×9+9= | 12345678×8+8= |
| 1234 | 66788 123456789×8+9= |
| | |

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II. COMPOUND NUMBERS.

- 1. A farmer had 38 ewt. 52 lb. of pork; he kept 4 ewt. and 86 lb. for his ewn use, and sold the rest in barrels of 198 lb. Howmany bbl. did he sell? Axe. 17 bbl.
- 2. In walking 1 mi. 212 rd. 4 yd. 2 feet James took 3766 steps, and Tom 5913 steps in 3 mi. 85 rd. 1 yd. 0 ft. 9 in. Find the difference in the length of their steps. Axe. 7 inches.
- If 72 cords of wood be taken from a pile 220 ft. long 12 ft. wide and 8 ft. high. How many cords will be left? Ams. 168 cords.
- 4. A farmer sold 3776 boxes of fruit averaging 1 qt. each. How many bushele did he sell? Ann. 115 bu.
- At the rate of 10 rods in a minute, how many miles and rods can a boy walk in an bourf Axs. 1 mi. 280 rods.
- 6. A field contains 348480 sq. ft. What is it worth at \$500 an acref Ams. \$4000.
- 7. If 32 sq. rd. of land cost \$96, what will be the value of 7 sq. 136 sq. rd.f . Axs. \$3768.
- 8. If a man earns £4 11s. 6d. in 6 days, what amount will he earn in 273 days. Ass. £208 8s. 3d.

- 9. If a cup weighing 11 oz. 15 dwt. cost £3 fs. 6jd., what must be paid for one weighing 17 oz. 10 dwt. 12 gr.? Ams. £5 2s. 2jd.
- 10. The intitude of Brantford is 43" 21' 22", and of Quebec 45' 30' 10". How many degrees is Quebec north of Brantford? Are. 4"
- 11. If 122 lb. 3 oz. 15 dwt. 16 gr. of gold be made into 14 ornaments of equal weight. How much will one ernament weigh? Axz. 8 lb. 8 oz. 16 dwt. 20 gr.
- 12. I sold 124 leads of wood, each containing 96 cu. ft. for \$418.50. What did I get per cord? Ams. \$4.50.
- 13. A farmer has 111 bu. 2 pk. 4 qt. of wheat which he wishes to put in bags which hold 2 bu. 1 pk. 4 qt. each. How many bags will be required? Axe. 47 bags.
- 14. How long will it take a man to walk 147840 yd. at 3 miles an hour? Am. 28 hours.
- 15. If a bey goes to bed at half-pest 8 p.m. and gets up at 7 a.m. How long is he in bed? Are. 10 hr. 30 min.
- 16. From a bbi. of vinegar containing 31 gal. 3 qt., 5 ga. 1 qt. were taken out, and 30 qt. were wasted. How much still remained in the barrel? Axe. 18 gal. 2 qt.
- 17. How many lb. es. dr. Ansir. wt. are there in 6 lb. 4 es. 10 dwt. Troyf 16 drams=1 es. Ans. 3 lb. 9 es. 9f dr.
- 18. Multiply the difference between 17 miles and 15 mi. 219 ml. 5 yd. 1 ft. 6 in, by 27. Ans. 27 miles.
- 19. There are 650 posts (including those at the end of the road) on a railway 18 mi. 465 yd. 1 ft. 6 in. long. How many rods apart are the posts? Axs. 9 rods,
- 20. A butcher bought 2 t. 8 cwt, of boof at \$190 a ten and sold it at 2 lb. for 25c. How much did he gain? Ams. \$144.
- 21. How many steps will a man take in travelling 20 mi. and 450 yd., allowing 2 ft. 6 in. to each step? Are. 42780 steps.
- 22. Find the cost of 25 lb. 14 cs. of quinine when \$192.50 is paid for 5 lb. 8 cs. Ams. \$905.621.
- 23. A cellar 42 ft. long and 24 ft. wide is flooded to the depth of 8 inches. How many barrels of water are there in it? I bbl.mm 31; gallons. Ams. 183; bbl.
- 26. I have a lot 90 ft. long and 75 ft. wide, which is enclosed by a tight board fence 6 ft. 3 in. high. Find the cost of painting both sides at 15c. per sq. yd. Ams. \$68.75.

- 35. A shed 32 ft. long, 34 ft. wide and 14 ft. high is filled with tan bark. What is the value of the bark at \$3.25 per serd? Ams. \$273.
- 26. A farm containing 123 ac. 80 eq. rd. has 80 ac. 100 eq. rd. eleared. What is the uncleared part worth at 600 per acref Axe. \$5550;
- 27. If water weighs 770 times as much as air, and 1 c. ft. of water weighs 1000 cc., how many c. ft. of air weigh 100 lb.? Ams. 1223 c. ft.
- 26. How many but of wheat will weigh as much as 180 but of Indian corn? Ams. 168 but
- 99. From a pile of wood 28 ft. long, 4 ft. wide, 4 ft. high 1 ed. 64 c. ft. is sold at one time and 96 c. ft. at another. What is the remainder worth at \$6.40 a cord? Am. \$8.00.
- 30. Mary's birthday is on Aug. 14th. When is Jane's, which is 137 days later? Aug. Dec. 29th.
- 31. How many times will a wheel 5 ft. 6 in. in eirenmference turn in going 4 miles? Ams. 8640 times.
- 22. 7 cwt. 20 lb. of sugar is taken in exchange for 1 cwt. 62 lb. of coffee at 2c. 9d. a lb. Find the price of the sugar per lb. Ams. 10d.
- 33. Find the cost of sodding a lawn 40 yd. long and 10 ft. wide with sods each containing 3 sq. ft.; the sods when laid costing 60c. per hundred. Ame. \$2.40.
- 34. A barrel of flour weight 196 lb. If 2 bu. and 2 pk. of wheat make 100 lb. of flour, how many bbl. can be made from 600 bu. of wheat? Am, 100 bbl.
- 25. What is the cost of 25 joints each 6 in. by 4 in. and 15 ft. long at \$34 per M. board measure? Ams. \$18.00.
- 38. How many tons of wire will it require to fence a rectangular farm 180 rods long and 120 rods wide, the fence being 6 wires high and 3 ft. of wire weighing 1 lb. f Axs. 9 tons 1800 lb.

III. AVERAGES AND SHARING.

- 1. The scores made by a side at cricket were 20, 5, 14, 6, 45, 16, 22, 0, 0, 10, 0; find the average score of each batter. Ars. 12.
- 2. A butcher sold 12 lb. beef at 11c. a lb. and 7 lb. at 8c. a lb. and 11 lb. at 12c. What was the average price per lb.? Ans. 10fc.

3. A traveller visiting England finds his average expenses for 56 days to be 10s. 6d. a day; for the first 42 days they averaged 10s. a day. What was the average for the last 14 days?

Total expense for 56 days is 588s, and for 42 days it is 420s.

Expense for 14 days is (588-420)s., or 168s. Axs. 12s.

- 4. The average number of runs made by 11 men at cricket was 12. The 10 of these who got out made respectively 22, 3, 7, 4, 18, 0, 21, 0, 0, 20. Find the score of the 11th man. Aus. 37 runs.
- 5. A farmer pays a rent of \$5 an acre for 150 acres, \$6.50 per acre for 120 acres, and \$8.30 per acre for 90 acres. What is the average rent per acref Ams. \$6.321.
- 6. Three schools educate 75, 33 and 31 children at an average cost annually of £2 10s., £3 10s. and £3 15s., respectively; they are united and an annual saving is made of £141 5s. Find the average cost after union. Ams. £2.
- 7. Divide \$3608 among three boys in the proportion of 1, 4, 6. Ams. 4828, \$1312, \$1968.
- 8. Divide an estate of 8374 acres among A, B and C; giving B 4 times A's share and C 9 times A's. Ams. A, 241 ac; B, 964 ac;
- 9. An examiner wishes to mark 3 questions in the proportion of 5, 8 and 12. The sum of the marks is 150. How must be distribute them? Ams. 30, 48 and 72.
- 10. A bag contains a certain number of sovereigns, three times as many shillings and four times as many pence. The whole sum amounts to £560. How many coins are there of each kind? Axe. 480 aov., 1440s. and 1920d.
- 11. A, B and C have \$200, B has twice as much as A, and the difference between the shares of A and C is \$3.92, C's being the greater. Find the share of each. AMS. A, \$49.02; B, \$98.04; C, \$52.94.
- 12. A sum of money is divided among A, B and C. C gets twice as much as A; A and B get \$200; B and C get \$240. How much does such get? Axs. A, \$40; B, \$160; C, \$80.
- 13. Divide \$31 among 5 persons giving two of them each \$3.50 less than each of the others.

If the two got the same as the others the sum distributed would be (2×\$2.50)+\$81=\$86. \$86÷5=\$17.20 for each of three; \$(17.20-2.50)=\$14.70 '' '' two.

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14. Divide 2563 ac. among A, B and C, giving B 228 ac. more than A and C 488 ac. more than B. Axs. A, 563 ac.; B, 791 ac.; C, 1229 ac.

15. A father divides his property, which amounts to \$56000, among his 4 boys in the proportion of the numbers 1, 2, 3, 4. Find the share of each. Ans. \$5600; \$11200; \$16800; \$22400.

16. Three brothers divide an estate of \$16000 in proportion to 2, 4, 5. The expenses of settlement are \$120, which are paid first from the estate. Find the samount received by the first. Ams. \$5070.

17. \$26000 is divided among 3 brothers. The eldest got half as much again as the second and twice as much as the youngest. Find the share of each.

The youngest receives \$3, the second \$4, and the eldest \$6 out of every \$13. Axs. \$12000, \$8000, \$6000.

IV. APPLICATIONS OF SIMPLE AND COMPOUND NUMBERS.

1. Make out a bill for 5 days' work at 60c. a day, 4 days' work at \$1.25 a day, and 4 bu. potatoes at 40c. a bu., crediting the person against whom you make the bill with 2 days' work of 8 hr. each at 25c. an hr. Ams. Balance \$5.00.

2. Make out a bill for the following and receipt it:—27 yd. of linen at 1s. 6d. a yd.; 35 yd. of silk at 2s. 11d. a yd.; 30 pairs of gloves at 2s. 6d. a pair; 46 yd. of velvet at 4s. 11d. a yd.; 4 doz. collars at 6s. 3d. a dozen, and 2 doz. neckties at 12s. 6d. a dozen. Ams. £25 3s. 7d.

3. Find the amount of the following bill:—13 yd. silk at \$1.85 a yd.; 27 yd. flannel at 75c. a yd.; 46 yd. muslin at 13c. a yd., and 65 yd. of calico at 7c. a yd. Ams. \$54.25.

4. Make out the following bill:—15 quires of paper at \$1.40 a ream; 25 quires at \$4.20 a ream; 2500 envelopes at 70c. per M; 750 envelopes at 18c. per C, and 120 Christmas cards at 15c. a dozen. Axx. \$10.90.

5. What will it cost to carpet a room 48 ft. long and 38 ft. 9 in. wide with carpet 27 inches wide at 4s. 6d. a yd.? Aws. £54.

6. The carpeting of an assembly room cost \$420 at \$1.75 per eq. yd. If the room was 38 ft. wide, find its length.

No. eq. yd. = \$420 - \$1.75 = 240; .'. length of room = (\$160 - 36) ft. = 60 ft.

- 7. A parior is 27 ft. long 18 ft. wide; what will it cost for rags 4 ft. 6 in. long and 2 ft. 8 in. wide to cover it, if each costs \$7.507 No. of rags is 48; cost, \$200.
- 8. Find the number of eq. ft. of plastering in a room 12 ft. 6 in. long 10 ft. 6 in. wide and 10 ft. high. Are. 460 eq. ft.
- 9. What will it cost to plaster the walls of a room 40 ft. long 52 ft. wide and 10 ft. high at 94.25 per 100 sq. ft. if an allowance of 140 sq. ft. is made for openings?

Perimeter, 124 ft.; height, 10 ft.; area of walls, 1340 sq. ft.; surface to be plastered, 1100 sq. ft.; cost, \$46.75.

- 10. A room 11 ft. high takes 143 yd. of paper 2 ft. wide for the four walls; how many feet of moulding will be required to go around the room? Axs. 78 ft.
- 11. A room is 12 ft. 6 in. long 10 ft. 6 in. wide and 10 ft. high. It has one door 7 ft. by 4 ft., one window 6 ib. by 35 ft. How much paper 2 ft. 6 in. wide would be required to paper the walls?

Area of walls is 460 sq. ft.; wrea of openings 40 sq. ft.; number of sq. ft. of paper is 411 sq. ft.; length of paper 164f ft.

12. A board fence 9 ft. high is built around a racing park 84 rd. long and 76 rd. wide at \$1.50 per 130 sq. ft. Find the cost.

Perimeter is 330 rd., or 5280 ft.; surface is (5280×9) sq. ft., or 47530 ft. at lie. per feet., is \$504.

- 13. A pacture is 48 rd. wide and contains 15 so. What will it cost to fence it at 66c. per rd.? Am. \$183.28.
- 14. What will it cost for lumber to fence a lot 135 rd. long and 160 rd. wide, 5 boards high, the boards being 6 inches wide, at 90.50 per Mf Ams, \$176.34f.
- 15. How many seantling each 16 ft. long, 4 inches by 5 inches, will be required to make 40 c. yd.?

No. of scantling=1080-21-486.

16. 27 c. ft. 1296 c. in. of lumber are required to floor a room
13 ft. 6 in. by 12 ft. 4 in. What is the thickness of the lumber?
Cubical content of floor=47952 c. in.;

Area of " =(162×148) eq. in; ... thickness=[47952÷(163×148)] in,=2 in.

17. 110 c. yd. of gravel are put on a read 40 rd. long 9 ft. wide and of uniform depth. How deep is it? Alls. 6 inches.

18. A rectangular shaft of marble contains 18 c. yd. 4 c. ft. and it is 3 ft. 6 in. square; find its height.

Cubical content of shaft, 490 c. ft.; area of end, 12 sq. ft. 422 sq. in.; length of shaft, 40 ft.

19. The ceiling of a room 27 ft. long 24 ft. wide and 13 ft. high is to be raised to increase the space 48 c. yd. How many feet must it be raised?

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Cubical content of room=7776 c. ft,; 48 c. yd.=1296 c. ft., or of 7776. ... height must be increased t of 12 ft., or 2 ft.

20. 116 c. yd. are taken from a cellar in. 168 loads; how many c. ft. are there in each load? Ams. 29 c. ft.

21. Two school reoms have equal subisal content. One has a floor area of 300 sq. ft. and is 12 ft. high. The other is 15 ft. high; find its floor area.

Cubical content is 4820 c. ft.; area of floor is (4320-15) aq. ft.

22. A log 24 ft. long and 2 ft. square is out into scantlings 4 inches square and 8 ft. long. What will they be worth at 22c. each. He allowance for waste,

Cubical content of log is 96 c. ft.; subject content of scantling is 1596 c. in.; number of scantling is 106; cost of 106 scantling a 22c. cost is \$23.76.

23. A farmer's granary 13 ft. long 12 ft. wide is filled with wheat to the depth of 6 ft. Find its value at 66c. a bu.

25 qt.=1 e. ft.; 1 qt. is worth Se.; 1 e. ft. is worth 75c. Axs. \$702.

26. What length must be cut off a beam 9 in. broad and 15 in. deep to contain 2 c, ft. 866 c. in.? Aug. 2 ft. 8 in.

25. A stick of tir" 27 ft. long and 12 in. square weighe 14 ewt. 112 lb. What will be the length of another stick which weighs 1 t. 520 lb. and which is 9 in. wide and 8 in. thick?

1 c. ft. weighs 56 lb.; the second stick weighs 2520 lb. It contains 45 c. ft. and its length is 90 ft.

26. A cubic foot of water weighs 1000 oz.; find the weight of rain-fall on one acre 1 in. deep. Ams. 113 t. 875 lb.

27. A street 1000 ft. long and 40 ft. wide costs \$1728 for paving. What will it cost to pave one 1320 ft. long and 66 ft. wide?

- 28. A reservoir is 40 ft. 4 in. long 25 ft. 6 in. wide. How many gallons of water will be required to fill it to the depth of 18 inches? Ame. 117938 gal.
- 20. A reservoir is 280 ft. long 193 ft. wide and 48 ft. deep. How long will it take to fill it at 286 gal. per minutef Ans. 38 da. 21 hr. 20 min.
- 30. A courtyard 46 yd. sq. is to have two pavements of brick necess it through the centre, one at right angles to the other. How many bricks 8 in. long 44 in. wide will be required if the pavement is 3 ft. wide?

Pavement contains 91 sq. yd., or (91×9×144) sq. in.; 1 brick =36 sq. in. of surface; ... number required is 3276.

31. How long will it take to ride around a field 233 yd. wide and containing 44 ac. 4196 sq. yd. at 5 miles 520 yd. an hour?

The area is 217156 sq. yd.; width is 233 yd.; .'. length is 932 yd.; perimeter is 2330 yd.; one rides 9320 yd. in 60 min.; hence, he rides 2330 yd. in 15 min.

- 32. Two rectangular plots of ground are offered for sale; one 80 yd. long and 56 yd. wide for \$1120, and the other 96 yd. long and 60 yd. wide for \$1800. Which is the better purchase and by how much per sq. yd.† Axs. The latter; 64c.
- 33. A man has a rectangular block of wood 20 ft. long 6 ft. wide and 3 ft. thick; how many blocks 8 in. long 4 in wide and 2 in. thick can be out out of it? No allowance for waste.

Cubical content of the block = (240×72×36) e. in.
one small block=(8×4×2) e. in.;
number of blocks=9730 Axs.

- 86. A pond 121 ft. by 180 ft. is covered with ice 2 in. thick. Find the weight in tons of the ice if 1 c. ft. weighs 56 lb. Azm. 101 t. 1380 lb.
- 35. A rectangular cistern is 12 ft. long and 8 ft. wide inside measurements: and the water is 7 ft. deep. How many tons of water are there in the cistern. Axs. 21 tons.
- 36. A street 20 rods long and 60 ft. wide is to be paved with brick laid flat-wise, each 8 in. by 4½ in. Find the cost of the brick at \$8.50 per M.

Surface to be covered=(20×16;×12×60×12) sq. in.; Surface of 1 brick=(8×4;) sq. in.; Number of bricks=79200; Cost=4073.20.

37. A men has a field 113 rd. long, and 68 rd. wide. How many more rods of fencing will be required to enclose it then a field of the same area and 84 rd. wide?

Area of field=(112×63) eq. rds;
.'. length in rods=[(112×63)+84] rd.=84 rd.;
Perimeter of first=3×(112+63) rd. =350 rd.

***second=2×(84+84) rd. =326 rd. Difference=14 rd.

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38. A room is 60 ft. 4 in. long and if it were 15 ft. wider the area would be 3484 sq. ft.; find its width.

Width of supposed rooms 3484×144 in. =008 in.

Width of room=(608-180) in.=25 ft. 3 in. Asts.

39. How many e. ft. of lead are there in a leaden eistern 15 ft. long 10 ft. wide and 8 ft. 6 in. deep, the lead being 3 in. thick? Cubical content with outside measurement=1275 c. ft.;

=1136 c. ft. 756 c. in. .'. number of e. ft. of lead=128 e. ft. 972 e. in.

- 40. If a c. ft. of markle weighs 2.716 times as much as an equal volume of water, find the weight of a block of marble 9: ft. long 3 ft. wide and 4 ft. thick. Ams. 9,t. 333 lb.
- 41. If 6 c. in. of iron weigh as much as 45 c. in. of water, find the weight of 26 c. ft. of iron. Ans. 6 t. 187; ib.
- 42. How many ib. Troy are there in 8640 lb. Avoirdupois? Am. 16600 lb. Trey!
- . 48. A man mixes outs and peas in the proportion of 11 bu. of cate to 4 bu, of peas and the mixture is worth 55c. per bu. If the oats are worth 35c. per bu., what are the peas worth per bu.f Axs.
- 44. The floor of a room which is 15 ft. high is a square and costs \$54 for carpeting it with earpet 2 ft. wide and worth \$1.00 a yd. What will it cost to paint the walls at 30c. a sq. yd.?

Area of floor is \$24 sq. ft.; length, 18 ft.; area of walls, [3×(18+18)×15] sq. ft., or 120 sq. yd. Ams. \$66.

- 45. How many miles are there in 2640 knots? Ans. 2043 mi.
- 46. What is the value of a block of marble 5 ft. 3 in. long 2 ft. 4 in. wide and 1 ft. 2 in. thick @ \$10.56 per c. ft. ? Axz. \$150.93.
- 47. A ear oad of wheat weighing 14 t. 6 cwt. was sold for \$429. How much is that per bu. ? Am. 906.

- 46. How many days are there from June 1st to October 6th inclusive? Ame, 126 days.
- 49. If there are 2 reams in a bundle and 5 bundles in a bale and 73 reams are sold outget twenty bales, what is the remainder worth at 10c. a quire? Are, \$254.00.
- 50. A tab of butter weighed 40 lb. 12 ca.; the tab alone weighed 4 lb. 3 ca. What is the butter worth at 33c. a lb.f Ara. \$11.70.
- 51. I buy pass books at \$5.04 a green and sell them at 60c. a dozen. What is my gain on 120 bloks? Ans. \$1.00,
- 52. A hound running 64 rd. a min. is after a fex running 56 rd. a min. The fex has a start of 240 rd. In what time will it be caught? Am. 30 min.
- 53. If steel rails weigh 25 lb. to the fost in length, what weight in tone will be required for 1 mi. of railroad? Am. 66 t.
- 54. A company melted 500 lb. 6 or. 10 dwt. of silver into 125 bars of equal weight. Find the weight of each bar. Ams. 4 lb. 8 or. 10 dwt.
- 55. A barrel of beef weight 200 lb. Find the value of the beef required for an army of 2000 men for 15 da. at \$18 per bbl., if each man receives 1 lb. 4 oc. daily. Ams. \$8275.
- 86. If 15 flags of the same size and quality cost \$834 at 15c. a eq. ft., find the length of a flag if the width to 8 ft.
- 1 fing costs \$21.00; number of eq. ft. in 1 fing 166; length of fing=15 ft.=18 ft.
- 87. A farmer sold 56 bu, barley and 87 bu, sats for \$84.68 receiving 26c, per bu, more for barley than for cats. Find the price of each per bu.

If all were barley the cost=\$84.68+(87×26)e.=\$107.30; ".". price of 1 bu. barley=\$107.30÷(58+87)=74e. " 1 bu. cats =(74-26)e.=48e.

- 88. Multiply 18 mi. 120 rd. 4 yd. 2 ft. 7 in. by 60. Am. 1884 mi. 90 rd. 2 ft. 5 in.
- 50. The fore wheel of a carriage is 8 ft. in circumference and makes \$10 revolutions more than the hind one in going 4 mi. 160 rd. Find the circumference of the hind wheel.

Number of revolutions by fore wheel=21700=2970; hind (= (2970-810)=2160; hind (= 23700 ft.+2160=11 ft.

66. If a number divided by 347 leaves a remainder of 73, what will be the remainder when the same number is divided by 137 Number=247×Quetient-i-73;

Number WX Quetient+ff

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= 19×Quetient+5/4. Bomainder is 8.

- 61. From a cask containing 262 gal., 26 gal. were taken out at one time, 26 gal. at another and 17 qt. at another. How many gal. and qt. are left? Am. 118 gal. 3 qt.
- 62. A milk man had 12 cans of milk, 4 of 8 gal. cach; 5 of 3 gal. 2 qt. each and the rest 6 gal. 1 qt. each. What is the milk worth at 50. a qt.f Ams. \$13.05.
- 63. A and B have equal shares in a field of wheat which yields 284 bu. A takes 97 bu. and B the rest, paying A \$48.15. What is the value of the field of wheat? Am. \$151.94.
- 64. By what number must 68 mi. 272 rd. be divided to give for quotient 2 mi. 123 rd. 5 yd. 1 ft. 6 in. 7 Ams. 26.
- 65. A party of 35 persons direct together; each man paid 50c. and each woman 45c. The bill was \$11.87. How many women were in the party? Are. 6 women.
- 66. A man mixes 56 gal. of spirits at \$5 a gal. with 17 gal. at \$1.00 per qt., and then adds 8 gal. of water. He wishes to gain \$61 on the transaction; at what rate per gallon must be sell is?

 AMS. \$5.00.
- 67. If 3 turkeys are worth 4 geore, and 6 geore are worth 30 chickens, how many chickens can be had for 9 turkeys? Am. 46 chickens.
- 68. A dealer sold 25 M shingles at \$5 per M; 75 doors at \$2 each; 20 windows at \$1.50 each and received in payment 25 tone of seal at \$5.25 per ten and 8 cords of wood at \$4.50 per cord. How much each must be receive to balance the account. Ann. \$38.25.
- 60. A man buys 36 lb. coffee at 24c. a lb. and 50 lb. at 23c. a lb., and after mixing them sells 40 lb. at 28c. a lb. At what price must be sell the remainder to save him from loss? Axs. 30c.
- 70. A man drew 215 loads of gravel at 75c. a load. He had a boy helping-him to whom he paid 37c. a load for 114 loads. If it took him 68 days altogether, find his average daily wages. Axx. \$1.50.

71. A man cold 100 animals, turkeys and goose, for \$104, the turkeys at \$1.25 and goose at 75c. each. How many gross did he cell. See question \$7, page 252. Axz. 42 goose.

72. Silver is 10) times as heavy as water, find the weight in tone of 28 c. ft. of silver. Ans. 9 tens 275 ib.

73. How many gallons of water will a cistern held whose outside measurements are 8 ft. 4 in. long 4 ft. 7 in. wide and 2 ft. 8 in. deep (no lid). The plank of which the cistern is made is 2 in. thick.

No. gallone=(8×4}×24×44) gal.=5314 gal.

74. Twenty-seven men earned a certain sum in 13 days. Had they received \$26.61 more than they did, each would have carned \$1.31 per day. Find the daily wages of each.

Hint \$38.61 for all=11e. for each per day;
... daily wages=\$(1.21-.11)=\$1.20.

75. A man bought 120 bbl. of apples for \$200. Some at \$6 and some at \$6.50 per bbl. How many at each price did he bay. Ams. 54 at \$6; 65 at \$6.50.

76. A man buys 5000 but of wheat at 600, per bu. He coils half of it at 600, per bu. At what rate per bu, must be soil the remainder to gain 130, a bu, on the whole quantity?

His total gain=5000 × 130,=0000; His gain on half=2500 × 80,=0200; Gain on 2nd ** = 0400; Gain on 3nd half per bu.=0400; 2500=160.; Solling price=760.

77. A stick of timber is 24 ft. long 14 inches wide and 16 in. thick. If a subje yard is out off the end, find the length of the remainder.

Area of end=\f eq. ft.;
... length to centain 1 c. yd.=(27+\f) ft.=17\f ft.;
Hence, (24-17\f) ft.=6\f ft.=remainder.

78. I bought apples at 5 for 7c. and sold them at 7 for 10c. and gained 68.36. How many did I sell?

48e. is paid for 35 apples; 50e. is received for 35 apples; 1e. is gained on 35 apples; 325e. is gained on 11375 apples.

79. A man is to receive \$425 and a watch for 12 menths' work. At the same rate he receives \$204 and 2 watches for 7 months' work. Find the value of the watch.

In 34 months he earns \$650 and 3 watches; in 7 months he earns \$304 and 9 watches; in 17 months he earns \$646 and in 12 months he earns \$456; value of watch is \$(456-425)=\$31.

60. How many palings each 3 ft. 6 in. long and 2 in. wide can be made from 20 boards, each '4 ft. long and 3 ft. wide, no deduction being made for waste in cutting? Ams. 400.

81. A man bought 24 horses for a certain sum, had he get 11 more at the same rate he would have paid out \$5145 ritogether. What did he pay for 24 horses?

Oust of 35 horses-\$5145; 11 11 24 " =94×4147=43536.

82. A man has a field 96 rd. long and 48 rd. wide, how many rods of fencing will be required for a square field of half the area?

A field half the length and same width would give half the area; .'. the side of square field is 48 rd. long and the perimeter

83. What is the difference between the smallest number of 4 Ageres exactly divisible by 34, and the largest number of 4 Agures exactly divisible by 43?

Smallest No. is 1020; the largest No. is 9976. Ams. 8056.

.. 84. An equal number of mon and boys carned \$528.50 in 6 weeks. Each man earned \$7.50 in 2 weeks. Each boy carned \$6.50 in 8 weeks. How many boys were employed?

1 man carne \$22.50 in 6 weeks; 1 boy carns \$13.00 in 6 we

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I man and I boy cars \$35.50 in 6 weeks;

No. of each employed 532.50 25.50 =15. Ams. 15 boys.

85. A pile of wood was 96 ft. long 8 ft. high 4 ft. wide and 5 cords 80 c. ft. have been sold. What is the length of the remainder of the pile?

A pile 4 ft. long contains a cord; .'. length to contain 5 cords 80 e. ft. is 22† ft.; 96 ft.—29† ft.=73† ft.

96. A carpenter caras \$2.20 a day. His expenses are \$7.20 a week. How long will it take to save \$8127

In a week he saves \$(13.20-7.20). Axe. 53 weeks.

87. How many feet board measure are there in 20 scantling 24 ft. long 5 in. wide and 7 in. thick. Ams. 1400 ft.

88. A farmer sold 54 bu. of wheat and 28 bu. of oats for \$54.40. The cats were worth 40c. a bu, less than the wheat; find the value of 2 be, of wheat and 3 be, of onte,

See example 57, page 252. Axs. 42.80.

80. A man bought \$16 head of cattle. He said half of them for \$1000 and gained. \$5 each. Find the whole gain if he sails the remainder at \$12 each above cost,

Gain is \$[194×(19+5)], or \$2100.

- 90. Two men divided equal sums of money. One gave his to 19 men and the other to a number of women. Such man received \$4.75 and each women \$1.14 less. How many women were there? Axe. 36 wemen.
- 91. A number is divided by the factors 3, 11, 5; the first remainder is 2, the second is 7 and the third is 4; if the quotient is 205 find the number. Am. 47100.
- 98. A man celle 60 chickens at a profit of 30c. each; what additional number must be sell at a profit of 40c, each to realize an average profit of 37c. on each?

The additional profit on 60 at 7s. each is \$4.30; house, number required is 430s.+3s., or 140.

98. A certain sum of money was divided among A, B and C. A and B get 687.80, A and C 686.35, B and C 681.26. What did A get less than B and C together? Am. 610.80.

V. FACTORS, MEASURES AND MULTIPLES.

1. Find the prime factors of 200056 and 213002 and multiply the common factors in each together.

Prime factors of 1st=2°×2°×7°;
"2nd=2, 7, 17, 29, 31; 16.

- 8. Simplify 285×466×95×87×171, Axs. 1890.
- 8. What number multiplied by 144×27 will give the product of 864×96×747 Am. 1152.
- 4. Affix a figure to the right of each of the following so that the resulting number may be exactly divisible by 9:—473; 295; 66719; 8712. Am. 4734; 2952; 667197; 87120 or 87129.
- 5. Affix a figure to the right of each of the following so as to make the resulting number exactly divisible by 11:-7428; 1739; 7525; 3473. Ams. 74288, 17391, 75250, 24739.
- 6. Determine which of the following numbers are prime:—103, 2197, 619, 4393, 7111, 997, 499, 1793 and 581. Ams. 103, 619, 997, 400.

- .7. What is the largest prime factor common to 1861 and 1677
- S. From a heap of shot weighing 54345 grains, a heap weighing 19361 grains is taken, show that a single shot cannot weigh me then 3 grains.

19921=8×8×37×57;

\$4346-3×5×3003. Hence, the heaviest weight is 3 gr.

9. A coal dealer has 5 bins holding 162 bu., 114 bu., 265 bu., 265 bu, and 223 bu, respectively. What is the smellest number of bushels that can be exactly measured in such?

L.C.M. of the numbers-9000 bu.

- 10. A railway Co. built three switches 6000 ft., 8071 ft. and 9367 ft. long. Find the length of the longest rails that sould be used without cutting them. Ans. 20 ft.
- 11. What is the least sum of money with which I can buy horses at \$75; males at \$50; sows at \$80, or shoop at \$12, and spend all
- 12. A man has three farms of 55 ac., 73 ac. and 56 ac., and wishes to divide them into fields of the largest possible equal size. How many fields will be have?

Sine of field, 8 ac. Ams. 27 fields.

13, Find the largest number that will exactly divide 11496, 10607 and 21420 after \$1 is added to it.

H.O.P. of the Nes.=479; .. No.=(479-81)=306.

14. Find the largest number from which if 97 be taken the somainder will exactly divide 3606, 5808 and 8448.

H.C.F.=528; .'. No.=528+97=625.

- 15. Find the largest number that will divide 2235, 2231 and 4615, leaving as rereainders 68, 79 and 84 respectively. Ams. 197.
- 16. The L.C.M. of 12, 15, 16, 24 and another number prime to there is 16020. Find the number.

L.C.M. of 12, 15, 18, 24-200; 16920+260-47.

- 17. Find the L.C.M. of all the numbers that exactly contain 16 between 48 and 128 inclusive. Ams. 13440.
- 18. Find all the integral divisors of 168. Ams. 1, 2, 3, 4, 6, 7, 8, 12, 14, 21, 24, 28, 42, 56, 84, 169. See page 147.
- 19, Find the G.C.M. of 182 per, and 223 per; 1 yd. 2 ft. 6 in. A300, 11 ft.

26. Find the smallest sum of money that the be divided into sums of 54c. 62c. or 50c. ANS. \$41.56.

21: Find the two lewest numbers that can be divided by either 103 or 135 without a remainder. Ams. 605 and 516.

22. Find the greatest length of which 48 per. 1 ft., and 55 per. 5 yd. 6 in. are multiples. Ams. 13 ft.

23. A company bought 3 blocks of land containing 1030 ac.; 1176 ac.; 1272 ac. respectively. They divided them into forme of the largest possible equal size. What did they get for all at \$1200 for each farm? Am. \$57000.

24. Find the least number which, divided by any integral number between 6 and 18, will leave a remainder of 2. Ann. 27722.

25. Three bells strike at intervals of 6, 7 and 8 min. They strike together at 8 p.m. At what time will they strike together again. Axs. 48 min. past 10 p.m.

26. Find all the numbers that are exactly contained in 2300 and 3008.

H.C.F.=34; the measures of 34 are 1, 2, 3, 4, 6, 8, 12, 24.

27. A street 10 miles long has telegraph poles 150 ft. and telephone poles every 195 /t. How many telegraph and telephone poles will some together?

Total distance 52800 ft.; L.C.M. of 150 ft. and 120 ft.=600 ft.; ... 4882 ft.=86; hence, 88+1 (starting point)=89 poles,

26. Find the L.C.M. of all the composite numbers from 49 to 50 inclusive. Ams. 44629200.

29. The H.C.F. of two numbers is 305; L.C.M. is 20165; one number is 6715, find the other.

The factors of the second number not found in the first must be 20145-6715, or 3. ... 395×3=1'35=the other number.

30. Find the two smallest numbers whose H.C.F. is 79 and whose difference is 237.

Since 79 is H.C.F. and 237-79=3; hence, one number is 4 times 79. Ams. 79 and 316.

31. The L.C.M. of two numbers is 28035; the only factor of the first not in the second is 7, and the only factor in the second not in the first is 5. Find the H.C.F.

The H.C.F. is the product of all the common prime factors; ... 28085+(5×7)=801=H.C.F.

22. The H.C.F. of two numbers is 316 and the L.C.M. 3676. Find the numbers.

2476-316-11-product of the factors not common to the aumbers; numbers are 1×316 and 11×316, or 316 and 3476.

23. The product of two numbers is 2304 and the L.C.M. is 144. Find the H.C.F.

The product of the two numbers is the product of the L.C.M. and the H.C.F.; 2804+144=16. Ams. 16 and 144.

34. Find the three lowest common multiples of 24 and 36.

Their L.C.M.=73; ... the three lowest common multiples are 73×1, or 72; 73×2, or 164; 72×8, or 216.

26. The factors 7, 3, 5 are common to two numbers, the other factors in one are 3, 2, 2, and in the other 5, 7, 11. Find the H.C.F. and L.C.M. of the numbers.

H.C.F.=7×3×5=105; L.C.M.=H.C.F.×3×3×3×5×7×11= 195×12×395-495100.

35. The H.C.F. of two numbers is 30; the factors in the first not in the second are 7 and 11, and those in the second not in the first are 2 and 13. Find L.C.M.

30×7×11×3×13==90000.

27. What is the smallest number by which 722 must be multiplied to produce a number which shall be exactly divisible by H.C.F. of 1980 and 2628.

H.C.F. is 36 and 733-36 leaves a remainder of 12; 35+12-8, t is, 733 must be multiplied by 3 to make it exactly divisible by 26. AMS. 8.

36. On a reck are three revolving lights; one revolves in 132 seconds; another in 187 seconds, and the third in 304 seconds. All were seen at midnight, when next will they be seen? Axe. in 37 min. 34 me.

VI. VULGAR FRACTIONS.

- 1. A man spent \$75% and then had left \$69% more than he spent. How much had he at fret? Ams. \$220%.
- 2. By selling a quantity of wheat for \$256} I lest \$22f. For how much should it have been sold to gain \$174? Awa. \$2964\$.
- 3. A farmer exchanged 155\$ as. of land for 135 horses valued at 983 each. What is the land worth per sere? Ams. 972.
- 4. A farmer raised \$10 t, of hay on 160 ac. How many neres should yield 631 t. ? Ams. 34 ac.

- 5; Hednes S da. 21 hr. 44 min. to the fraction of a week.
- 6. A man ewning f of a best sold f of his share for \$11705.

 37nd the value of the boat and the value of the part he had left.

 Ams. \$2720; \$5050 (1)
- 7. A drover sold 504 pige at 97\$ each and invested in the proceeds in shoop at \$11% each. How many sheep did he buy?

 AMS. 189.
- 8. The fencing of a field whose area is 20025 eq. rd. cost \$140\delta_c.

 If the field is in the form of a rectangle 30\$ rd. wide, find the cost
 per rd.

Longth is 50% rd.; perimeter is 180% rd.; cost per rd.= 0(140%+186%)==0;

- 9. Two men, A and B, start to walk towards each other from London and Montreal, respectively, at the teams time, one going 9% mi. and the other 8% mi. per hr. If they ment in 24% hr.; how far is London from disentreal? Ann. 450% mi.
- 10. What part of 3 ewt. 25 lb. 2 cc. is 1 ewt. 80 lb. 10 caf
- 11. A morehant paid \$517 for apples at \$01 a bbt. and sold it of them at a profit of \$17 per bbt. How much did he receive for what he sold? Am. \$150.
- 12. If one edge of a subleal block of marble is 4 ft. 6 in. long, what will it cost to polich 4 of its faces at 61% per eq. ft.? Ass. \$100)\$.
- 13. A man divided \$ of his form between his two some giving to the younger \$ as much as to the elder. If the elder received 25 asres more than the younger, how many acres are there in the farm?

In every 16 ac. divided the difference is 2 ac.; honce, 200 ms. were divided, or \$ farm. Ans. 220 ac.

16. A travels 5692 mi. in 165 da.; B 6185 mi. in 195 da. How far will they be apart in 12 da., if they travel in the same direction, starting from the same place at the same time.

Each day A goes 562; mi.÷16;, or 33; mi.; each day B goes 618; mi.÷19;, or 31; mi.; difference in 1 day is 3; mi.; in 13 da. it is 26 mi.

15. Divide the difference between $\frac{2l}{3l}$ and $\frac{3l}{12}$ by the product. Am. 2.

16, I have \$2554. If I expend \$ of it for wheat at \$750, a.bu.; \$6 for bariey at \$650, a ba. and the rest in corn at \$150, per ba. How many bushole of each do I receive?

Wheet, 2001f bu.; barley, 1255% bu.; corn, 801ff bu.

26. Write the following functions in the order of magnitude:

Reduce to common Mamorator, then the fraction with smallest denominator will be the greatest, etc. The order is wife, wife,

- 17. Find the least number which edded to the sum of \$, \$ and \$1\$, will make the result a whole number. Axe, \$\$\frac{1}{2}\$.
- 18. Reduce refer so, to the fraction of a eq. ft. Ams. 448 eq. ft.
 - 19. Rednes Mr c. ft. to the fraction of a cord. Ann. abby cord.
- 30. What part is 15 lb. 7 cz. 12 dwt. of 27 lb. 4 cs. 6 dwt?
- 21. 13 ac. 30 eq. rd. 34 eq. yd. is the unit. Find the measure of 11 ac. 40 eq. rd. 20 eq. yd. Axs. §.
- 22. Simplify £1 2s. 11d. 1 t. 17 cwt. 50 lb. 1 cs. 15 dwt.

 Ann. 1/1. 2 t. 10 cwt. 4 cs. 7 dwt. 12 gr.
- 25. If (\$+-1/2) of an estate is worth \$6023 2s. 6d., 2nd the value of (44+-113) of it. Ans. \$2372 10s.
- 21. Find the value of \$ of 30s. 0d.+\$ of 27s.-A of So. 81, Ams. 41 as. 7\$4.
 - 25. Simplify | of | of | of 2540. Am. 4
- 26. Find the value of \$ of Se. +2 of Siz. +1 fr of £25; and reduce the nesset to the fraction of \$ of £18 180. 10d. Ans. \$.
 - 27. Find the G.C.M. of 19t, 19t, 21t. Ans. if.
 - 20. Find the L.C.M. of 24, 24, 24, 24, 24. Ars. 72.
- 99. Find the G.C.M. and L.C.M. of 22, 1, 71, 1, 1. Ann. G.C.M. -- L.C.M. -- 33.
- 30. Divide the L.C.M. of 155, 15, 15, 25 by the G.C.M. of 5, 5, 1, 1. Ans. 455-11, or 12250.
- 31. Three girls step at the same mement, and then step at intervals of \$, \$ and \$ seconds respectively. How long will it be before they again step tegether? Ass. 12 sec.

- . 32. Find the smallest fraction which whom divided by either th, sk or sk will give a whole number for quotient. Am. 4.
- 33. What is the largest sum of menoy that can be paid as exact number of times from either £3055, or £1005257 Ann. 424.

VII. DECIMALS.

- 1. At the rate of \$.015 each, how many pencils can I get for \$05.727 Ams. 2668 pencils.
- 2. A boy had corned \$130.75; he spent .57 of it for a hisyele. What had he left?

Sum left is .13×\$129.75, or \$16.006.

- 3. A man travelled 439.75 mi. in 6 dn. On each of the first 5 dn. he went an equal distance and on the sixth he went 98.25 mi. How far did he go the first da.7 Am. 66.5 mi.
- 4. A man receives \$0.12 for 4.75 days' work of 8 hr. each. What does he got per hr.f Amp. Me.
- 5. A man had 608 bu. of wheat; he said .25 of it at \$.80 per bu. and .6 of the rest at \$.73 per bu. How much did he seesive altegather and how many bu. had he left? Acce. \$605.70; 250 bu.
- of it worth at .875 no much yer yel, as the first last Ama. \$66.96.
- 7. A morehant paid \$1165 for \$7.5 pt. of cloth. Ho sold A of it at a gain of \$.165 per yd. and the rest at a gain of \$.265 per yd. Find the average celling price per yd. Ann. \$1.475.
- 8. Find the sum of .8 of a gal.+.8 qt.+.8 gt.+.8 gill. Asm. 1 gal. 1 pt.

Ness-t-gillo-Lute.

- 9. A's money is .8 of B's and B's is .75 of C's. -If C har-\$120 more than A, how much has easth? Aug. A, \$100; B, \$205; C, \$200.
- 19. The fore wheel-of a buggy is 11.25 ft, round and the hind wheel 13.5 ft. How many more revolutions will one make them the other in going 2.25 mi.f

11. A grain excellent paid \$1000 for sorn at \$.625 per bu. and sold .5625 of it for \$1000 and the rest of it for \$1000. Find the gain per bu. on each let. Am. \$.25'and \$.2125.

- 12. A let is 26.8 rd. long and 27.8 rd. wide. It produces potatons at the rate of 540 bs. per sers. Find the value of the crop at \$.65 per bu. Ams. \$800.70.
 - 13. Simplify .045 × 3.125 , 20.125 . Ams. .0015.
- 14. The fencing of a field 42.15 rd. long in the form of a rectangle and containing 1277.145 eq. rd. coot \$217.86. Find the cost per rd. ANS. 01.50.
- 15. A man owning .06 of a tract of land sold .45 of his single for \$0001.50. What is the value of the whole tract? Am. \$12750.
- 16. My watch at 9.15 a.m. on June 30th, 2000, was 12.65 min alow, but it gains .0025 hr. every 3.75 hr. How much 100 alon will is be in a week? Ars. 6.23 min.
- 17. Find the value of 2.35 of a mile. Ams. 2 mi. 2 far. 28 per. 2 ft. 2 in.
- 26. Find the value of 14.1275 of an acre. Axs. 16 ac. 20 per. 12 yd. 120.6 in.
 - 19. What decimal of a severeign is .215 of £4.16. Axe. 1.002.
- 59; Seduce 3 pk. 1 gal. 2 qt. 1 pt. to the decimal of 8 bu. Axe.
 - 21. Proce S. 142007 take 5.142007. Ann. .000000142007.
- 23. Find the desired which will become 2 when swittplied by STATE AND BAR
- 23. 28 1 2b. of motal consisting of copper and size in the pretion of .86 to .16 to mined with 2 lb. of the same metals mixed in the properties of .25 to .25, and how much copper and sine are in the s

ap=2.24 lb.=2 lb. 5.44 os.

Imflarly.

foot minimum.16 fb.;

-. S Ib.;

OHE. THADE DESCRIPT.

1. The retail price of an invoice of grecories was \$1350, but the purchaser received a discount of \$ and 12% off. What was the

Controlly of 4 of \$1000-0000.40

2. I bought 26 kegs of nails, each containing 100 lb. at 6c. a lb., but received a discount of 124% and 10% off. What was the not price?

Not prico- & of \$ of \$216-\$170.10.

3. A merchant sold goods at 20%, 15% and 10% off, and the discounts amounted to 9405. Find the list price.

20%, 15% and 10% off=28.8% off; .: 38.8% of list price=9485; List price=\$1250.

- 4. Sold goods at 25%, 20% and 16% off, and the discounts amounted to \$187.50. Find the list price. Ann. 2275.
- 8. The not price of an invoice of goods was \$1000.29, the purchaser having been allowed 16%, 16% and 10% off. What was the list price?

16%, 15% and 10% off=35.74% off; Hence, 64.26% of list price=\$1000.29. Aus. \$1660.

- 6. What is the difference between 25% off and 15% and 10% off Ams. 14%.
- 7. What is the difference between 15% and 10% off and 10% and 15% off. Am. No difference.
- 8. I bought 300 yd. of cloth far cash, the list price boding 80c. a yard, at 15% and 10% off and an additional 5% being allowed for each. Find the cost of the cloth. Ars. \$174.42.
- 9. I bought apples at discounts of 29% and 121% off. The list price was \$1.25 per bbl. How many barrels did I buy if the discount amounted to \$112.567

Single discount=30%; 30% of cost=\$112.50; ... cod=\$275.00; No. of bbl.=375÷1.25=200,

IX. PROFIT AND LOSS.

- 1. A merekant buys 400 yd. of silk for \$620; he sells 200 yd. at \$1.10 per yd. and the rest at 400. per yd. Find the gain or loss %. 300 yd. at \$1.10+100 yd. at 400.=\$370; \$370-\$320-\$50. Ame. gain 15† %.
- 2. If I buy two lots of ton, one at \$1.00 per lb. and the other at \$75 per ewt. How must I mix them to sell at \$80. a lb. and gain 10 %?

Seiling price without gain=90c. a lb.; loss on let, 10c. a lb.; gain on 2nd 15c. a lb.; proportion in mixture 8 of 1st to 2 of 2nd.

S. I paid \$70 for apples at 40c. a bushel, part being damaged were lest, and the remainder sold at 30% profit for \$00.' How many were lest?

No. of bushels bought=178; sold ==180; Loss=(175-180) bu,=25 bu,

4. My retail price for eloth is 60.75 per yd., and my gain 23} %. I sell to a customer and give him 20% discount from the retail price. Find my gain %.

of the cost is 69.75; cost is 69.8125; price to customer 68; gain on 69.8125 in 6.1875, or 68.5.

5. If a wholesaler sells at 10% profit and a retailer at 50% profit. What proportion of the price paid by a sustomer is profit?

Wholesaler's selling price is jif of cost; retailer's selling price is jif of jif of cost; profit is fit or jif of price paid.

6. A merchant selling goods at a certain price lesses 10% but if he sold them for 664 more he would have gained 8%. Find the cost of the goods.

Difference between the two prices=(10+8) % of cost=454;

7. By coiling ought at \$4.50 per out, a morehant gains 12 \$\infty\$ on his outlay. How much greater would have been his gain \$\infty\$ on his original outley had he cold at \$0. 3. ib.

119; af cost=\$4.50; .'. cost=\$4.00; 5c. a lb.=\$5.00 per cwt.; gain on \$4 cost=\$1, or \$5%; (35-124) 5=1215.

8. At what price must goods which cost \$16.80 be marked so that when sold at 25 % discount the merchant may still realize 25 % on his outlay?

\$1 cost realizes \$1.30; \$16.30 realizes 38.80)c41.25, or \$21.60, but \$21.00 is 75% of marked price. Arm. \$22.00,

9. If goods are listed at \$42 a dress and I buy at 40 % and 30 j % off, what discount must I make from the list prices in addition to 40 % to still realize 25 % on the not east?

List price=\$12; not cost=\$4.50; .'. not colling price=}# of \$4.50=\$6.00. But the sailing price at 40% of list price=\$7.20; .'. additional discount=\$(7.20-6.00)=\$6.20, or \$6\$ %.

10. An agent sold wheat for \$600 on a commission of \$15. After deducting his commission for buying at \$6, he invested the

preceeds in action at life, a.gd. If he bought at a discount of 10% and 6% off, how many yd. did he buy!

Amount to be invested in 9422.7619; cost per yd. after discounts are allowed—12.60p. Ams. 3881.46 yd.

X. COMMITTANON.

- 1. An agent sold a house for \$1500 at 175 commission. What did he send to his employer. Ann. 61826.50.
- 2. An agent's commission for seiling \$12000 worth of goods was 8415.89. Find the rate of commission. Ann. 8%.
- 3. A commission merchant sold rice on a commission of 11%, and sent his employer \$0007.50. What was the amount of commission. Am. 6148.50.
- 4. The not preceeds of sale were \$8494.45 after paying \$56.75 expenses and 31% commission. What was the amount of the make P

100%-3}%-061%; 961% of enles-68404.45-1-56.75; .'. paleone

- 5. I received \$3025 to invest in wheat at 25 commission. After recerving tay commission, how many bushels can I buy at 75c, per bushelf Ams. 5000 bu.
- 6. A merchant sold lumber on 2% commission for \$6006, and invested the proceeds in goods on 4% commission. What sam did be linvert?
- 2% commission cut5006—\$101.02;.*.\$(5006—101.92)=\$4604.08; m invested=\frac{122}{22} of \$4604.08=\$4602.
- 7. A commission merchant cold 1800 lb. of turkeys at 25c, a lb. and retained for his services \$63.50. What rate of commission did he channel

Amount received for turkeye=#\$150; \$150 gives \$22.60 commission, or 55.

8. A commission morehant page 42.25 freight, deducts commission, and sends \$82.33 to his employer as the not preceeds of a firkin of butter. Find his commission at 4%.

Freight and remittance=\$84.45; commission merchant has 4% commission, hence, 85% of calca=\$24.45; .*. his commission=#4 of -834.48=-61.08.

9. An agent sold 266 bbl. ougne, 200 lb. cach, at 4fc. a lb. Find his commission at io. a lb. Axe. \$191.25.

10. A commission merchant sold 250 bbl. sugar of 200 lb. such at 44c. a lb., and 120 bbl. syrup of 40 gal. sach at 204c. a gal. Find his whole commission at 25c.

Price of sugar—60375 syraps 1806 Total price—65371 Commission at 3 % = 6105.46.

XI. INGURANCE.

1. A house is worth \$6000, and furniture \$6000. The house is insured for \$6500 at 3% and the furniture for \$1500 at 3%. Find the cost of insurance. AMS. \$105.

2. I have a house worth \$6530 insured for \$ of its value. The premium is \$600. Find the rate. Ann. 2455.

3. Insured a store for f of its value at 21%. The premium was \$16.26. Find the value of the store.

2}% of the amount of insurance=\$40.25; .'. amount of insurance=\$1610; .'. \$ of the value of the store=\$1610; .'. value=

4. I paid \$61 for incuring a dwelling worth \$6625 at 1\$5. What fraction of its value was incured?

1#% of policy=\$61.00; policy=\$4500=# of his value.

5. A store is worth \$6200; contents, \$6240. The store is insured at \$ of its value at \$5, and the contents at \$ of their value at \$5. The policy cost \$8.35. How much was paid for the insurance?

. f of \$5200—00000; \$% of \$0000—000.00; \$ of \$6000—04000; \$% of \$4600—407.46; total cast—6(22.00+37.46+2.36)—401.00.

6. A merchant insured his stock for \$00000; \$ in the Western at 156; \$ in the Equity at 2%, and the balance in the London Mutual at 156. What was the total passions?

at 15%. What was the total premium?

15% of \$10000-\$150; 2% of \$500-\$150; 15% of \$13000-\$150.

Total premium-\$150.

7. A house was insured at 42% for 2 of its value. The company secound \$180, including \$1.50 for the policy. Find the value of the house.

Promium=#(180-1.50)=#178.80; 42% of policy=#178.50; ... policy=#4900; ... % of value of house=#4900; ... value=#6900.

8. James Smith owns # of a huniness which is insured for # of its value at 14%. His total premium is \$400. Find how much the business is worth.

14% of Buith's policy=\$1000; .'. Smith's policy=\$10000; .'. \$ of Buith's share=\$10000; .'. Smith's share=\$10000; and whole business=\$72000.

9. The contents of a conning factory were insured at 1\$%. The goods were damaged by thre and water to the extent of \$18750, which was \$ of the amount insured. If the amount of the insurance was \$ of the total value of the contents, find their value.

* \$ of incurance—\$18780; .'. incurance—\$30136; \$ of the value of

contentementalist, '. value of contentementa7500.

19. Mr. Smith paid \$100 for insuring \$ of the value of his house at 25%. Mr. Jones paid \$110 for insuring \$ of the value of his house at 25%. Find the difference in value of the two houses.

2)% of Smith's policy=\$100; ... Smith's policy=\$4000; \$ of value of Smith's house=\$4000; ... value of Smith's house=\$5000; 20% of Jones' policy=\$110; ... Jones' policy=\$4000; \$ of value of Jones' house=\$4000; ... value of Jones' house=\$4000. Axe.

TARRES. M. XIII. TAXES.

- 1. The cost of building a school house to be paid by a tax of 23 mile on the dollar was \$3795; what was the assessment? Ams. \$165000,
- 2. If a man's property is assessed at \$2000 and he pays \$67.30 taxes, what is the total amount received in taxes if the assessment is \$607200?

Tures on \$2560 --- \$67.20;

" " 0007200-(0007300× 0730)-003016.

3. The tax is \$6352.50; what is the assessment if A paye \$40.50 on \$63501

Assessment to give \$40.80-42250; .'. sessessment to give

4. The city of London requires \$12000 for building and repairs, \$7500 for salaries, \$2500 for other expenses. The 'a, rement grant is \$1500. The rest is to be raised by tax on property valued at \$6100000. Find the rate,

Amount required=#(12000+7500+2500-1500)=#20500; #100000 gives #20500; ... rate, 5 mills.

5. A farm worth \$10000 is rated by the assesser at \$ of its value. The rate of taxation is 3 mills on the dollar. Find the amount of taxes paid.

The of & of \$10000-402.50.

C. The assessed value of A's property is \$60000. He pays \$6 mills obly tax, 13 mills school tax, \$\displays \text{mill poor tax, and \$1.50 poil tax. What is the assessment of his taxes.

\$00000 at 17 mills in dellar=\$510; \$(510+14)=\$511.50.

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- 7. I own farm property worth \$6000, personal property worth \$6180 and mortgages worth \$4300. I pay 45% on \$ of the value of the farm; 5% on \$ of the value of personal property, and 3 mills the deliar on the mortgages. Find the amount of taxes. Ano. \$146.32.
- 8. In a town of 860 votors, 60000 is to be raised. Each voter pays \$1.35 poil tax and the rest is raised by uniform tax of 5 mills on the dollar. Find the assessment.

Poll tax=840×\$1.25=\$1050; assessment=1452 of \$(2000-1050) =\$770000\$.

9. A county requires \$5000 to build a bridge, allowing 3% for collecting and 5% commission on cost of bridge for inspection. What must be the accomment if taxes are levied at 4 mills on the dollar to raise the amount required?

Cost of bridge and inspection = \$(5820+291);
Sum to be raised = \$\frac{1}{2} \text{ of \$\frac{1}{2}\$ of \$\frac{1}{2}\$ of \$6111}
= \$\frac{1}{2}\$75000.

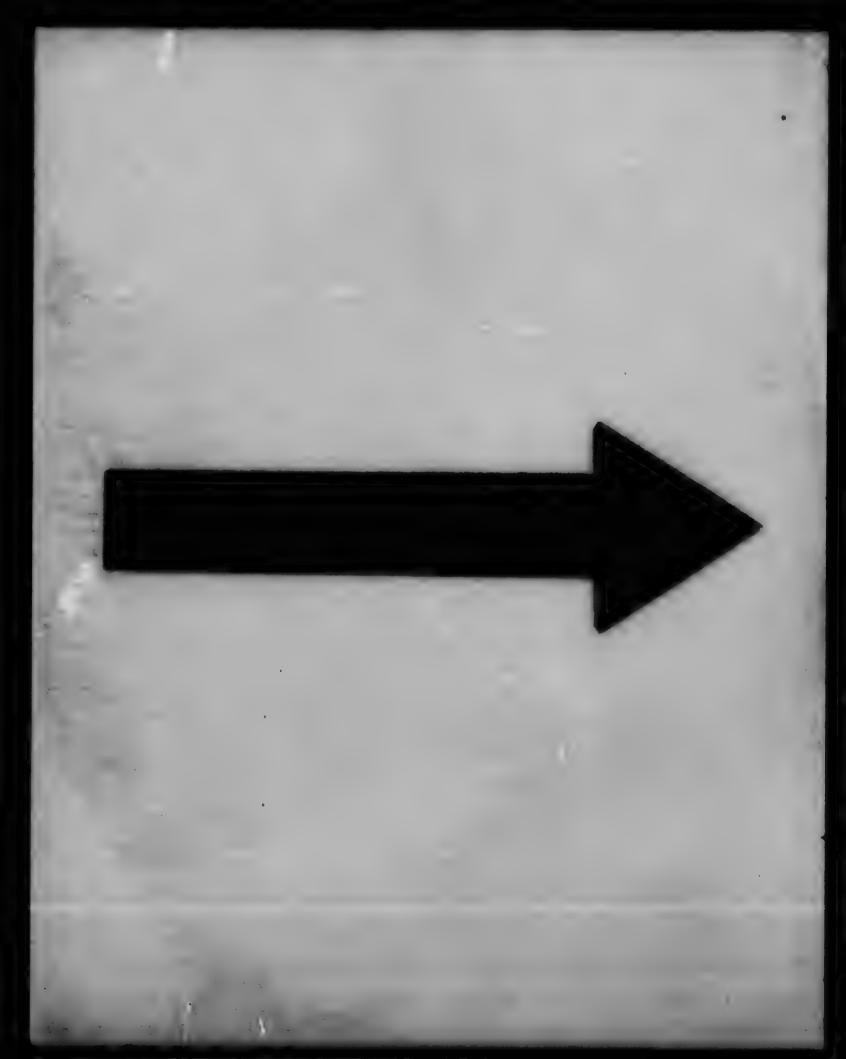
10. A town-hall is to be built for \$6006. The preperty is valued at \$600070. What will be the tax on \$10007 Ams. \$6.90.

NIM. INTEREST.

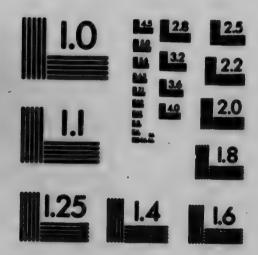
- 1. Find the interest on a note drawn Jan. 1st, 1899, and due August 5th, 1900, for \$2200 at 45%. Am. \$277.82.
- 2. What principal will amount to \$1416 at 5% from March 9th, 1887, to Oct. 14th, 1980?

Principal=### of \$1416-\$1200.

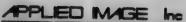
- 2. Principal \$250; interest \$32.75; time 1 yr. 6 me. Find the rate S. Am. 9%.
- 4. Principal \$468; interest \$88.28; rate 6%. Find the time. Interest in 1 yr. on \$468 at 6%=\$28.08; \$96.28+\$28.08=34; time 3 yr. 6 mo.
- 6. A certain sum of money invested at 6% simple interest for 11 yr. amounted to \$1166. In what time would it amount to \$1266.00. Ann. 13 yr. 6 me.



(ANSI and SO TEST CHART No. 2)







1653 East Main Street Rochester, New York 14608 USA (716) 462 - 0300 - Phone (716) 260 - 2600 - Fax

- 6. A friend loaned me \$463.50 at 6%, which I kept till it amounted to \$472.77. How long did I keep it. Ans. 4 mo.
- 7. \$1800 was borrowed Jan. 1st, 1999, at 5% per annum. What sum will repay the debt on October 20th? Ans. \$1872.
- 8. At what rate per cent. will a given sum double itself in 30 years? Ams. 31%.
- 9. A man borrowed a certain sum May 11th, 1898, at 6%, and on Feb. 27th, 1900, paid \$637.10, which was the amount due. How much did he borrow?

Time 1‡ years; rate 6%; amount of \$100 for given time and rate=\$110.80; ... amount borrowed= $\frac{100}{110.8}$ of \$637.10=\$575.

10. I loaned Mr. Jones a sum of money July 7th, 1897, at 8% simple interest, and on Nov. 30th, 1900, he paid the interest due, which was \$188.60. How much did I loan him?

Interest on \$100 for 3f yr. @ 8%=\$27.20. Axs. \$675.

- 11. Find the compound interest on \$2080 in 3 yr, at 4% per annum. Ans. \$259.71.
- 12. What principal will amount to \$4250 in 2 years at 5% compound interest? Ams. \$3854.875.
- 13. What is the difference between the simple and compound interest on \$1500 for 3 yr. at 6%? Ans. \$16.524.
- 14. What is the amount of \$2000 for 11 yr. at 6% per annum, payable half yearly?

There will be 3 payments at 8%; Amount=\$[2000 (1.03)*]= \$2185.45.

- 15. Find the compound interest on \$3000 for 2 years at 8%, payable half yearly. Ans. \$509.58.
- 16. Find the amount of \$1700 for 2% yr. at 4% per annum compound interest.

Amount= $\$(1700 \times \frac{188}{188} \times \frac{198}{188} \times \frac{188}{188}) = \$1893.88.$

17. Find the amount of \$6282 in 2 yr. at 31% per annum compound interest.

Amount= $\{[6282 \times (1.035)^{*}]=$6729.4355.$

18. What principal will amount to \$8279 in 2½ yr. at 3% compound interest?

Principal= $\$[8279 \times \frac{189}{189} \times \frac{100}{101}]$ = $\$[8279 \times (\frac{189}{189})^2 \times \frac{189}{101}] = \$7688.432.$ 19. What is the difference between the simple and compound interest on \$1250 from June 30th, 1898, to December 31st, 1900,

Amount=\$[1250 (\frac{188}{188}) (\frac{108}{108}) (\frac{184}{108}) = \$1516.32; ... compound interest=\$(1516.32-1250)=\$266.32; Simple =\$250: . difference=\$16.32.

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20. Find the amount of \$1080 for 31 yr. at 31% compound interest.

Amount= $*[1080 \left(\frac{103\frac{1}{2}}{100}\right)^{6} \times \frac{101\frac{1}{2}}{100}] = *[1080 \left(\frac{1}{2}\right)^{6} \times \frac{1}{2}] = *1211.50.$

XIV. BANK DISCOUNT.

1. A note of \$1850 was dated Oct. 19th, 1899, payable in 5 mo. and discounted Dec. 17th, 1899, at 4%. Find the proceeds.

Time, 95 days; rate, 4%; interest on \$1350 for given time and rate=\$14.05; proceeds \$1335.95.

2. \$750. LONDON, June 1st, 1900.

Eleven months after date, for value received, I promise to pay J. M. Northcott, or order, seven hundred and fifty dollars with interest at 8%. REGINALD HOWARD.

Discounted Jan. 15th, 1901, at 5%. Find the proceeds. Ams. \$792.98.

3. A note for \$1314, dated Jan. 1st, 1899, is payable in 3 mo. and is discounted Feb. 12th, at 21%. Find the discount.

The note is legally due April 4th; number of days from Feb. 12th to April 4th=51; interest on \$1314 for 51 da. at 21%=\$4.59.

4. A note for \$600 dated Oct. 12th, for 60 da. at 6% interest was discounted Oct. 15th at 6%. Find the proceeds.

The note is due Dec. 14th; time of discount, 60 days; amount of note when due at 6%=\$606.214; interest on \$606.214 for 60 days=\$6.06; net proceeds \$600.15.

5. For what sum must a 70 day note be drawn without interest so that when discounted at the bank at 6% the proceeds will be

Discount on \$100 for 73 da. @ 6%=\$1.20; note to produce \$98.80=\$100; note to produce \$573.90=\$580.87.

6. The discount on a note for \$1825, legally due on 21st August and discounted June 24th, was \$40.60. At what rate was it dis-

Time 58 days; interest \$40.60.

Interest on \$100 for 365 da. = \$100 × 365 × 40.60 =\$14. Ams. 14%, 58×1825

7. The face of a note is \$900; date Feb. 8th, 1900; time 90 days; interest 5%; discounted Feb. 20th, 1900, at 6%. Find the proceeds.

Amount of note when due in 93 days=#072.23; Discount off #072.23 at 6% for 81 da.=#12.945; Proceeds=#(972.23-12.945)=#059.285.

3. I wish to use \$3224.20 for 2 mo. For what sum must I give my note that when discounted at the bank at 12% per annum I shall receive that amount. Days of grace not taken.

Face of note=134 of \$3224.20=\$3290.

Tonomro, Dec. 23rd, 1900.

Three months after date, for value received, I promise to pay Frank Stover, or order, sixteen hundred dollars with interest at 6%. Discounted Jan. 9th, at 6%; no days of grace. Find proceeds.

Amount of note at maturity=\$1624; due March 23rd; term of discount 73 da.; interest on \$1624=\$19.48\$. Axs. \$1604.51\$.

10. Find the face of a 70 da. note that will yield \$1482 when discounted at 6%.

Face of note-set of res of face of note-\$1483. Ams. \$1500.

XV. STOCKS.

1. Find the cost of eighty \$100 shares of Bank of Ontario steek at 121; brokerage, \$5.

Cost of 1 share=\$(121+1)=\$1211; ... dost of 80 shares=

2. What sum must I invest in 5% stock at 108 to yield an income of \$720?

Investment to yield \$5- \$103; ... investment to yield \$720-

3. What income will I derive from \$6240 invested in 5% stock at 1047

Income from investing \$104=\$5; ... income from investing \$6240=\$300.

4. A man bought bank stock at 31% discount, and sold at 41% premium, and gained \$960 by the transaction. Find the par value of the stock.

\$8 is gained from \$100 stock; ... \$960 is gained from \$12000 stock.

5. Which is the more prefitable investment—\$46000 in 7% stock at 90, or the same sum in 10% stock at 130, and how much?

Income from 1st—\$3640 "2nd—\$3600 The 1st is better by \$40

- 6. A man invests 40% of his capital in 4% stock at 90 and the remainder in 7% stock at 135; which yields him an income of \$2200 a year. Find his capital. Ann. \$45000.
- 7. What rate per cent. do I receive on my money by investing in stock at 95\$, brokerage \$, and paying a yearly dividend of 8%. \$100 stock costs \$(95\$+\$), br \$96; ... \$96 yields \$8 interest and rate=8\$%.
- 8. If I buy stock at 115 and thereby realize 6% on the investment, at what rate should I have bought it to realize 7;%?

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Rate= $\frac{6}{74}$ of \$115=\$92.

- 9. I bought \$9500 stock at 75, at what price must I sell to gain \$570?
- \$9500 stock at 75 cost \$7125; ... s. p.=\$(7125+570)=\$7695; ... selling price of stock=81.
- 10. Sold stock at 171% discount and realized 10% on my money. Find the rate of discount at which I bought.

XVI. EQUATION OF PAYMENTS.

- 1. A debt of \$600 is to be paid as follows:—\$150 at once, \$150 in 6 mo., \$150 in 12 mo. and \$150 in 18 mo. When should it all be paid together? Ams. 9 mo.
- 2. A man lends \$10000 in four sums. He gets 3% for \$2000; 3% for \$4000 and 5% for \$2500. What per cent. must be realize on the remainder, if his average rate is 34%?

Interest from \$(2000+4000+2500)=\$325; total interest at 3\frac{1}{2}\frac{1}{

- 3. A merchant purchased goods on April 1st, 1900, as follows:
 —\$700 on 2 mo.; \$1000 on 3 mo., and \$1400 on 6 mo. eredit.
 What is the equated time of payment? Ans. 4% mo., or Aug. 5.
- 4. I borrowed \$720 for 10 mc. and \$1080 for 8 mc. I paid \$1200 at end of 7 mc. How long after the equated time for the payment of the whole may I keep the balance?

Equated time for payment of all, 9\$ mo.; \$1200 is paid 1\$ mo. before it is due and hence \$600 may be kept 3\$ mo. after it is due.

- 5. If & lends B \$1250 for 6 me., how long ought B to lend A \$900 to repay the favor? Ams. 9 me.
- 6. E owes F \$4800 payable in 8 mo. without interest. At the end of 2 mo. he pays \$1200; in 3 mo. \$1600, and in 4 mo. \$400. How long should E be allowed to keep the remainder after maturity?

The interest on the money paid before it is due is equal to the interest on \$16800 for 1 mo.; hence, \$1600, the remainder may be held 1800 mo. after it is due. Ars. 10j mo.

XVII. PARTNERSHIP.

- 1. A, B and C sell grain for \$2550. How much should each receive if for every 4 bu. A sells, B sells 5 bu.; and for every 2; bu. B sells, C sells 3 bu.? The grain is all equal in quality and price per bu. Ams. \$680, \$250, \$1020, respectively.
- 2. A and B enter into partnership with \$4500 and \$6750 respectively. In 8 mo. A puts in \$3750. 15 mo. from the beginning their profits were \$3120. How should they be divided? Ann. A=\$1500; B=\$1620.
- 3. A, B and C agree to pay a hotel bill in the proportions of 4, 5 and 6, respectively. A pays the first day's bill, \$12; B pays the second day's bill, \$14.50; and C the third, \$15.50. How must they settle accounts?

Amount of bill=\$42; A should pay 4, or \$11.30; B 4, or \$14; C 12, or \$16.80; .*. C must pay A 80c. and B 50c.

4. A began business with \$4500 and is joined by B with \$13500. They divide the profits equally at the end of the year. When did B join?

B's capital for 4 mo.=A's for 12 mo.; . B joined 8 mo. after A began business.

5. A and B rent a pasture for 10 mo. at \$6 per mo. A has 10 horses for 9 mo. How many can B put in for the remaining mo. if he pays \$12 less than A?

A pays \$36; B, \$24. \$36 pays for 90 horses for 1 mo.; ... \$24 pays for 60 horses for 1 mo. Ans. 60 horses.

6. A, B and C join in partnership. The capital is contributed in the proportion of 1, 1, 1 respectively. In 4 mo. A takes out

one-half of his, and at the end of the year the profits amount to \$5200. What should A receive?

Capital of each in the proportion of 6, 4, 3; A's=48 for 1 mo., B's 48 and C's 36; ... A gets 155=11 of gain=11 of \$5280=\$1920.

7. Three brothers, John, James and Henry engage in business with a capital of \$20000. John puts in \$2000 more than James, and James \$1500 more than Henry. The profits amount to \$1360. What amount should John receive?

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John's capital=\$8500; James', \$6500; Henry's, \$5000; .'. John receives for of \$1360, or \$578.

- 8. A and B enter into partnership with a capital of \$6390, and the gain is \$8550, of which A takes \$250 more than B. How much capital had each?
- A=\$3420; B=\$2970.

 9. A, B and C are partners; A's money is in 9 mo., B's 8 mo., C's 7 mo., and they gain \$600, \$1000 and \$1050 respectively; if A's capital is \$4500, what is B's and C's?

A's monthly gain=\$100; B's \$125; C=\$150; .'. if \$4500 gives \$100 a mo. for A; then B's capital=\$5625; C=\$6750.

10. A man left his property to his children in the following proportion 1, 1 and 1. His property amounted to \$14976. What should each receive? Ams. \$6912, \$4608, \$3456.

XVIII. APPLICATION OF INVOLUTION AND EVOLUTION.

- 1. Find by factoring the sq. root of (a) $12\times35\times105$. (b) $8\times14\times21\times27$; (c) $21\times77\times132\times6\times24$. Ans. (a) 219; (b) 252; (c) 5544.
- 2. A sq. field contains 18 ac. 36 sq. rd. Find the cost of fencing it at 68 c. a.rd.

Perimeter=216 rd.; ... 216×684c.=\$148.50.

3. A man has a field three times as long as it is wide, containing 37 ac. 155 sq. rd. What will fencing it cost at \$1.75 per rd.?

Number of sq. rd.=6075. Divide field into three equal parts by lines parallel to the end and each part will be a square and contain 2025 sq. yd. Width is 45 rd. and length 135 rd.; perimeter 360 rd. Cost=360×\$1.75=\$630.

4. A boat in crossing a river 736 yd. wide landed on the opposite side 273 yd. farther down the stream. How far are the starting and landing points distant from each other in a straight line?

 $(\sqrt{736^{\circ}+273^{\circ}})$ yd.=785 yd.

- 5. What distance would be saved by walking along the diagonal instead of the two sides of a rectangular field 66 rd. wide and 84 rd. longf. Ams. 42 rd.
- 6. How much more fencing would be required for a field 100 rd. long and 00 rd, wide than a square field of equal area? Are. 30 rd.
- 7. The diagonal of a square field is 84 rd.; find the diagonal of another square field 4 times as large. Ams. 168 rd.
- 8. A pile of wood in the form of a rectangular solid is 48 ft. wide, 36 ft. high and 216 ft. long. If it were in the shape of a cube what would be the length of one edge? Axe. 72 ft.
- 9. A subject block of stone contains 2406104 c. in.; what is the area of its faces? Ams. 748 eq. ft. 24 eq. in.
- 10. A river is 880 mi. long 2640 ft. wide and 12 ft. deep; find the depth of a subject reservoir that would hold all the water in the river.

Depth of recervoir=(**880×5280×2840×12) ft.=5280 ft.

- 11. Find the area of a triangle whose sides are 52 ft. 56 ft. and 60 ft. Ams. 1344 sq. ft.
 - 12. Find the value of 4 \$\sqrt{5625} \times 8 \sqrt{19688} \div 4. Ars. 4060.
 - 13. Find the value of 8 \$\square 4096 \div 4096 \div 4 \square 82768. Axs. 4.
- 14. The surface of a cube is 3750 eq. ft.; find its solid centent.

 ATAR eq. ft.=625 eq. ft.=surface of one face; side=25 ft. Axs.

 15025 c. ft.
- 15. Find the area of the largest circle that can be drawn in a square, 56 in. on each side.

Area of sirele=(28°×4°)sq. in.=2464 sq. in.

- 16. If a horse is tied to grase on an acre, what is the length of the rope?

 Radius=(\sqrt{4840-48}) yd.=39.24 yd.
- 17. The volume of a subleal block is 60698.457 c. ft. Find its surface.

7 60698.457=edge=39.3 ft.; surface=[6×(39.3)*] eq. ft.= 9266.94 eq. ft.

18. A square field contains 5 ac. 46 rd. 8½ yd. How many acres are there in a rectangular field whose adjacent sides are respectively 82 yd. and 72 yd. longer than the former?

Side of square field= $(\sqrt{25600})$ yd.=160 yd.; area of rectangular field= (242×232) sq. yd.=11 as, 96 sq. rd.

- A rectangular vessel is 143 in. wide, 1873 in. long and 13 in. deep.
 Find the side of a subject vessel of equal capacity.
 Side of vessel=[∮(143×13×1573)] in.=143 in.
- 20. Find the contents of a subisal eletern that contains 17150 gal. of water.

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Side of eistern= $[\sqrt[4]{(17150 \times \frac{16}{624})}]$ ft.=14 ft.

21. How long will it take to ride around a square field containing 52 ac. 324 sq. yd. at 3j mi. an hr.f

Perimeter=2008 yd. Ams. 19ff hr.

22. A square field contains 8 ac. 121 eq. yd.; another field in the form of a rectangle contains 4 ac. 160 eq. yd. more, and is 56 yd. wider. Find its length.

Longth of side of 1st field=121 yd.; area of 2nd=7 ac. 281 aq. yd.=34161 aq. yd.; width of 2nd=(121+56) yd.=177 yd.; ... length=(34161+177) yd.=193 yd.

23. A square plot contains \$24464 sq. yd. What will be the area of a rectangular field whose length is three times and breadth twice as much?

Area=(3×2×824464) sq. yd.=4946784 sq. yd.

24. The area of 6 faces of a cube is 37\frac{1}{2} sq. ft., find its weight assuming that a cu. ft. weighs 1648 os.

Side of enbe=2.5 ft.; .. en. content 15.625 en. ft.; (1648× 15.625) on.=25750 on.

25. By what number must the following be multiplied to make them perfect squares?

775; 539; 42526, and 972. Factors of $775=(5\times5)\times81$; ... other factor 31; similarly the other numbers require 11; 21; and 3 respectively.

- 26. What is the area of an isosceles triangle whose base is 12 ft. and each of the equal sides 10 ft.? Ans. 48 sq. ft.
- 27. Find the area of a triangle whose sides are 409 ft., 169 ft. and 510 ft. long. Ams. 30600 sq. ft.
- 28. By what number must the square of 126 be multiplied to become a perfect cube ?

 $126^3=2\times3\times3\times7\times2\times3\times3\times7=2^5\times3^5\times3\times7^2$; hence, the multiplier is $2\times3^5\times7$, or 126.

29. Find the largest perfect square contained in 2016. The factors are 2°×3°×7; ... highest sq. No.=144.

. 30. What is the least number by which the following may be multiplied to make them complete squares: -48, 252, 2000?

48=4°×3; '.' 3 is the multiplier; similarly 7 and 30.

31. Find the smallest perfect cube that contains 296 without a remainder.

288-2°×2°×3°; number required=2°×2°×3°=1728.

- 22. Find the smallest square and cube numbers which contain both 12 and 27 as factors.
- L.C.M. of 27 and 12=108; the factors of 108 are 2°×3°×3; .'. square number=2°×3°×3°=324; cube number=2°×3°=216.
- 29. What perfect square factors are contained in 33075. Ams. 9, 25, 49, 225, 441, 1225, 11025.
- 34. A farmer owns a farm in the form of a rectangle 58619 ft. long, and 18491 ft. wide. How many more rods of fencing will it take to enclose it than a square farm of equal area?

Side of square field= (1/58619×18491) ft.=32923 ft.; perimeter of rectangle=154220 ft.; perimeter of square=131692 ft.; difference=22528 ft.=1365} rd.

- 35. What is the 5th power of the square root of .0004? 1.0004=.02; (.02)*=.0000000022,
- 36. Find the area of a circular ring of which the inner and outer diameters are 73.6 ft. and 106.4 ft. respectively. Axs. 4638# sq. ft.
- 37. Find the volume of the moon whose radius is 1080 miles. Axs. 5278793142# c. mi.
- 28. Find the quantity of iron in a spherical shell whose inner and outer radii are 10% in. and 14 in. respectively.

Quantity of iron=(\$\display*\frac{4}{2}) (14*-10\display*)c. in.=6647\display* c. in.

39. Find the weight of a 12 inch shell of iron, the iron being 1 in. thick, if a c. ft. of iron weighs 444 lb.

Quantity of iron= (4×4) $(6^{\circ}-5^{\circ})$ c. in.=1144 c. in.; weight (\frac{1144}{3\times 1728} \times 444) lb.=97## lb.

XIX. METRIC SYSTEM.

- 1. How many times will 84 m. go around a circular disk 7 cm. in circumference? Ans. 1200 times.
- 2. If the diameter of a cent is 25 mm., how many of them placed in a continuous straight line will reach a kilometre? Axe.

- S. A bicycle wheel being 2 m. 28 cm. round, what distance has been passed over when it has made 7930 revolutions? Ams. 18.0804 Km.
- 4. A draper bought \$5.54 m. of cloth, and so'd at one time 17.5 m., at another 6.5 m., at another 19.25 m., . Tanother 23.84 m. How much had he left? Ams. 18.45 m.
- 5. A train goes 72 Km. per hour. How many metres does it go per second? Axs. 20 m.

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- 6. A metre equals 39.3708 inches. How many millimetres are there in one inch? Axs. 25,3005.
- 7. How many litres remain after taking 3947 cl. from a each containing 2.75 Hl. Ams. 235.53 l.
- 8. If 2.25 litres of milk cost one franc, how many hectolitres could be bought for 73 francs? Ams. 1.6425 Hl.
- 9. Find the difference in grams between 68.575 Kg. and 4962.5 Dg. Ams. 18750 gr.
- 10. How many square metres are there in a floor 5.64 m. long and 4.75 wide? Axs. 26.79 sq. m.
- 11. What is the number of square metres in a path 38.40 m. long and 85 cm. widef Ams. 32.64 sq. m.
- 12. Find the number of hectares in a rectangular plot 1.225 Km. long and 556 m. wide. Ams. 68.11 ha.
- 13. A train leaves Lyons at 10.30 a.m. and runs 45.64 Km. per hour. At what rate must a train run which leaves 45 min. later and overtakes it at 15 min. past 2 p.m.? Ams. 57.05 Km.
- 14. If the interest on 568.25 fr. for 3 years is 127.86 fr. Find the rate of interest.

Rate=
$$\left(\frac{100}{568.25}\right)$$
 of $\frac{1}{2}$ of 127.86 %=7.5% nearly.

- 15. It costs 688.5 fr. to dig a ditch whose depth is .68 m. and width .48 m. If the cost of digging is 6.75 fr. per c. m., find the length in kilometres. Ams. .3125 Km.
- 16. The area of a field is 5.695 hectares. Find its size in acres, rods, etc.
- 1 hectare=11960 sq. yd.; ... 5.695 hectares=5.695×11960=68112.2 sq. yd.=14 ac. 11 sq. per. 19 sq. yd.
 - 17. How many grams are there in 1 lb. avoir.? Ams. 451.61.

. 18. How many area are there in 90 acres?

1 are=119.0004 eq. yd.; 00 ac.=90×4840 eq. yd.=435000 eq. yd.; No. of aree=435000+119.0054=3041.976.

19. How much is a pile of wood 20 ft. long 4 ft. wide and 5 ft. high worth at \$1.25 per store?

1 stere-35.316 e. ft. i.

Value of wood= 20×4×5 25.316 ×01.25=014.157.

20. A man divided 5 Hl. of wheat among 20 persons. How many litres did each receive?

Share of each=A H1,-44 1.-25 1.

21. If a person steps 80 cm. at each step, how many steps will he take in walking around a square field containing 18 hectares

18 hoctares 626 eq. m.=180625 eq. m.; .*. side of field= (1/180625) m.=425 m.; number of steps=118848=2125.

23. A elstern is 4 m. long 24 dm. wide and 80 cm. deep. Find its capacity in litres.

Capacity=(400×240×80) e. cm.=7080 l.

23. At 62c. a litre, find the cost of 9 l., 8 dl. of molasses. 9.8 litres at 62e. = \$6.076.

24. How many letters, each weighing 3.5 g. will be required to weigh 1.75 kg.f Axs. 500.

XX. WORK PROBLEMS.

1. A can cut 8 ac. in 4 hr.; B, 8 ac. in 5 hr. They cut 10 ac. together for \$3.99; what share should each gut?

In 1 hr. A cuts # ac.; B, # ac. t . . money is divided in proportion of \$ to \$, or of 10 to 9. A's share-18 of \$3.99-\$2.10; B's, \$1.89.

2. A can do as much work in 3 da. as B can in 4 da. If B has done i of a work in 12 da., how long will it take both to finish it?

B can do the work in 24 da.; A, in \$ of 24 da., or 18 da; . . A and B do vi in 1 da., or i the work in 5; da.

3. A can cut a field of grain in 24 hr., B in 10 hr. and C in 27 hr. They work together for 47 hr. and then A finishes the work. How long did A work altogether?

A, B and C do iff of work in 4 hr.; time for A to do At of work=(44 : 44) hr.=47 hr. Ans. 9 hr.

4. A and B do f of a work in 2 da. and then B finishes it in 4 da. In what time could A do the work?

A and B do A in 1 da.; B A in 1 da. Ans. 32 da.

- 5. 12 men can do a work in 17? da. How long may 4 remain away and yet finish in the same time by bringing 9 men more with them?
- 4 men do † of work in 17† da.; .'. 13 men do † of work in 5† da.; .'. time 4 men may remain away= (17†-5†) da.=12f da.
- 6. A certain number of men mow 4 ac. in 3 hr. and a certain number of others mow 8 ac. in 5 hr. How long will it take to cut 11 ac. all working together?

First lot mow 1½ ac. in 1 hr.; second lot mow 1½ ac. in 1 hr.; both mow 2½ ac. in 1 hr. .'. time to mow 11 ac. $=\frac{11}{214}=3$ hr.

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7. A and B agree to do a work for \$5.60. A could do it in 7 da., B in 8 da. Together, with a boy, they do it in 3 da. How much should the boy get?

A carns 80c. and B 70c. a da., and both in 3 da. carn \$4.50; ... boy carns \$(5.60-4.50), or \$1.10.

8. A can do † of a work in 8 da.; B † of the remainder in 5 da., and C could finish it in 4 da. What time will it take for all working together to do the work?

A can do it in 24 da.; B in 123 da.; C in 15 da.; .'. altogether in 5 A.

XXI. CLOCK PROBLEMS.

1. Two clocks, one of which gains 5; min. a day and the other 3; min. per day, are set right on Tuesday at noon. In what time will one be half an hour ahead of the other?

Time for one clock to gain 14 min. on the other=1 da.;

- 2. At what time between 9 and 10 o'clock s.m. is the hour hand 31 minute-spaces in advance of the minute-hand? Ans. 17 min. past 9.
- 3. Two clocks gain and lose equally 25 sec. in 8 hr. They are together at noon. How long before they will differ in time by 1 hr.† Axs. 24 da.

4. A watch is right at noon but loses time at the rate of 4%. What is the true time when the watch shows 12 o'clock at night?

96 min. on the watch=100 min. true time;

... $(12\times60)^{44}$ 44 44 $= \frac{12\times60\times100}{96}$ min. true time=12\frac{1}{2} hr.

5. At what time is the number of minutes past 5 equal to † of the number of minutes to 6?

No. of min. past 5=# of (60-No. of min. past 5). Ans. 5.22#.

- 6. One clock gains 4 min. in 6 da. and another loses 1 min. in 24 hr. They are together at noon; when will they differ by 15 min.? Time to differ 13 min.=1 da.; ... time to differ 15 min.=9 da.
- 7. A man walking, finds on looking at his watch that the hands are at right angles, and when he has gone 1920 yd. they are together for the first time. At what rate per hour is he travelling?

The hands are 15 min. apart and will be together in 16 $^{\circ}$ min.; distance walked in 60 min. = $\frac{60 \times 1920}{16 \, ^{\circ}}$ yd. =4 mi.

8. I looked at my watch between 8 and 9 o'clock and also between 9 and 10, and found the hands had changed places. What time was it when I looked first at my watch?

When the hands have changed places, the sum of the distances moved must be an exact number of times around the face (in this case, once), or 60 min.-spaces. The hr.-hand goes is and min.-hand if of the distance. The hr.-hand goes is of 60 spaces, or 47s spaces. This is the distance the min.-hand was ahead when I first looked; ... it has gained 447s spaces since 8 o'clock. 11 spaces are gained in 12 min.; 447s spaces are gained in 4874s min. Time, 4874s min. past 8.

9. I looked at my watch between 11 and 12 and again between 2 and 3 and found the hands had changed places. At what time did I first look? Ans. 9% min. past 11.

XXII. PROBLEMS INVOLVING VELOCITIES.

1. A hare is 810 yd. ahead of a hound and takes 10 leaps of 7 ft. each in 6 pecon.ls, the hound takes 12 leaps of 9 ft. 41 in. each 3 seconds. How long before the hound will catch the hare?

Hare goes 70 yd. in 18 second; Hound 4 225 4 4 18 4 1 gains 155 4 4 18 4 4 310 4 4 36 4 2. A train 176 yd. long passes a telegraph post in 6 sec., and passes a man in another train going in the opposite direction in 3† sec. At what rate is each train running?

1st train goes 176 yd. in 6 sec.; ... 60 mi. per hr.

Distance travelled by 1st train in 3\(\frac{1}{2}\) sec.=100\(\frac{1}{2}\) yd.;

2nd '' 3\(\frac{1}{2}\) sec.=(176-100\(\frac{1}{2}\)) yd.;

2nd '' 1 hr. =45 mi.

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8. A can run 400 yd. in 42 sec.; B, 500 yd. in 56 sec. How much start must B have to come out even with A in a 200 yd. race? A runs 400 yd. in 42 sec., or 200 yd. in 21 sec.; B runs 187‡ yd. in 21 sec.; ... start=(200-187‡) yd.=12‡ yd.

4. In running 1760 yd. A beats B 32 yd. and C by 48 yd., by how much can B beat C in 1296 yd.?

A runs 1760 yd. while B runs 1728 yd., or C 1712 yd. ... B runs 1728 yd. while C runs 1712 yd., and 1296 yd. while C runs 1284 yd.; ... B beats C by 12 yd.

5. A man in a buggy goes 6 miles per hr. and starts at 8 a.m. A boy on a bicycle starts 1 hr. 50 min. later and overtakes the man at noon. At what rate did the boy ride?

The man goes $4\times6\frac{1}{2}$ miles=26 miles; the boy goes 26 miles in $2\frac{1}{2}$ hr., or 12 mi. per hr.

6. A man standing at a station noticed a train pass him in 10½ sec.; and that it passed completely over the distance between two posts 108 rd. apart in 37½ sec. Find the length and rate of the train.

7. The Imperial Limited travels from Montreal to Vancouver, 2700 miles, in 99 hours, but in the last half of the journey it goes 60 miles in the same time it took to go 50 miles in the 1st half. Find its rate per hour in the 2nd half of the journey.

Time to make the journey at 5 mi. for the first half and 6 mi. for the 2nd half= $(\frac{1450}{5} \times \frac{1450}{5})$ hr.=495 hr.; this time is $\frac{495}{99}$ times as long as the actual time; ... the actual rate for 2nd half was $\frac{485}{99}$ as fast as 6 mi., or 30 mi.

8. A train running 25 mi. an hr. is 60 mi. ahead of another which runs 15 mi. in † of the time it takes the first to run 25 mi. How long will it take the fast train to overtake the other?

Rate of fast train per hr.=45 mi.; time to gain 60 mi.= $\frac{60}{45-25}$ hr.=3 hr.

9. A train running 45 mi. an hr. crosses a bridge 240 yd. long in 36 sec. Find the length of the train.

Distance train goes in 36 sec. 36×45×1760 yd.=792 yd.; 60×60 length of train=(792-240) yd.=552 yd.

- 10. A man can row 3 mi. an hr. in still water. How long will it take him to go 12 mi. down stream and back again if the stream flows 1 mi. per hr.f Axs. 9 hr.
- 11. A train travels 25 mi. in 7 hr.; find its rate in feet per min. Ams. 3142\$ ft.
- 12. A boat runs 24 mi. down stream in 11 hr. and 15 mi. up stream in the same time. After running down for 9 hr., how long will it be in returning? Ans. 14f hr.
- 13. A can run 8 mi. and B 7 mi. per hr. How much start can A give B in a mi. race; and yet win by 44 yd.?

A runs 1760 yd., B runs (including start) 1716 yd. While A runs 1760 yd., B runs i of it, or 1540 yd. ... (1716-1540) yd.=176 yd.

14. Two trains start from Toronto for the same place, one at 8 a.m. at 25 mi. an hr., the other at 10 a.m. at 30 mi. an hr. The faster arrives 1 hr. ahead of the other. Find the distance travelled.

Distance gained by faster train=(2×25+25) mi.; time to gain 75 mi.=1 hr.=15 hr.; distance travelled=(15×30) mi.=450 mi.

15. A train running 30 mi. per hr. overtakes a man going 5 mi. an hr. and passes him in 18 sec. Find the length of the train.

Distance gained by train in 1 hr.=25 mi.; distance gained by 18×25×1760 yd. =220 yd.; length of train=220 yd.

16. A can walk 10 mi. in 22 hr.; B, 11 mi. in 23 hr. They start to walk a race of 55 mi. Which will win and by how much time? A walks 10 mi. in 21 hr., or 55 mi. in 121 hr.; B walks 11 mi. in 21 hr., or 55 mi. in 124 hr.; .. A wine by (124-128) hr.=

71 min.

17. A train going 40 mi. an hr. takes 18 sec. to pass another standing on a switch. Find the length of the moving train if the other is 192 ft. long.

Distance travelled by train in 18 sec.= $18 \times 40 \times 5280$ ft., or 1050 60×60 ft.; length of train=(1056-192) ft.=864 ft.

18. A man can row down stream 16 miles per hr., and up 8 miles per hr. How far can he go down stream so as to be back at the starting point in 12 hours.

Time to go 1 mi. down stream and back=(1+1) hr.; Distance gone down and back in 1 hr. =1 mi.;

19. A train 418 yd. long overtakes a man walking at 3 miles an hr., and passes him in 15 sec. Find the rate of the train in miles per hr.

Distance the man goes in 15 sec. =22 yd.;

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" train " 1 hr. =
$$\frac{60 \times 60 \times (418+22)}{15 \times 1760}$$
 mi.=60 mi.

XXIII. MISCELLANEOUS EXERCISES.

- 1. Simplify $\frac{5\frac{4}{4}-\frac{1}{4} \text{ of } 15\frac{3}{4}+2\frac{1}{4}+2\frac{1}{4}+2\frac{1}{4}\times 2}{\frac{1}{4} \text{ of } 7\frac{1}{4}-5\frac{1}{4}+3\frac{1}{4}}$.=Ans. \frac{1}{4}.
- 2. A train 264 ft. long takes 10 sec. to cross a bridge 132 ft. long. Find when it will be 25 miles farther away.

Train goes (264+132) ft., or 396 ft. in 10 sec., or 2376 ft. per min. No. of feet in 25 miles=(25×5280) ft.;

$$\therefore \text{ time} = \frac{25 \times 5280}{2376} = 55 \frac{1}{8} \text{ min.}$$

3. I buy three town lots whose cost is in the proportion of 4, 3, 2. I sell them at once and gain 10% on the first, 6% on the second and lose 4% on the third. My whole gain is \$505. Find the value, of each lot.

\$4 investment gives 40c. gain; \$3 investment gives 18c. gain; \$2 investment gives 8c. loss; ... \$9 investment gives 50c. gain; \$9090 investment gives \$505 gain; hence, the values are \$4040; \$3030; \$2020.

4. A dealer buys pigs at \$5 each and sells \(\frac{1}{2} \) of them at \$6\(\frac{1}{2} \), and the other half at 10\(\frac{1}{2} \) loss. The total gain was \$25. How many pigs did he buy?

Gain on each of 1st half \$1\frac{1}{2}, or \$\frac{1}{2}\$ on each; loss of 10% on 2nd half=5% on all=25c. a pig; ... net gain on each pig=66\frac{1}{2}c.-25c.=41\frac{1}{2}c., or \$25 on 60 pigs.

- 5. Show that the product of 72 and 99 is the product of their L.C.M. and G.C.M.
- 6. A man has two fields; a square one containing 22½ acres, and the other a rectangular field of 31½ acres. A boy rides round the square at 12 miles an hr. Another round the rectangular field in

1 min. longer time. Find the rate per hour of the 2nd boy, if the shorter side of the rectangle is the same as the side of the square.

Side of square=60 rd.; ... sides of rectangle=(60 and 84) rd.; time riding round square=3\$ min.; time riding round rectangle=(3\$+1\$\$) min.=5\$ min.=10 mi. an hr.

- 7. 2, 3, 5, and 7, being known to be factors of a number, what other factors must it have? Ams. 1, 6, 10, 14, 15, 21, 30, 35, 42, 70, 105, 210.
- 5. A note for a certain sum at 4% interest is due in 2½ months. What fractions of the principal are the interest and true discount? Ans. 125 and 121.
- 9. The men in a factory work 10 hr. a day for \$6.50 a week. How much per cent. will the wages be increased for doing the same work, working 9½ hr. per day, and receiving \$6.65 per week?

1st rate is 10tc. per hr.; 2nd rate is 11tc. per hr.; gain= (11t-10t)c.=tc., or 7,2%.

10. Find the publisher profit on the sale of 10400 copies of a book retailing at 70c. The publisher allows 25% discount to the retailer and also gives 18 copies for a dozen, and the cost of printing, binding, etc., is 25c. a copy.

The retailer pays 52 to., but gets 13 for a dozen; net sum received for each copy published=\frac{1}{2} of 52 to.=48 to; net profit=(48 to.=25)e.=25 to. total profit=(10400×23 to)e.=\$2440.

11. A rectangular eistern 4½ ft. long when full contains 28½ c. ft. of water. If the breadth and depth are the same, what will be the cost of lining the inside of the cistern with lead (no lid) at 28c. per sq. ft.f

Breadth and depth, each= $\sqrt{\frac{28\frac{1}{4}}{4\frac{1}{2}}}$ ft.=2 $\frac{1}{2}$ ft.; ... 46 $\frac{1}{4}$ sq. ft. to be lined. Ans. \$12.95.

- 12. Show that the G.C.M. of the squares of two numbers is the square of the G.C.M.
- 13. A boy does in 4 days what a man does in 3 days, but a man gets \$1.40 per day and a boy \$1.00. How much will a man gain if he employs 7 boys for 12 days instead of men?

7 men will do the work in 9 da.; cost=\$88.20; 7 boys will do the work in 12.; cost=\$84.00; saving \$4.20.

14. If I buy G.T.R. stock at 1221, I get \$7 per share of \$100, but if I invest in mining stock at 105, I get \$52 per \$100 share.

The former investment gives me \$185 more income than the latter. Find the amount invested.

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15. A banker's discount on \$4920 for 2½ years is \$615. What will be the true discount on \$18400 for 3 years at same rate, and simple interest?

The banker's rate is 5%; the true discount on \$18400 for 3 yr. at 5%=11 of \$18400=\$2400.

16. Find a number whose square is equal to the sum of the squares of 1392 and 580; also one whose square is equal to the difference of the squares of 1460 and 876, and subtract the one from the other.

1st=1508; 2nd=1168; difference=340.

17. A man meets 5 beggars and he divides a certain sum among four of them in the proportion of 1, 2, 3, 4, with the understanding that each must give the fifth $\hat{\tau}_{s}$ of his share. The fifth gets \$5.25. Find the share of each of the others.

The fifth gets #\$ of the amount the first receives; the first receives #\$ of \$5.25, or \$2.80; etc.

18. A runs 800 yd. in 3 min.; B, 1100 yd. in 4 min. How much start must one give the other to reach the winning post together in a mile race?

A runs a mi. in 6‡ min.; B, in 6‡; . . A must have ‡ min. start or 53‡ yd.

19. A man has an income of \$1660 from capital in 4% stock. He sells out at 119 and buys bonds which pay 5%; find the price of the bonds in order that his income may be \$1700.

He has \$41500 of 4% stock; he sells at 119 and realizes \$49385; bonds must=\$34000 to give \$1700 income; ... price must be 1452.

20. A note for \$24530 drawn March 14th at 9 mo. was discounted at a bank May 12th at 32%. Find the net proceeds.

Time of discount, 219 da.; bank discount is \ of \$\frac{24}{5} of \$\frac{24530}{24530}, or \$478.335; hence net proceeds=\((24530-478.335) = \(\frac{24530}{24051.665}. \)

- 21. The rent of a square field at \$11 per ac. is \$110. Find the cost of fencing it at 15c. a yd. Ams. \$132.
- 22. ABCD is a four-sided field; AB is 48 rd. long; BC, 20 rd.; AC, 52 rd.; and the perpendicular from D on AC, 30 rd. Find the value of the field at \$80 an ac. Ams. \$680.

23. A man on a western eatile ranch increased the number of his cattle in four successive years by \$, \$, \$ and \$ of the number he had at first and at the end of 1st, 2nd and 3rd years respectively. He then had 4000 head. How many had he at first?

of \$ of \$ of a of number at first=4000 head. Ams. 2400

- 24. What is the weight of a circular brass plate 30 in. in diameter and 11 in. thick if 1 c. in. of brace weighs 5 oz.? Ams. 560 lb. 34 08.
- 25. What is the highest cube number contained in 108086, and what is the least number as a multiplier that will make the given number a perfect cube.

Factors of 108086=17°×2×11; ... 17°=4913, the highest cube number, and to make the given number a perfect cube, multiply by 2°×11°, or 484.

26. Two sums of money are divided among A, B and C; each gets & of the first sum; and the 2nd sum is divided in the proportion of 3, 5, 8. A's share is \$53.80 and B's, \$67.80. Find the amount of each sum.

of 1st and A of 2nd=\$53.80; } of 1st and A of 2nd=\$67.80; .'. 2nd=\$112; 1st=\$98.40,

27. The true discount on a sum of money due in 4 mo. at 41% is \$16. Find the interest on the sum for the same time at the same rate.

Interest on \$16 for 4 mo. at 41 % = 340.; .'. interest on the given sum, etc.,=\$16.24.

28. A man invests # of his money at 6%; # at 41% and the rest at 3} %. His income is \$1938. How much did he invest at each rate?

6% on }=1+% on all; 4+% on }=1+% o.. all; 3+% on 1+= 110% on all; ... 445% of his money is \$1988; ... his money=\$42000. 1st=\$12000; 2nd=\$16800; 8rd=\$13200.

29. How deep may a round eistern which is 4 ft. in diameter be made so as to have the same inside surface as a cubical one whose side is 4 ft., and compare their capacities? Ams. 5.3636 ft.; capacity, 1.0536:1.

30. A man invests \$28600, part in 3% stock at 88 and part in 5% railway bonds at 1151. He wishes to get the same income from each investment; how much of each stock must be buy?

\$1 income is received from investing \$29} in the first stock or \$23 to in the second. Hence, \$28600 must be divided in proportion to 29% and 23%. AMS. \$18181% of first and \$10909% of second.

31. The weights of equal bulks of gold and silver being as 15:8 and a bar of gold 2 ft. long 2 in. wide and 3 in. thick weight 100.56 lb.; find the weight of a bar of silver 6 in. long 3 in. wide and 1; in. thick.

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Weight of 1 c. in. of gold is $(100.56 \div 144)$ lb.; weight of 27 c. in. of silver is [$\frac{1}{16}$ of $27 \times (100.56 \div 144)$] lb., or 10.056 lb.

- 33. A man bought a farm and paid for it in 4 equal annual payments, including interest at 5%, of \$3941.35 each. What was the each value of the farm? Ams. \$11490\$.
- 33. A c. in. of iron weighs 100 dr. I have an iron rod 2 in. in diameter, which weighs 119 dr. Find its length. Ans. 24 44 in.
- 34. The interest on a sum of money for 4 yr. is \$281,25, and the true discount for the same time and rate is \$225. Find the sum and rate %.

Interest=discount+interest on discount; ... \$(281.25-225)=\$56.25=interest on discount for 4 yr.; ... rate=6i%; sum \$1125.

85. A man has two chests of mixed green and black teas of 48 lb. and 42 lb. respectively. The proportion of black to green is 13:7 in the first and 18:17 in the second. The two chests are then mixed and 20 lb. green tea added. What will now be the proportions of black and green teaf

of 48 lb.=31½ black and remainder 16½ green; ## of 42=21½ black and remainder 20½ green; now (31½+21½) lb.=52½ lb. black; (16½+20½+20) lb.=57½ lb. green; hence, proportion 12:13.

- 36. If a note for \$11602.50 due in 12 mo. is discounted at 5% true discount, how much more will be paid than if 5% from the whole amount is deducted?
- P. W. of 1st=\$11050; P. W. of 2nd=\$11022.375; difference=
- 37. The accounts of a company show that when 54% of the receipts are used for working expenses, 10% for receive fund, and 6% preference dividend paid on \$1,000,000 of capital, \$120000 remains which is sufficient to pay 2½% on the rest of the capital. Find capital and receipts.

Working expenses and reserve is 64% of receipts; 6% on \$1000000 is \$60000; hence, the remainder is 36% of the receipts -\$60000; the receipts are $\frac{100}{88}$ of \$(120000+60000), or \$500000; capital is $\frac{100}{24}$ of \$120000+\$10000000, or \$5800000.

38. There are two wells, the area of the tops are 20 sq. ft. and 21 sq. ft. respectively. A hose that fills the first in 4 min. would

take 7 min. to fill the 2nd, and the water that would fill the amailer would fill the larger within 15 ft. of the top. Find the depth of each.

4 times larger=7 times smaller; 4 times smaller+ $4(15\times21)$ s. ft.=7 times smaller; 3 times smaller= $4(15\times21)$ s. ft.; smaller=420 s. ft. and $(420\div20)$ ft.=21 ft. the depth, 2nd is 35 ft. deep.

30. A person finds by investing money in G.T.R. bonds paying \$6 per \$100 share, when they are selling at \$132, that he will obtain \$54 more income than by loaning his money at \$27 per cent. per annum. What amount has he for investment?

\$132 cash gives \$5 income; \$100 cash gives \$47 income; a loan of \$100 gives \$37 interest; hence, the gain on \$100 invested in bonds is \$150; ... to gain \$54 he must invest \$4092.

- 40. The Lehigh train 364 ft. long, going 35 mi. per hr., meets the Atlantic Express, 364 ft. long and passes it at 12 o'clock, in 6 see. Then 15% min. later the Lehigh meets the International Limited, 396 ft. long, and passes it also in 6 see. How long before the International Limited will overtake the Atlantic Express? Ams. 15% min. past one.
- 41. A dealer mixes inferior brandy at \$2.88 per gal., with a better quality in the proportion of 3:1, and by selling the mixture at \$3.45 per gal. he realizes 15% gain. Find the price of the good brandy.

If sold at \$3.00 there will be neither gain nor loss; 4 gal. mixture at \$3.00=\$12.00; 3 gal. inferior=3×\$2.88=\$8.64; ... price of good brandy=\$3.36.

42. Two rectangular rooms of equal height were papered. The first was 16 ft. long and 14 ft. wide; the second 14 ft. long by 12 ft. wide. The paper was 21 inches wide and cost 5 to. a yd., and the hanging 1 to. a yd. The whole cost was \$20.16. Find the height of the rooms.

5½ sq. ft. cost 7e.; .'. 2016c. would cover $\frac{2014}{1} \times 5$ sq. ft., or 1512 sq. ft.; 2(16+14)+2(14+12)=112 ft.=distance around both rooms; .'. height= $1512\div112=13$ ft.

43. A nugget weighing 62 os. Avoir., cost \$12\frac{1}{2} per os. After separating the gold from the quarts, it was found that the gold was to the quark as 21:4. The gold was sold at \$19\frac{1}{2} per os. Troy. Find the gain or loss.

Cost=62×6121=4759.50; gold=52.08 oz. Avoir.=4711 oz. Troy; 4711 oz. @ \$191 per oz.=\$917.73; gain=\$(917.73-759.50)=\$158.28.

44. If I buy 50 shares of railway stock at \$53 per share, and 100 more at \$31 per share, and I receive 72c. a share half-yearly as a dividend, what % per annum do I receive?

50 shares at \$62=\$4100; 100 shares at \$31=\$3100; sum invested =\$7200; } yearly dividend=150×72s.=\$108; ... yearly income=\$216, or 3%.

45. I wish to have an income of \$1840 per annum. I can invest in City Gas Co. stock at 87\$ and paying 3% dividend, or in Bank stock which is selling at \$233 and paying a dividend of 7\$% on each share of \$100. How much more would I require to invest in the latter than the former?

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\$\\$\$ income is got from \$87\\$; \$1840 income is got from \$53590. Again, \$7\\$\$ income is got from \$233; \$1840 income is got from \$55920. Additional expenditure in latter is \$2330.

46. A body when weighed in one scale of a false balance weighs 81 oz. and in another 372 oz. What would a merchant gain % by selling goods with such a scale?

Real weight=1/87\$×81=84 oz.; 84 oz. gain (87\$-84) oz.=

47. A circular yard 240 ft. in diameter has a circular plot in the centre whose radius is 32 yd. A driveway is constructed around the outside of the plot and is 24 ft. wide. Find the cost of construction at 27c. per sq. yd.

Area of drive= $[(40^{2}-32^{2})\times4^{2}]$ sq. yd.=1810 \dagger sq. yd.; cost of 1810 \dagger sq. yd. at 27c. is \$488.77 \dagger .

48. A room is 25 ft. long and 15 ft. wide and has a semicircular bow 20 ft. long thrown out on one side; find the area of the whole room.

Area of rectangular part=375 sq. ft.; area of semicircular part = $\frac{1}{10^8 \times \frac{3}{10^8}}$ sq. ft.=157 $\frac{1}{10^8}$ sq. ft.; whole area=(375 $\frac{1}{10^8}$) sq. ft. =532 $\frac{1}{10^8}$ sq. ft.

49. Three boys, A, B and C, start in a 3 mi. race; A goes 32 yd. while B goes 30 yd. and C 22 yd. How far from the winning post will B and C be when A reaches it? Ams. B, 380 yd.; and C, 1650 yd.

50. A invests a certain sum in 2½% stock at 90; B invests an equal amount at 89‡ and his income is \$25 more; find the amount invested by each. Ams. \$128700.

51, An ornament of gold and silver contains 8 je. in. and weighs 64 j oz. A c. in. of gold weighs 10 j oz. and of silver 5 j oz. How much gold is there in the ornament?

If all was gold the weight would be (8\$ × 10\$) on., or 87\$ on.; the actual weight is 64† os.; (87†—64†) os.=22† os. Every os. of silver reduces the weight (10½—5‡) os., or 4† os.; ... 22‡+4‡=5½

No. of e. in. of silver. Weight of gold is [(3†—5½) × 10‡] os.,

52. A has sugar worth \$4.55 per 113 lb.; Bezehanges flour with A for sugar, but gives him only if of the weight to which he is entitled. A finding this out raises the sugar accordingly. What price per lb. does he charge B? Axs. 4jc. a lb.

53. A has \$41030 deposited in the bank at 3%. He takes it out to invest it in G.T.R. 32% stock at 982, and thus increase his income, but before he has time to do so, the banker offers him 2; %, and the stock rises to 93;. How much more would his income be increased by the former than the latter arrangement?

Income from bank=\$1230.90; Income from G.T.B. stock at 932=\$1430.00;

Increase by change=\$(1430-1230.90)=\$199.10; П. Income from stock at 98; #1426.17; Bearly;

Income from bank at 3; % = \$1333.47 ;

Increase by change to stock= \$92.70; ... gain by 1st over 2nd arrangement=\$(199.10-92.70)=\$106.40.

54. A room 44 ft. long, 32 ft. wide has a floor partly covered with earpet, and a margin 4 ft. wide round the outside painted. The carpet and painting together cost \$321.60. The carpet was \$22 per sq. yd. Find cost of painting per sq. ft. Azz. 15c.

55. A man bought 136 pigs; he sold \$ of them at 15% profit; † at 50% profit, and the remainder at a loss of 26%. His gain

altogether was \$19.25. Find the cost of the pigs.

† at 15% gain=6}% gain on all; † at 50% gain=7}% gain on all; † at 25% loss=10}}% loss on all; ... net gain %=(6)+7+-10}}% =3}}%; 3}% % of cost=\$19.25; cost=\$51.25.

56. Divide \$12200 between John and James so that the simple interest on John's for 3 years at 4% will be equal to that on James' for 71 yz. at 5%.

John gets # and James & of the sum; John's, \$10000; James' #3200.

57. At London the mean annual rainfall is estimated at 38 in.; find the side of a subleal reservoir that would hold all the water that falls on to of an acre in one year. Ans. 33 ft.

58. What is the least number when divided by 98 leaves 97 as

remainder, and by 35 leaves 34, and by 49 leaves 48.

The L.C.M. of 98, 85, 49=490; ... 490-1=489=No. divided by 98, 85 and 48, will leave the given remainders. Ams. 460.

- 60. A room is 3 times as long as it is wide, and costs \$20.60 to carpet it at \$1.06 per sq. yd.; the walls are papered at 18c. per sq. yd., and cost \$20.16. Find the dimensions. Ams. 10‡ yd. long, 5‡ wide, 4 yd. high.
- 66. A yard measure made of steel expands ψ_0 of an inch in warm weather and contracts ψ_0 in cold weather; what is the true length of a fence which measures 3ψ in. more in hot than in cold weather?

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- 61. A rectangular piece of lead 16 in. long 10 in. wide and 3 in. thick is melted. Find how many cubes 2 in. each way can be made from it and how many is in. each way can be made from the remainder? Ams. 35 and 7525.
- 62. There are 150 bu. of grain in two bins, and † 1 bin there are 15 bu. less than † as much as there are in t', other. How many bu. are there in the smaller bin?

No. of bu. in larger bin+4 of No. of bu. in larger bin=165 bu. Ans. 45 bu.

63. If 30 c. in. of gunpowder weigh 1 lb., find the diameter of a hollow sphere that will hold 11 lb.

\$×₩×r*=330; .'. r=4.2863 . . . Ams. 8.5726 . . .

64. A bought 16 cows and 120 sheep for \$465, the animals of the same kind costing a uniform price. He sold them for \$496.50, gaining 71% on the cows and 6% on the sheep. Find the cost of each per head.

Total gain is \$31.50; 6% gain on all is \$27.90. Hence, 1\frac{1}{27} of value of cows is \$(31.50-27.90), or \$3.60. Ams. \$15.00; \$1.87\frac{1}{2}.

65. There is a mixture of vinegar and water in the proportion of 93 parts of vinegar and 7 parts of water. How much water must be added so that in 25 qt. of the mixture there may be 2 qt. of water?

was against mixture is 23 qt. Hence, the original mixture was again qt. The new mixture is again qt. Hence, the first mixture has been increased by v of itself.

66. I buy two horses for \$225, and sell one so as to lose 4% and the other so as to gain 5%. If on the whole, I neither gain nor lose, what did each horse cost?

4% of price of 1st=5% of price of second; ... price of 1st=

† of price of second. Ams. \$125; \$100.

67. A laborer was engaged at \$1.25 and his board for each day he worked, but was charged 45c. for each day he was idle. At the end of 47 da. he received \$48.55. How many days did he work?

Sum lost by being idle= $(47\times1.25-48.55)=$10.20$; sum lost by being idle 1 da.=\$1.70. Ann. 41 da.

- 66. Divide \$7804.04 among 3 men, 4 women, and 6 children, so that each woman shall have twice as much as a child, and each man 5 times as much as a woman. What is the share of each? Ams. A man, \$1794.10; a woman, \$358.82; a child, \$179.41.
- 69. A certain number is divided by 9, and the quotient multiplied by 17. The product is then divided by 300, and 23 is added to the quotient. The result is next divided by 3, and to this quotient 19 is added, and the resulting sum divided by 12½. Now † of ‡ of ‡ of this last quotient is 3. Find the original number.

Begin with the last result, 3, and work towards the beginning. Axs. \$1000.

To. Assuming that an express train runs 40 mi. an hour, and an ordinary train 30 mi. an hour, and that the express fare is ic. per mile more than the ordinary fare, find how much a man's time is worth, if it costs him the same to travel by one as by the other.

The extra expense by traveiling 40 mi. by the express train is 10c. The extra time to travel 46 mi. by the ordinary train is ‡ hr. Hence, value of time per hr. is 30c.

71. At a game of skill A can give B 10 points out of 50, and B can give C 10 points out of 50. How many points can A give C out of 50, and yet be sure to winf

When A makes 50, B makes 46; when B makes 40, C makes 32. Hence, A can give (50—32) points, or 18.

72. The population of a certain town increases at a certain rate per cent. per annum. Now it is 194481. Four years ago it was 160000. What will be the population two years hence?

160000×(1+rate)4=194481; rate=5%. Axs. 214415.

73. Gold weighs 19.3 times, and copper 8.89 times as much as water. How many times as heavy as water is a coin containing 11 parts of gold, and 1 part of copper.

No. of times= $(11 \times 19.8 + 1 \times 8.89) \div 12 = 18.4325$.

74. The true discount on a sum of money for one year @ 5% is \$1 greater than the sum of the true discounts of one-half of it @ 4%, and the other half @ 6%. Find the sum.

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vy of sum-vy of half sum+4 of half sum+\$1; hence. (vy-vy-vy) of sum-\$1; sum is \$11575.29.

75. My purse and the money in it are together worth \$66.50. If I spend 121% of my money, and sell the purse for 1 its value, I shall then have \$57.25. Find the value of my purse.

money and # value of purse are worth \$57.25; hence, # money and # value of purse are worth \$9.25; hence, money and 4 times value of purse are worth \$74; 3 times value of purse is worth \$7.50. Ans. \$2.50.

76. A man purchased a farm for \$3000, and agreed to pay principal and interest in 4 equal annual instalments. Interest being 6% per annum, what was the annual payment?

\$1 paid yearly amounts to $\frac{(1.06)^4-1}{1.06-1}$, or \$4.3746;

Debt amounts to $\#[3000 \times (1.06)^4]$, or \$3787.4307; annual payment is #(3787.4307 + 4.3746), or \$865.77.

77. A cube of lead, whose edge is 10 in., is wholly immersed in a cylindrical tub partly filled with water, whose internal diameter is 20 in. How much will it raise the water in the tub?

Area of bottom of tub= $(4^{\circ}\times100)$ eq. in.; hence, depth the water will rise is $[1000+(4^{\circ}\times100)]$ in., or 3° in.

78. A, B and C form a company. A's stock is in trade 3 mo. and he claims is of the gain; B's stock is 9 mo. in trade; and C advances \$3024 for 4 mo., and claims half the profit. How me do A and B contribute?

The profits are $\frac{1}{16}$, $\frac{1}{16}$ and $\frac{1}{16}$, respectively; ... A's stock = $\frac{672 \times 3 \times 5}{6 \times 3}$ =\$1120.

79. A tea merchant mixes 40 lb. of tea @ 45c. per pound, with 50 lb. @ 27c. per pound, and sells the mixture @ 45c. per pound, What per cent. profit does he make? Axs. 284.

80. Divide \$2400 into two parts, such that the annual interest on the first part @ 3\forall \infty, added to that on the second @ 6\forall \infty may equal that on the whole sum @ 5\forall \infty.

52%-32% is 18%; hence, 12% of all is 3% of second part. Ams. \$1000, \$1400.

81. A boat's erew can row 15 ml. down stream in the same time that they can row 7 ml. up it. If their rate of rowing is 5½ ml. an hr. in still water, what is the velocity of the stream?

The rate in still water is to the rate of the stream as 11 to 4; hence, rate of stream is $\frac{4\times5\frac{1}{4}}{11}$ mi. per hr., or $1\frac{19}{11}$ mi.

82. The three per cents. are @ 91‡, and the three-and-one-half per cents. @ 96‡. A person has a sum to invest which will give him £100 more of the former stock than of the latter. Find the difference of income he could obtain by investing in the two stocks.

100×sum 100×sum 91\(\frac{1}{2}\) \(\frac{1}{2}\) \(\frac{1}{2

- 83. A conical tent, whose slant height is 12 ft., requires 66 sq. yd. of canvas to make it. How much ground does the floor of the tent cover? Ams. 779f sq. ft.
- 54. I buy two horses for \$260. If I sell the first at a gain of 5%, and the second at a loss of 5%, I would gain 15%. What was the price of each horse?

My gain is 1500 of \$260, or \$1. Hence, 150 of cost of first 150 of (\$260—cost of first)=\$1. Ams. \$140 and \$120.

- \$5. An agent sold 10 mowing machines @ \$80 each, and 15 @ \$100 each. He paid \$85 for transportation, and, after deducting his commission, remitted \$2100 to his employer. What was the rate of his commission? Ans. 5%.
- 86. A train, 352 ft. long, overtakes a man walking in the same direction, at the rate of 4 mi. per hr., and passes him completely in 15 sec. When going at the same rate, the train passes another man, walking in the opposite direction, in 9 sec. At what rate is the second man walking?

In 15 sec. the first man goes 88 ft.; hence, the train goes 440 ft. in 15 sec., or 264 ft. in 9 sec. In 9 sec. the second man must go (352—264) ft. Ams. 62 mi. per hr.

87. A lady wishing to give 25c. each to some poor women, found she had not money enough by 15c. She gave each of them 20c., and had 35c. left. How much money had she?

(25-20)e. ass to each woman, was (15+35)e. less on the whole. Hence, there were $\frac{40}{2}$ women. Her money was $(10\times25-15)e$., or $\frac{42.35}{2}$.

83. From the first of two cannon, 36 shells are thrown before the second is ready for firing. Shells are thrown from both in the proportion of 8 from the first to 7 from the second. The second requires as much powder for 3 charges as the first does for 4. After how many shots will the quantity of powder consumed by the second equal that consumed by the first?

11 charges of the first are gained every 7 shots of the second, and 36 charges of the first are gained every 189 shots of the second.

While the second is firing 180 shots the first fires 216. Ams. 86+216+189, or 441.

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- 89. How many bricks, each 9 in. long, 4½ in. broad and 4 in. thick, will be required for a wall 80 ft. long, 12 ft. high and 2½ ft. thick, allowing 6½% of the space for the mortar? Ams. 24000.
- 90. A farm cost 32 times as much as a house. By selling the house at a loss of 10%, and the farm at a gain of 74%, \$3993.30 is received. Find the cost of each.

To of cost of house + 75 of 14 of cost of house = \$3993.30. Ans. House, \$612; farm, \$3045.

91. Calculate correctly to 7 places of decimals the value of $\frac{1}{1.2} + \frac{1}{1.2.3} + \frac{1}{1.2.3.4} + \frac{1}{1.2.3.4.5} = 4c.$

$$\frac{1}{1.2} = .500000000$$

$$\frac{1}{1.2.3} = .16666666$$

$$\frac{1}{1.2.3.4} = .04166666$$

$$\frac{1}{1.2.3.4.5} = .00633333$$

$$\frac{1}{1.2.3.4.5.6} = .00138888$$

$$\frac{1}{1.2.3.4.5.6.7} = .00019841$$

$$\frac{1}{1.2.3.4.5.6.7.8} = .000002480$$

$$\frac{1}{1.2.3.4.5.6.7.8.9} = .00000275$$

$$\frac{1}{1.2.3.4.5.6.7.8.9.10} = .000000027$$

$$\frac{1}{1.2.3.4.5.6.7.8.9.10} = .000000002$$

$$\frac{1}{.7182818}$$

92. In firing at a target A hits it twice out of three shots, B three times out of four, and C four times out of five. The target was hit 931 times. If each fired the same number of shots, find how many hits each made and the total number of shots fired.

Out of 60 shots by A there are 40 hits; by B, 45 hits; by C, 48 hits. There are 133 hits out of 180 shots. But there are 7 times 133 hits, hence there are 7 times 180 shots, or 1260, and A hits it 280 times, B 315 times, and C 336 times.

93. The money deposited in a savings bank during the year 1897 was 5% more than that deposited in 1896. In 1896 the deposits were 33% greater than in 1897, while the amount deposited in 1899, exceeded the average of the three previous years by 20%. The aggregate for the four years was \$150937.50. Find the amount deposited in each year.

Sum deposited in 1896+# of this sum+# of # of this sum=#150937.50. Ams. #31250; #32812.50; #43750; #43125.

94. A compound of tin and lead weighs 10.43 times as much as an equal bulk of water, while tin weighs 7.44 times, and lead 11.35 times as much as equal bulks of water. Find the number of pounds of each metal in 765 lb. of the compound.

7.44 times the No. of lb. of tin+11.35 times (765—the No. of lb. of tin)=10.43 times 765. Ans. 180 lb. tin and 585 lb. lead.

95. A circular race-course 22 yd. wide covers 12 acres. Find the diameter of the inner circle. Ans. 818 yd.

96. On March 23rd a bank gave me \$845 for a note of \$860. Interest being charged at 8%, when was the note due?

. The time for which \$15 is the interest on \$860 is 80 days. Axs. June 11th.

97. The map of a country is drawn on a scale of $\frac{1}{12}$ of an inch to a mile. What area on the map will represent 36000 ac. f 36000 a. is represented by $(\frac{26000}{640} \times \frac{1}{140})$ sq. in. Ans. $\frac{24}{64}$ sq. in.

98. A number of men can be formed either into a solid square, or into a hollow square 9 deep having 970 men in the front rank of each side. How many men are there in each side of the solid square?

Number= $\sqrt{9\times[2\times970+2(970-18)]}$ =186.

99. There are three kinds of tea, valued respectively at 32c., 36c., and 42c., per lb. A mixture is to be made containing 6 lb. more of the second than of the first, and 8 lb. more of the third than of the first. What total quantity must be taken that the value of the mixture may be 38c. a lb.?

If there is 1 lb. at 32c., there must be 7 lb. at 36c. and 9 lb. at 42c. These give a mixture in which the gain is greater than the losses by 4 42 9+4=13 l6c. The difference between the gains and losses by taking 1 lb. of each kind is 4c. Hence, 4 lb. in the mixture.

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100. Two cogged wheels work together, there being 16 cogs on one and 27 on the other. The larger wheel makes 80 revolutions in \$ of a minute. How often does the smaller turn in 8 seconds?

No. of revolutions= $\frac{11}{15} \times \frac{8 \times 80}{45} = 24$.

101. A box with a lid is made of material 1 inch thick. If the internal dimensions are 3 ft. by 2 ft. by 1 ft. 5 in. find the number of cubic inches of the material.

Cubic content of interior of box= $(36\times24\times17)$ c. in.=14688 c. in.; cubic content of entire box= $(38\times26\times19)$ c. in.=18772 c. in. Ams. 4084 c. in.

102. The French 20-franc piece weighs 6.45161 grams (a gram =15.43235 grains) and is $\hat{\gamma}_0$ pure gold. The severeign is $\hat{\gamma}_0$ fine, weighs 123.274 grains, and is worth \$4.8665. How much is the 20-franc piece worth?

Value of (11 of 123.274) gr. of pure gold=\$4.8665; weight of pure gold in 20 fr.=(15 of 6.45161×15.48235) gr. Axs. \$3.85...

103. If 76 men and 59 boys can do as much work in 299 days as 40 men and 33 boys can do in 557 days, how many men will do as much work in a day as 15 boys?

The work of (299×76) men and (299×59) boys equals the work of (557×40) men and (557×88) boys. Hence, the work of 15 boys= $\frac{15\times444}{746}$ men=9 men.

104. Find the cost of polishing a marble pillar 2 ft. 4 in. in diameter, and 18 ft. long, at \$1.25 per sq. yd. Ams. \$182.

105. A bought goods at \$5.70 on 4 months' credit, and sold them immediately at \$6.12 on such a term of credit as made his immediate gain 62%. Reckening interest at 4% per annum, how long credit did A give?

If each had been paid, the goods would have been sold for \$6.08; time for 4e. interest on \$6.08 at 4% is 60 days.

106. A bar of gold weighing 196 lb. 10 oz. 10 dwt. is cased in lead weighing 24 lb, 14 oz. Find the weight of the whole in avoirdnpois.

196 lb. 10 os. 10 dwt.=1134000 gr.=162 lb. Ams. 186.875 lb. 107. A person having a certain sum of money to invest finds that an investment in 5 per cent. stock at 117‡ will yield him \$29 more interest annually than an investment in 3 per cent. stock at 92‡. Brokerage being †%, how much money has he to invest?

 $\frac{5 \times \text{sum}}{117\frac{1}{2}} = \frac{3 \times \text{sum}}{92\frac{1}{2}} = $29. \text{ Ams. $2890.50.}$

106. A bought 200 m. of cloth in France at 162 fr. a m.; he paid 194c. a yd. for duty and freight, and sold it in Toronto at \$4.622 a yd. How much did he gain, a franc being 193c. f

Cost of eloth=
$$(200 \times 16\frac{1}{4} \times 19\frac{1}{2})$$
 e. =\$628.33\frac{1}{2};

Duty, etc.= $(\frac{200 \times 39.375}{36} \times 12\frac{1}{2})$ e. =\$27.34\frac{2}{2};

Selling price= $(\frac{200 \times 39.375}{36} \times 462\frac{1}{2})$ e. =\$1011.71\frac{1}{2};

Gain=\$356.04\frac{1}{2}.

100. Each member of a pedestrian club walks as many miles as there are members in the club, and the expense of the trip is for each member as many cents per mile as there are members in the club. The total expense is \$973.86. How many members are there in the clubf Ams. 46.

110. A steel rod 1 ft. long and 1 in. square, weighs 3 lb. and will just support 50 t. What is the greatest length of steel wire, when hung up by one end, will just not break by its own weight?

Length= $\frac{24\times50\times2000}{7}$ in.=5.44 mi.

111. The sum of \$540 is to be divided among 200 persons, consisting of men, women and children. The sums of the men's, women's and children's shares are proportional to the numbers 5, 4, and 3, but the individual shares of a man, woman, and child are proportional to the numbers 3, 2, 1. Find the number of men, women and children.

The men receive \$225, the women, \$180; and the children, \$185.

The number of men is \$ of 75; of women, \$
of 90; of children, \$ of 185.

112. One vessel contains 10 gal. of wins; another contains 10 gal. of water. 1 gal. is taken from each, and is then poured into the other. This is done 3 times. How much wine and how much water will the vessels then respectively contain?

At the end of the first pouring, the first contains \$\frac{1}{10}\$ of 10 gal. of wine; at the end of the second, \$\frac{1}{10}\$ of \$\frac{1}{10}\$ of 10 gal.; and the end of the third, \$\frac{1}{10}\$ of \$\frac{1}{10}\$ of 10 gal., or 7.29. Ans. 7.29 gal. wine; 2.71 gal. water; and 7.29 gal. water and 2.71 gal. wine.

113. The sum of the ages of A and B is now 60 years, and 10 years ago their ages were as 5 to 3. Find their present ages.

Ten years ago the sum of their ages was 40 yr.; A's age was ‡ of 40, or 25; present age is 35.

116. A sum of money is put out at compound interest for 4 yr. During the first two years interest is paid at the rate of 4% per annum, but during the last two years at 5% per annum. The total amount at the end of that time was \$74529. What was the sum invested?

Sum×(1.04)*×(1.05)*=\$74529. Ans. \$62500.

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115. A bought 22% stock at 95. He sold it and with the proceeds bought 32% stock. He obtained \$900 less stock than before, but the same income. How much money did he originally invest?

The of 1st stock—20 of second; 1st stock—17 of (1st stock—4900).

AMS. \$3000.

116. A rectangular solid is hammered until its length is increased 10 per cent., and its width 15 per cent. By how much per cent. has its thickness been diminished?

New this ness is 100 of 110 of old thickness; diminution is 100 of old thickness, or 20.94 . . . %.

117. A founder is required to supply a ton of fusible metal consisting of 8 parts by weight of bismuth, 5 of lead, and 3 of tin. The only bismuth he has in stock is an alloy consisting of 9 parts bismuth, 4 lead, and 3 tin. How much alloy must he take and how much lead and tin must he add to fill the order?

The fusible is to have \$\frac{1}{2}\$ t. bismuth; \$\frac{1}{12}\$ t. lead and \$\frac{1}{2}\$ t. tin. It is evident \$\frac{1}{2}\$ t. will supply the weight of bismuth; but \$\frac{1}{2}\$ t. alloy supplies \$\frac{1}{2}\$ t. lead and \$\frac{1}{2}\$ t. tin; hence, \$(\frac{1}{12} - \frac{1}{2})\$ t. lead, or 180\$ lb. lead and \$(\frac{1}{2} - \frac{1}{2})\$ t. tin, or 41\$ lb. must be taken.

118. If the manufacturer makes a profit of 10%, the wholesale dealer one of 15%, and the shopkeeper one of 20%, what was the cost to the manufacturer of an article bought at a shop for \$75.907

188 of 188 of 188 of cost=\$75.90. Ams. \$50.

119. A train 160 yd. long is overtaking another 150 yd. long on a parallel track. The first is going at the rate of 40 miles an hour and the second at the rate of 18. Find how long a person in the long train will see the other while passing it.

Time= $\frac{150\times60\times60}{22\times1760}$ sec.=13### sec.

120. A trader in London owes a debt of 1000 pistoles to one in Codis. Find what he gains by sending it to him through France, the exchanges being £1=25.4 francs; 19 france=1 Spanish pistoles=£3.

By direct exchange 1000 pistoles—£750; by indirect exchange they—£748 0s. 774vd. \ms. £1 19s. 47fvd.

191. If 60 c. in. of lead, together with 54 c. in. of cork are equal in weight to 1538\$ c. in. of fir, and the weights of equal bulks of lead and fir are represented by the numbers 11.324 and .45, what number represents the weight of an equal bulk of cork?

60×11.234-1-54×No.=1538\$×.46. Ars. .24.

122. A cistern containing 600 gal. measures externally 7 ft. in length, 2 ft. 11 in. in breadth and 5 ft. 6 in. in height. The sides being 1† in. thick, find the thickness of the bottom.

Space cosupled by water is $\frac{6000\times1728}{62\frac{1}{7}}$ e. in. and the depth of the water is $\frac{6000\times1728}{81\times32\times62\frac{1}{7}}$ in., or 64 in. Ans. 2 in.

123. Two trains 92 ft. and 84 ft. long, respectively, when moving with uniform velocities on parallel rails in opposite directions pass each other in 1½ sec., but when they move in the same direction the faster passes the other in 5 sec. Find the rates of speed in mi. per hr.

Bum of rates per hr. = \frac{60 \times 60 \times 176}{5280 \times 176} \text{ mi. = 80 mi.;}

Difference " " \times \frac{60 \times 60 \times 176}{5280 \times 5} \text{ mi. = 24 mi.}

Ans. 52 mi. and 28 mi.

124. The capital of a railway company is \$18500000. It has borrowed \$11500000 at 42% per annum. Its receipts for the year are \$3175000. Its working expenses are 45% of the receipts. What rate of dividend will the shareholders receive for the year, \$55000 being retained as reserve fund?

Cash for dividend is \$(55% of 3175000-41% of 11500000-55000). Ams. 61%.

125. A can reap a field in 15 days, and B in 12 days. The former works a certain time, and is joined by the latter, the whole work being completed in 7½ days. How long did they work together?

A works all the time and does is the work; B does the other half in 6 da. Ans. 6 da.

126. A travels 66 mi. in 3 hr., partly by stage and partly by rail. Had he gone all the way by rail he would have ended the journey an hour sooner and saved ‡ of the time he was on the stage. How far did he go by stage?

Rate by rail is 30 mi. per hr.; the time on the stage is 23 hr., and that on train 2 hr.; distance travelled in train is 15 mi. Axs. 45 mi.

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137. A vessel in the shape of a conic frustum is to hold 3¢ gal. If the diameters of its ends are 10 in. and 6 in. respectively, find the height of the frustum, the gal. being 277.274 e. in.

h(4×25+4×9+4×15)=3+×277.274. Ame. 18.91 in. nearly.

138. The length, breadth and depth of a rectangular wooden box with a lid, are 16 in., 12 in. and 8 in. respectively, and the thickness of the wood is ‡ in. When the box is empty it weighs 3 ib., and when filled with sand it weighs 25 lb. Compare the weight of wood and sand.

Cubic content of box is 1536 c. in., and of sand is 1155 c. in.; hence, 381 c. in. of wood weigh 3 lb., and 1155 c. in. of sand 22 lb. Aws. 105 to 254.

129. A man running at the rate of 10 mi. per hr. towards a point where minute-guns are discharging, finds that 18 min. 45 sec. elapse between his hearing the 1st and 20th reports. Find the velocity of sound.

The man's rate per min. is 880 ft. In 182 min. he runs 16500 ft. This is the distance travelled by sound in 15 sec. Ams. 1100 ft.

130. A builder sells a house to B for \$2480 at a loss of 19%. B disposes of it to C at a price that would have given the builder 17% gain. Find B's gain.

The house cost the builder \$3000 and B's gain is \$(3510-2430).

Ams. \$1080.

131. A lends B a certain sum. At the same time he insures B's life for \$2950.50, paying annual premiums of \$80. At the end of \$ yr., and, just before the fourth premium is to be paid, B dies, having never repaid anything. What sum must A have lent B in order that he may just have enough to recoup himself, together with 5% compound interest on the sum lent and on the premiums paid?

Sum (1.05)*+80[(1.05)*+(1.05)*+1.05]=2950.50. Ams. \$2320.

132. Prove that the difference of any two numbers composed of the same digits is divisible by 9.

If a, b, c, d, etc., are digits of a number the number may be a+10b+100c+1000d, or 10a+100b+1000c+d. The difference, —9a—90b—900c+999d is evidently divisible by 9. The same may be shown for any other arrangement of the digits.

133. An agent sold a consignment of lumber for \$1006 and invested the preceeds, less his commission, in sugar. His total commission on the two transactions amounted to \$312. What rate did he charge, the rates on both sale and purchase being the same?

Commission on \$[4056+(4056-\$12)] is \$312. Ams. 4%.

134. A wholesale merchant allows three equal discounts on purchases. The three are equivalent to a single discount of 48.8%. Find the rate of discount allowed each time.

135. I bought through a broker in Toronto a bill of exchange on Glasgow for £600, paying the broker \$2915.27 for it. At what quotation was the bill purchased, allowing 1% for brokerage?

Cost of bill of £601+ is \$2915.27. Ann. \$4.84+.

136. A person shooting at a target, distant 550 yards, hears the bullet strike the target four seconds after he fires. A spectator, equally distant from the target and the shooter, hears the shot strike the target two and a half seconds after he heard the report. Find the velocity of sound.

Time for ball to go to target and of sound to return to shooter is 4 sec. Time for ball to go to target and for sound to return half distance—time for sound to come from shooter and 2½ sec. Hence, time for ball to go to target is 2½ sec. Hence, sound travels the 550 yd. in 1½ sec. Ams. 1100 ft. per sec.

137. In building a house, A paid 2† times as much for material as for labor. If the latter had cost 8% more, and the former 10% more, the whole cost would have been \$2872.50. Find the actual cost.

188 of cost of labor+188 of 28 times cost of labor is \$2872.50. Ams. \$750; \$1875.

138. A starte to walk from P to Q at the rate of 4 mi. an hr., and 1 hr. afterwards B starts from P and overtakes A in 4 hr. Walking on B arrives at Q 2 hr. before A. Find the distance from P to Q.

B walks at the rate of 5 mi. per hr. In 4 hr. he goes 20 mi. To gain 2 hr. on A he must go 40 mi. Ams. 60 mi.

139. A is 12 yr. older than B. Should they both live 8 yr. longer, B's age will then be 75 of A's. Find the present age of each.

A's age 8 yr. hence is to B's at that time as 10 is to 7. Hence, A's age: (A's-12)::10:7. A will then be 40 yr. Ars. 32 yr. and 20 yr.

140, An 8 gal. cosk is full of brandy, and a 13 gal. cask is full of water. How much must be transferred from each cask to the other that the mixture may be of equal strength?

The contents of each cask must be # brandy and # water. Hence, # of 8 gal. of brandy must be taken out. Ams. 4# gal.

141. A contractor undertakes to execute a certain work in a given time. He employs 55 meu, who work 9 hr. daily. When ‡ of the time has expired, he finds that only ‡ of the work is done. How many men must be now employ 11 hr. a day to fulfil his contract?

The problem is this:—55 men working 9 hr. daily do † of a work in † of a time; how many men working 11 hr. daily can do † of the work in † of the time? Ams. 180.

162. Three men form a partnership, with a capital of \$3200. A's stock was in trade 6 mo., B's 12 mo., and C's 15 mo., and at the settling of accounts, A receives \$240 of the gain, B \$800 and C \$400. Find each person's stock.

A's stock earns \$40 per mo.; B's, \$66‡, and C's, \$26‡. Hence, A has $\frac{40}{133\frac{1}{2}}$ of the capital; etc. Ans. A, \$960; B, \$1600; C, \$640.

. 143. In a pond the top of a plant was 9 in, above the water but forced by the wind the plant leaned over and was submerged at a distance of 3 ft. from where it stood erect. Find the depth of the water.

(Measure of depth+9)2-362=(Measure of depth)2. Ams.

144. A merchant bought 500 lb. of sugar and 80 lb. of tea. The cost of the sugar per lb. was 16‡% that of the tea. He sold the tea at a loss of 8‡% and the sugar at a gain of 25% and gained \$4.25 on the whole transaction. Find the selling prices per lb.

80 lb. of tea=480 lb. of sugar; 91% of 480 times cost of 1 lb. sugar+125% of 500 times cost of 1 lb. sugar=980 times cost of 1 lb. sugar=980 times cost of

145. A ailroad train travels † of the distance at the rate of 30 mi. per hr., the next † of the distance at the rate of 35 mi. per hr., and the remaining distance at the rate of 40 mi. per hr. What is the average rate in mi. per hr.?

If the distance is 3 mi. and each section 1 mi., it will require (30+35+46) of an hr. to run 3 mi.; 3-(36+36+46)=34#\$. Ams.

146. How may 7061 pounds be weighed with the weights, 1 lb., 8 lb., 9 lb., 27 lb., etc., using only one of each kind?

3)7961

Put 1 lb., one 3 lb. wt., one 3 lb. wt. and one 3 lb. wt. and one 3 lb. wt. and one 3 lb. wt., one 3 lb. wt. te balance these.

147. A number of two digits is multiplied by 8, and the product pinced to the left of the original number. Show that the number so formed is always exactly divisible by 7.

If 10a+b represent the number, then 3000a+300b+10a+b will represent the new number. It is evident that this is exactly divisible by 7.

146. A number of men and women earned \$93 a day, each man getting \$2.25, and each women \$1.50. Had there been 6 more men and 7 more women the whole number of women would have earned the same as the whole number of men. Find the actual number of each.

With the additional number of men and women the total sum earned would be \$117. The men carn half of this. Hence, number of men is $58\frac{1}{2}$, or 26, and number of women is $58\frac{1}{2}$, or 39. Axs. 20 and 32.

149. A ditch has to be made 360 ft. long, 10 ft. wide at the top and 3 ft. wide at the bottom, the angle of the slope of each side being 45°. Find the number of c. yd. to be excavated.

By drawing a diagram of a cross section, it will be seen that the depth will be $3\frac{1}{2}$ ft.; No. of e. $yd = \left(260 \times \frac{10+3}{2} \times 3\frac{1}{2}\right) \div 27 = 303\frac{1}{2}$.

150. A dealer bought 100 animals for \$100; ealves @ \$21, lambs @ \$11, and turkeys @ \$1. How many animals were there of each kind?

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2 calves and 6 turkeys average \$1 each;

1 lamb and 1 turkey average \$1 each. Hence,

2 calves, 1 lamb and 7 turkeys average \$1

2 calves, 1 lamb and 7 turkeys average \$1

3 calves, 10 lambs and 70 turkeys will give this average.

Other solutions as 17 calves, 16 lambs and 67 turkeys may be found,

PART V. A TABLE OF SQUARES, CUBES, AND ROOTS.

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